

## **Supplementary Information File**

### **The Boron-doped Scandium Clusters $B@Sc_n^{-/0/+}$ with $n = 2-13$ :**

### **Uncovering the Smallest Endohedrally Doped Cages**

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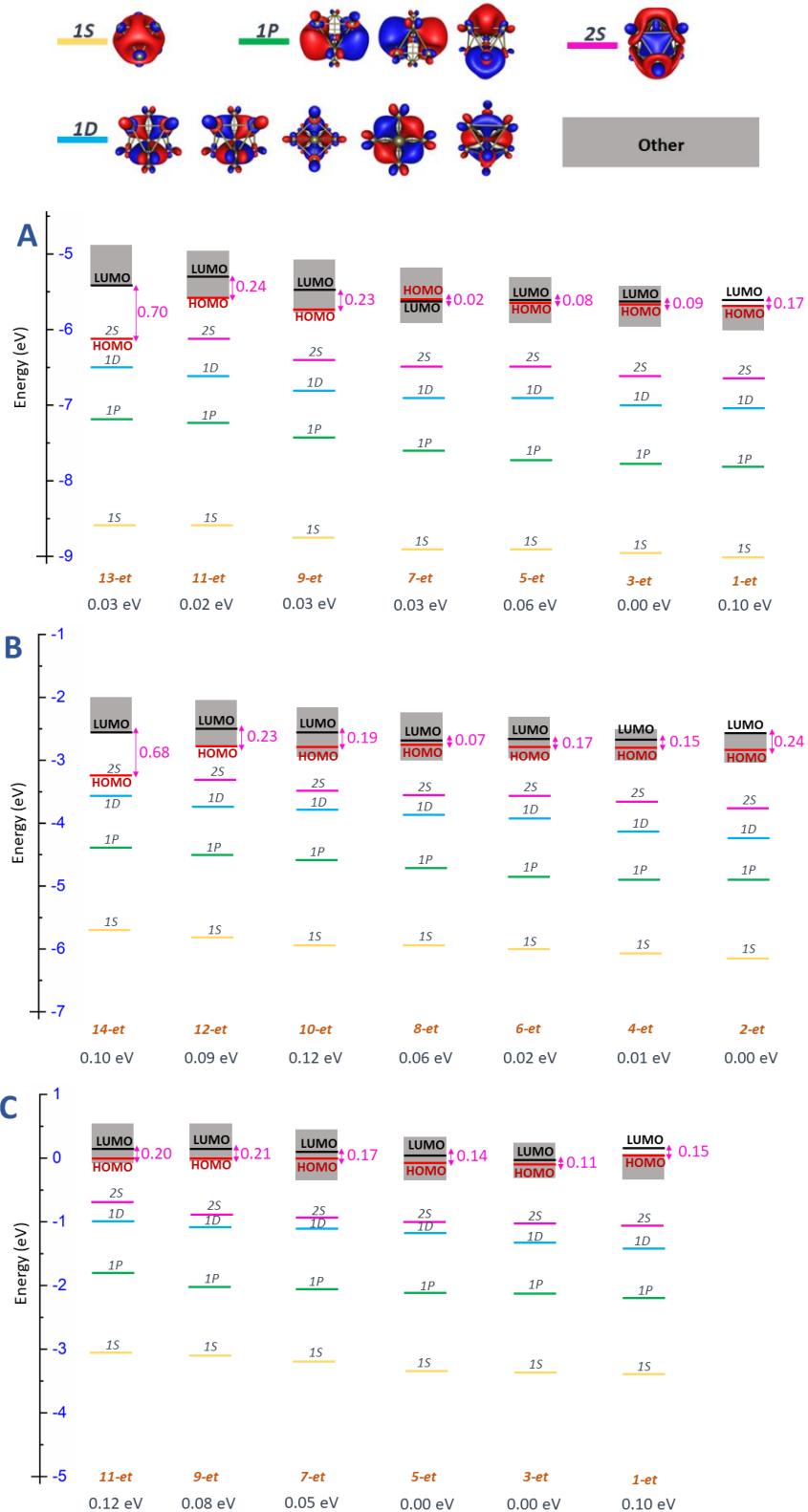
## Content

- Electronic structure and HOMO-LUMO gap (eV) of the  $\text{Sc}_3$  trimer at  ${}^2\text{A}_1'$  state computed using the PBE, B3PW91, PB86, TPSSh and M05 functionals with the def2-TZVP basis set (Table S1).
- The Structures, Multiplicities (M, in bracket) and Relative Energies ( $rE$ , kcal. $\text{mol}^{-1}$ ) of the lowest-lying  $\text{Sc}_n^{+/0/-}$  ( $n = 2-13$ ) clusters calculated at the PBE/ Def2-TZVP theory method (Figure S1).
- The molecular orbital (MO) diagram of the  $\text{Sc}_6^{+/0/-}$ ,  $\text{B}@\text{Sc}_6^{+/0/-}$  and  $\text{Sc}_{11}^{+/0/-}$  at different spin states (Figures S2-S7).
- Calculated density of states (DOS) for the lowest-lying neutral clusters of the  $\text{Sc}_6$ ,  $\text{Sc}_7$ ,  $\text{B}@\text{Sc}_6$  and  $\text{B}@\text{Sc}_7$  isomers (Figures S8 and S9).
- Coordinates of the lowest-lying  $\text{Sc}_n^{+/0/-}$  and  $\text{Sc}_{n-1}\text{B}^{+/0/-}$  ( $n = 2-13$ ) clusters (Pages 12-25).

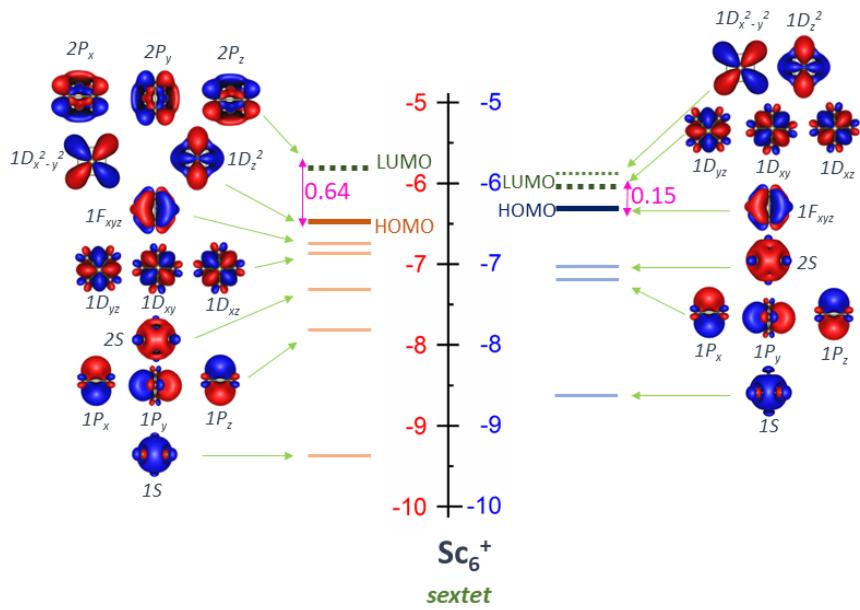
**Table S1.** Electronic structure and HOMO-LUMO gap (eV) of the Sc<sub>3</sub> trimer at <sup>2</sup>A<sub>1'</sub> state computed using the PBE, B3PW91, PB86, TPSSh and M05 functionals with the def2-TZVP basis set.

<b>Functional</b>	<b>Electronic structure</b>	<b>HOMO-LUMO gap (eV)</b>	
		<b>Alpha</b>	<b>Beta</b>
PBE	1S <sup>2</sup> 1P <sup>6</sup> 2S <sup>1</sup>	0.66	0.42
B3PW91	1S <sup>2</sup> 1P <sup>6</sup> 2S <sup>1</sup>	2.07	1.81
BP86	1S <sup>2</sup> 1P <sup>6</sup> 2S <sup>1</sup>	0.68	0.43
TPSSh	1S <sup>2</sup> 1P <sup>6</sup> 2S <sup>1</sup>	1.52	1.19
M05	1S <sup>2</sup> 1P <sup>6</sup> 2S <sup>1</sup>	2.50	1.89

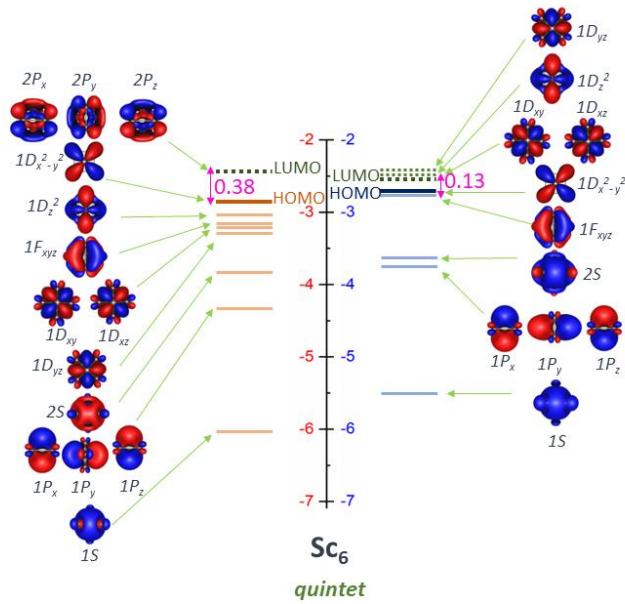
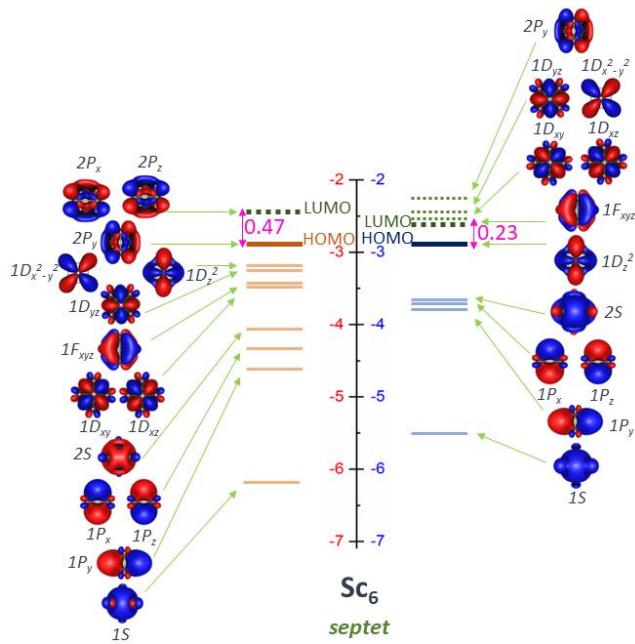




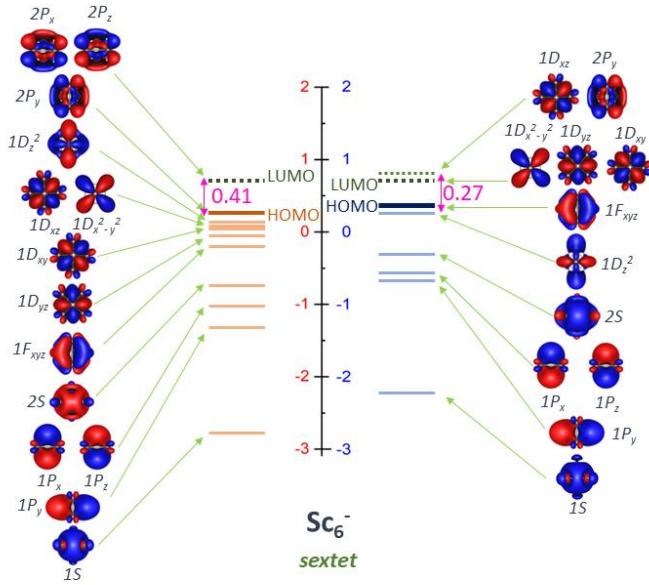
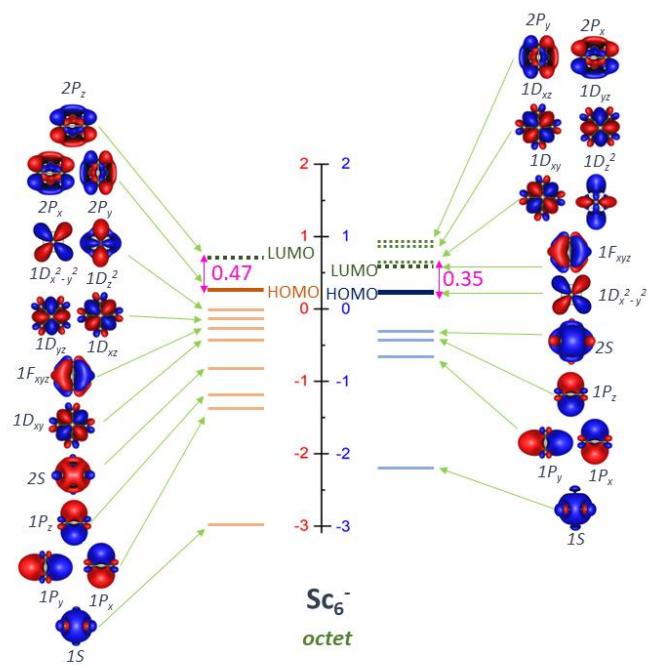
**Figure S2:** The molecular orbital (MO) diagram illustrates the beta side (excluding the singlet state) of the cationic (A), neutral (B), and anionic (C) Sc<sub>11</sub> clusters across different spin states. This analysis was calculated using the PBE/Def2-TZVP method.



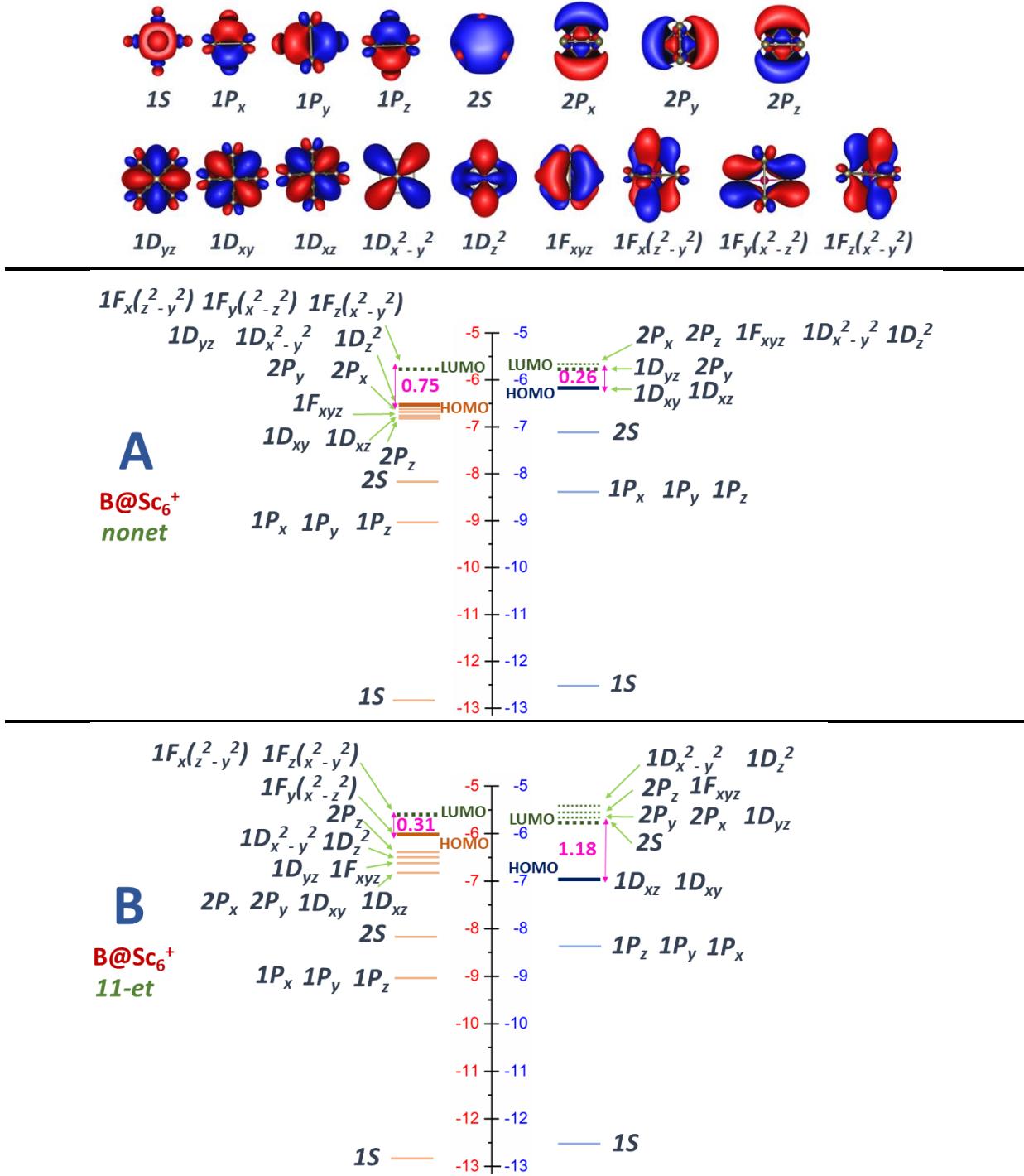
**Figure S3:** Molecular orbital (MO) diagram of cationic  $\text{Sc}_6^+$  cluster at sextet spin state, using the PBE/ Def2-TZVP theory method. Left and right sides denote alpha and beta, respectively.

**A****B**

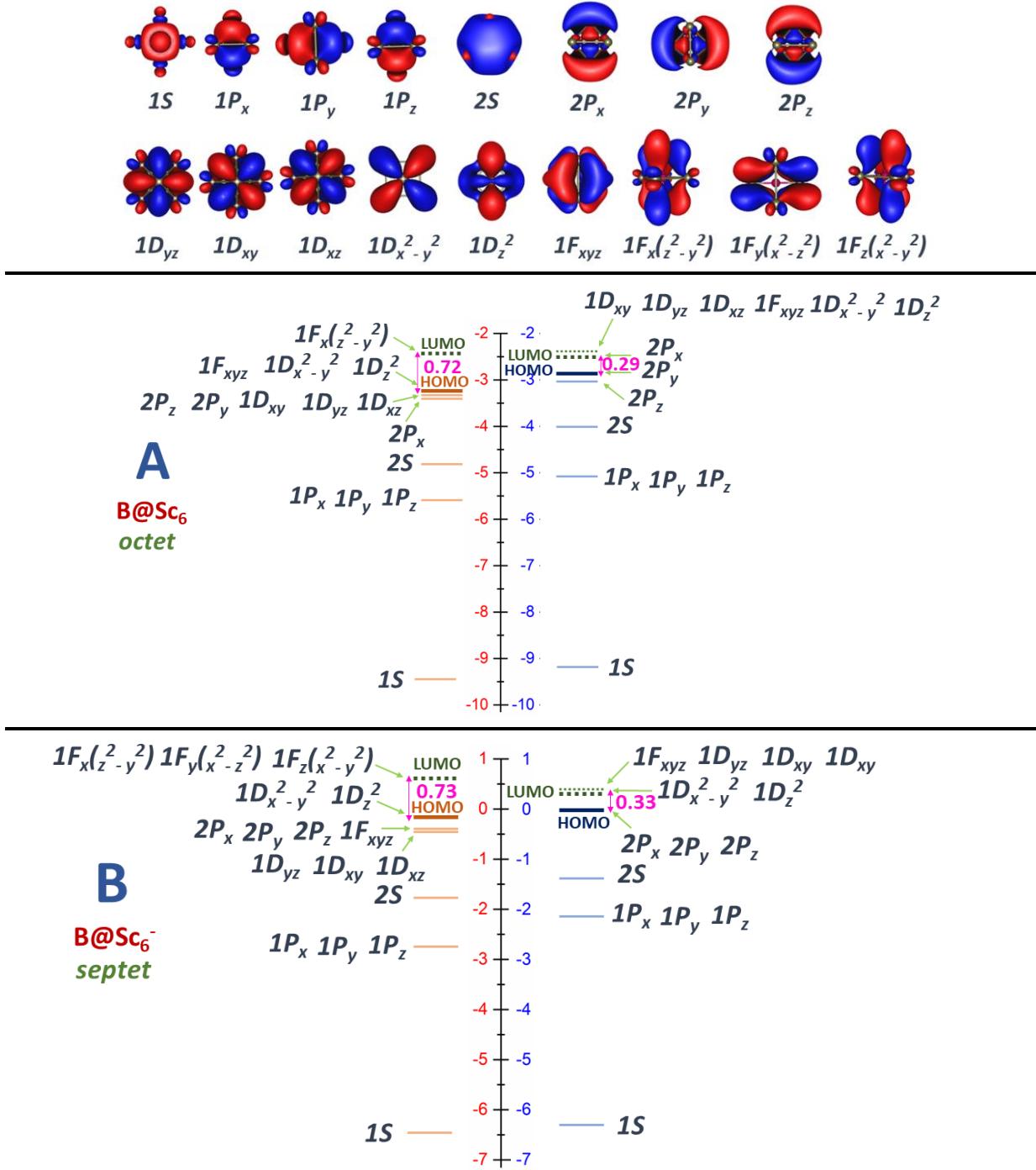
**Figure S4:** Molecular orbital (MO) diagram of neutral  $\text{Sc}_6$  cluster at (A) quintet spin state and (B) septet spin state, using the PBE/ Def2-TZVP theory method. Left and right sides denote alpha and beta, respectively.

**A****B**

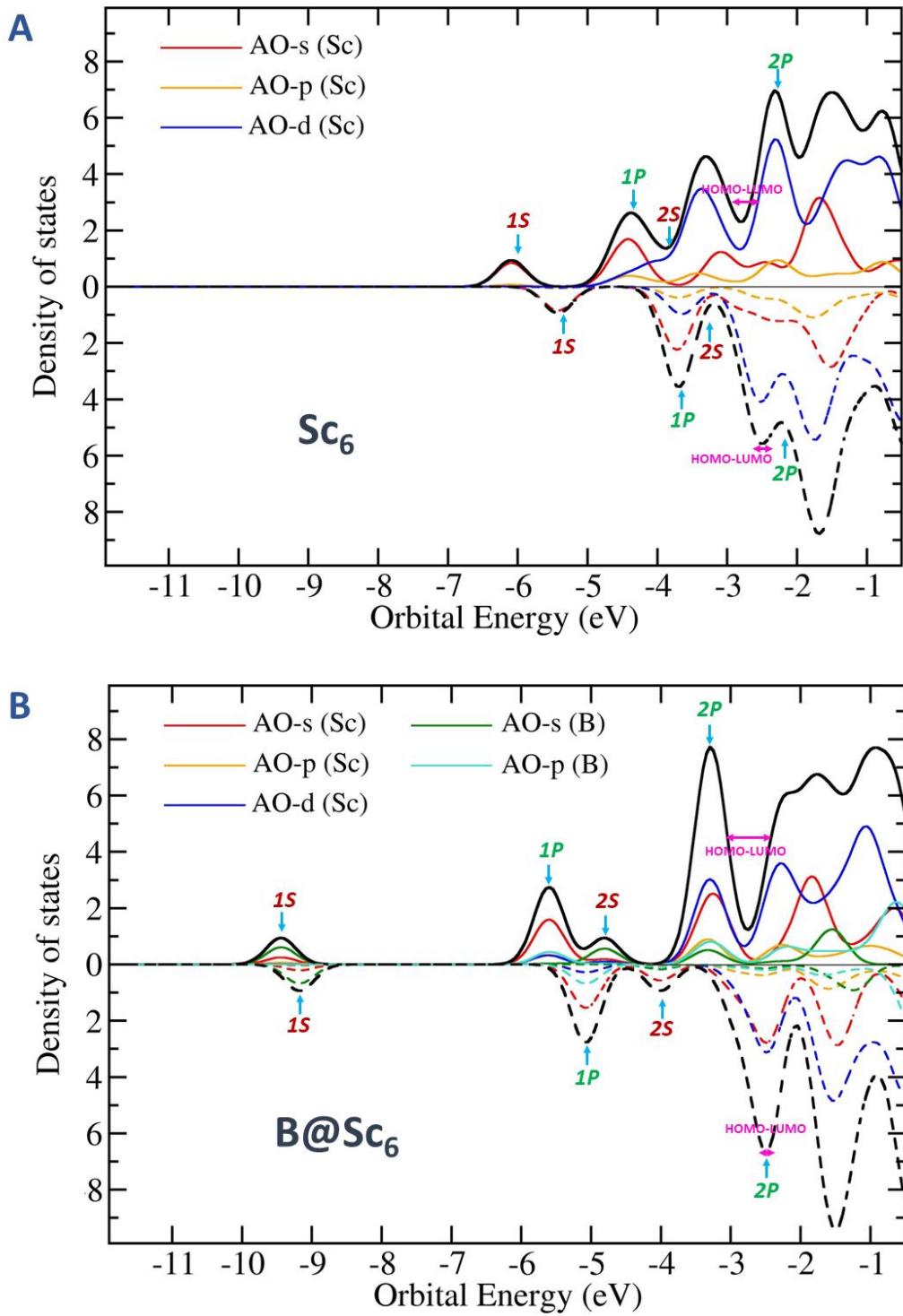
**Figure S5:** Molecular orbital (MO) diagram of anionic  $\text{Sc}_6^-$  cluster at (A) sextet spin state and (B) octet spin state, using the PBE/ Def2-TZVP theory method. Left and right sides denote alpha and beta, respectively.



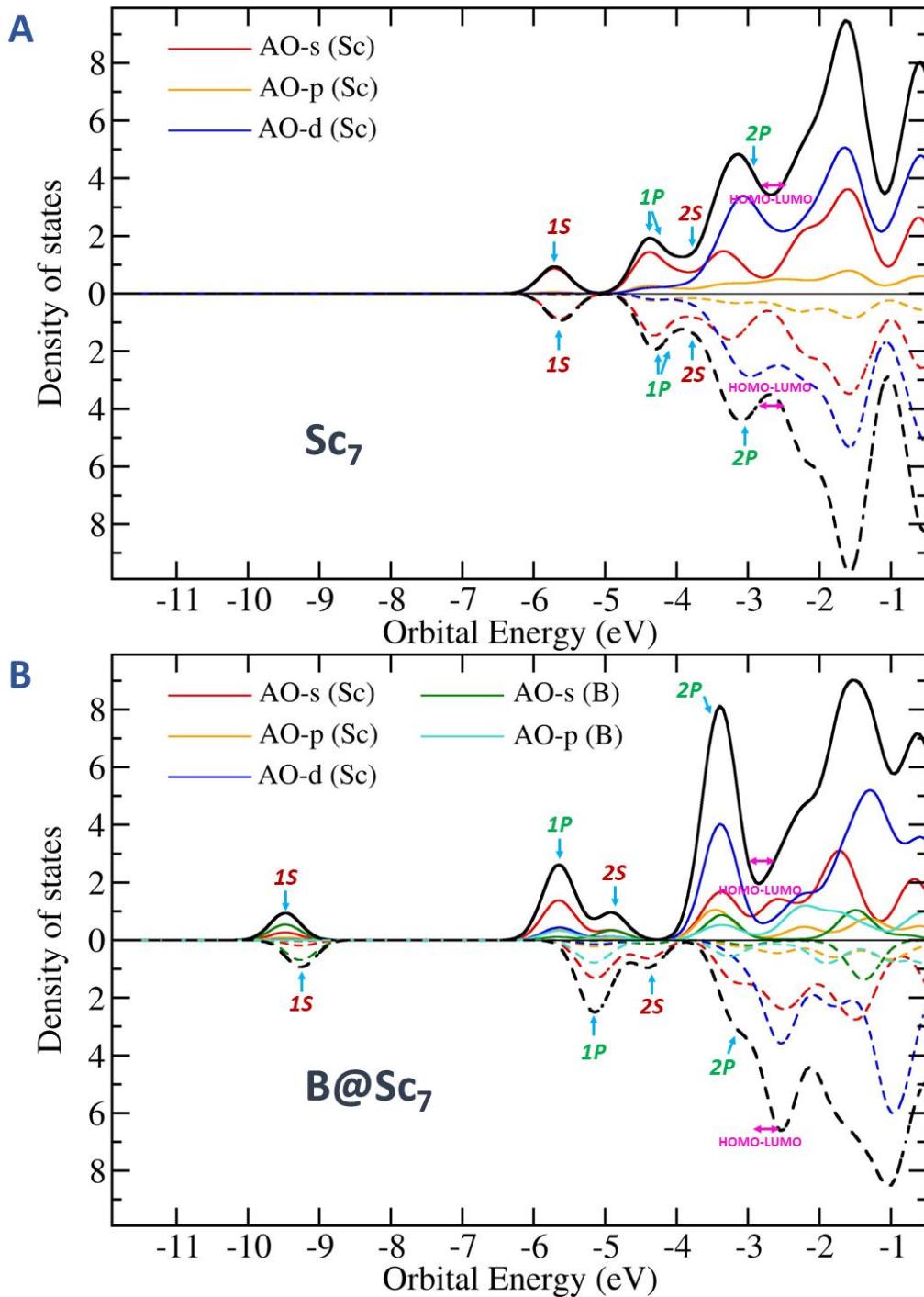
**Figure S6:** Molecular orbital (MO) diagram of cationic B@Sc<sub>6</sub><sup>+</sup> cluster at **A**: a nonet spin state and **B**: a 11-et spin state, using the PBE/ Def2-TZVP method. Left and right sides denote alpha and beta electrons, respectively.



**Figure S7:** Molecular orbital (MO) diagram of **A**: neutral B@Sc<sub>6</sub> cluster at an octet spin state, and **B**: an anionic B@Sc<sub>6</sub><sup>+</sup> at septet spin state, using the PBE/ Def2-TZVP method. Left and right sides denote alpha and beta electrons, respectively.



**Figure S8.** Calculated density of states (DOS) for the lowest-lying neutral clusters of (A) Sc<sub>6</sub>, and (B) B@Sc<sub>6</sub>. Positive and negative DOS represent spin-up and spin-down electrons, respectively.



**Figure S9.** Calculated density of states (DOS) for the lowest-lying neutral clusters of (A) Sc<sub>7</sub>, and (B) B@Sc<sub>7</sub>.

Positive and negative DOS represent spin-up and spin-down electrons, respectively.



<b>Isomer</b>	<b>Spin state</b>	<b>Coordinate</b>			
<b>c.6.A.1</b>	sextet	21	-0.017946000	-0.000016000	2.129820000
		21	-0.017946000	-0.000016000	-2.129820000
		21	-0.017946000	2.129866000	0.0000000000
		21	2.118795000	0.000012000	0.0000000000
		21	-0.017925000	-2.129783000	0.0000000000
		21	-2.047031000	-0.000063000	0.0000000000
<b>n.6.A.1</b>	septet	21	-0.000043000	-2.006274000	-0.321191000
		21	0.000058000	-0.321016000	2.005706000
		21	0.0000853000	2.006239000	0.320759000
		21	-0.0000624000	0.321052000	-2.006070000
		21	2.289598000	-0.0000346000	0.000036000
		21	-2.289842000	0.0000344000	0.0000759000
<b>a.6.A.1</b>	octet	21	-2.213433000	0.177547000	-0.000537000
		21	-0.177675000	-2.213095000	-0.000515000
		21	2.213387000	-0.177690000	0.000363000
		21	0.0000616000	0.000482000	-1.915090000
		21	0.177606000	2.213176000	0.000337000
		21	-0.0000502000	-0.000419000	1.915442000

<b>Isomer</b>	<b>Spin state</b>	<b>Coordinate</b>			
<b>c.7.A.1</b>	septet	21	0.000018000	-0.001250000	1.487865000
		21	2.516477000	0.781278000	0.000000000
		21	-2.516097000	0.783307000	0.000000000
		21	1.583411000	-2.069166000	0.000000000
		21	0.000018000	2.575290000	0.000000000
		21	0.000018000	-0.001250000	-1.487865000
<b>n.7.A.1</b>	doublet	21	-1.583846000	-2.068210000	0.000000000
		21	-0.000025000	-0.014502000	1.392309000
		21	1.561150000	2.090945000	0.000000000
		21	-2.514819000	-0.780583000	0.000000000
		21	-0.000025000	-2.591365000	0.000000000
		21	-1.560806000	2.091232000	0.000000000
<b>a.7.A.1</b>	triplet	21	-0.000025000	-0.014502000	-1.392309000
		21	2.514551000	-0.781225000	0.000000000
		21	0.000112000	0.039048000	-1.415564000
		21	0.004576000	2.590815000	0.000023000
		21	1.531525000	-2.104570000	-0.000004000
		21	-1.538923000	-2.099317000	0.000000000



<b>Isomer</b>	<b>Spin state</b>	<b>Coordinate</b>			
<b>c.10.A.1</b>	octet	21	-0.940898000	-2.236776000	-1.078973000
		21	-2.935491000	-0.006788000	-0.001649000
		21	-0.952974000	2.231691000	1.078478000
		21	1.673938000	0.742368000	2.116749000
		21	1.671797000	2.120493000	-0.737203000
		21	-0.945491000	-1.081171000	2.233620000
		21	1.680296000	-0.733982000	-2.115114000
		21	1.681866000	-2.112336000	0.738631000
		21	-0.948999000	1.076652000	-2.234453000
		21	0.015948000	-0.0000151000	-0.0000086000
<b>n.10.A.1</b>	quintet	21	-3.389667000	0.000012000	0.591587000
		21	-1.838716000	1.623001000	-1.413497000
		21	-1.838883000	-1.622812000	-1.413680000
		21	-0.862528000	-1.504509000	1.392145000
		21	1.536467000	-2.500009000	-0.208099000
		21	1.816459000	0.000005000	1.666747000
		21	3.411057000	-0.000009000	-0.786129000
		21	1.536411000	2.500004000	-0.208107000
		21	-0.862442000	1.504322000	1.392293000
		21	0.491843000	-0.000004000	-1.013259000
<b>a.10.A.1</b>	14-et	21	-0.076133000	2.894901000	-0.171740000
		21	2.616799000	1.603741000	-1.122779000
		21	-2.697444000	1.464028000	-1.122779000
		21	-1.593428000	0.865020000	1.589578000
		21	-2.468939000	-1.513433000	-0.171495000
		21	0.047702000	-1.812301000	1.589616000
		21	0.080645000	-3.068027000	-1.122784000
		21	2.545064000	-1.381566000	-0.171498000
		21	1.545707000	0.947581000	1.589602000
		21	0.000027000	0.000055000	-0.885722000

<b>Isomer</b>	<b>Spin state</b>	<b>Coordinate</b>		
<b>c.11.A.1</b>	triplet	21	-0.373102000	-0.014519000
		21	-1.364468000	1.803081000
		21	1.397979000	-2.181426000
		21	1.402575000	2.169584000
		21	-1.389194000	-1.796198000
		21	1.400074000	0.005274000
		21	-3.292289000	0.013648000
		21	-1.364766000	1.802240000
		21	3.572511000	-0.010754000
<b>n.11.A.1</b>	doublet	21	-1.389343000	-1.795780000
		21	1.400022000	0.004851000
		21	-1.378955000	-1.772319000
		21	1.395131000	-2.175679000
		21	3.560977000	0.002624000
		21	1.413146000	2.187182000
		21	1.404658000	-0.006292000
		21	-3.243785000	-0.009133000
		21	-1.399434000	1.768494000
<b>a.11.A.1</b>	triplet	21	1.404843000	-0.009083000
		21	-1.379367000	-1.770176000
		21	-1.399719000	1.770658000
		21	-0.377495000	0.013722000
		21	-3.540724000	-0.006209000
		21	-1.389931000	0.003979000
		21	-1.378950000	-2.222356000
		21	-1.372934000	2.206633000
		21	-1.389846000	0.003920000

<b>Isomer</b>	<b>Spin state</b>	<b>Coordinate</b>			
<b>c.12.A.1</b>	14-et	21	2.402262000	-1.297230000	-1.525029000
		21	0.488648000	2.667836000	1.029666000
		21	-1.180841000	2.460989000	-1.525816000
		21	-2.385957000	1.289381000	1.030124000
		21	-0.491802000	-2.684779000	-1.525905000
		21	-0.000051000	0.000095000	2.704633000
		21	1.172319000	-2.445584000	1.029880000
		21	-2.706229000	-0.362082000	-1.524866000
		21	-1.963067000	-1.871226000	1.030022000
		21	2.687999000	0.359599000	1.030318000
<b>n.12.A.1</b>	13-et	21	1.976778000	1.882812000	-1.525378000
		21	-0.000059000	0.000190000	-0.227649000
		21	1.272639000	-2.436068000	-1.515501000
		21	0.005036000	0.010475000	2.698981000
		21	-0.397577000	-2.650191000	1.038074000
		21	2.408031000	-1.206759000	1.027431000
		21	1.896301000	1.928625000	1.020066000
		21	2.694422000	0.457834000	-1.517808000
		21	0.404151000	2.693875000	-1.523564000
		21	-1.251253000	2.393866000	1.022351000
<b>a.12.A.1</b>	12-et	21	-2.451708000	1.227375000	-1.514223000
		21	-1.928457000	-1.961847000	-1.518061000
		21	-2.648234000	-0.450865000	1.033456000
		21	-0.003350000	-0.006320000	-0.251201000
		21	-1.029703000	-0.829062000	2.551214000
		21	-1.029549000	2.170280000	-1.576823000
		21	1.515049000	2.758782000	0.000000000
		21	1.514909000	0.852496000	2.623817000
		21	-1.029549000	2.170280000	1.576823000
		21	1.514909000	0.852496000	-2.623817000
		21	1.514909000	-2.231978000	1.621526000
		21	1.514909000	-2.231978000	-1.621526000
		21	-1.029703000	-0.829062000	-2.551214000
		21	0.272575000	0.000108000	0.000000000
		21	-1.029768000	-2.682518000	0.000000000
		21	-2.698987000	0.000155000	0.000000000

Isomer	Spin state	Coordinate		
c.13.A.1	19-et	21	1.871993000	-0.040463000
		21	1.542510000	2.533698000
		21	2.946655000	-0.074110000
		21	1.416050000	-2.605131000
		21	-0.002049000	0.000128000
		21	-1.007146000	-1.611074000
		21	0.904593000	-1.626999000
		21	-1.826123000	0.039946000
		21	-2.973215000	0.074794000
		21	-1.403185000	2.582393000
n.13.A.1	20-et	21	0.984017000	1.570505000
		21	-1.528947000	-2.512454000
		21	-0.925153000	1.668767000
		21	1.438503000	-2.433381000
		21	1.262555000	-1.795633000
		21	-1.336479000	-2.655976000
		21	-1.199459000	-1.349735000
		21	0.000081000	-0.000002000
		21	1.484145000	0.317818000
		21	-3.005902000	-0.042311000
a.13.A.1	19-et	21	-1.438551000	2.433396000
		21	1.336448000	2.655987000
		21	1.199465000	1.349803000
		21	-1.484215000	-0.317822000
		21	-1.262536000	1.795543000
		21	3.005944000	0.042312000
		21	-1.587558862	2.555177126
		21	-2.559630523	0.000000000
		21	0.000000000	-1.589153903
		21	0.000000000	1.589153903
a.13.A.1	20-et	21	1.587558862	-2.555177126
		21	0.000000000	1.589153903
		21	2.559630523	0.000000000
		21	1.587558862	2.555177126
		21	2.559630523	0.000000000
		21	-2.559630523	0.000000000
		21	-1.587558862	-2.555177126
		21	0.000000000	-1.589153903
		21	0.000000000	-2.566961464
		21	0.000000000	0.000000000



<b>Isomer</b>	<b>Spin state</b>	<b>Coordinate</b>		
<b>c.5.B.1</b>	octet	21	-1.695179000	-1.423486000
		21	-1.540827000	1.552168000
		21	1.695100000	-1.423565000
		21	1.540937000	1.552066000
		21	-0.000030000	-0.251659000
		5	-0.000004000	-0.023206000
<b>n.5.B.1</b>	singlet	21	2.056130000	-0.373037000
		21	0.000000000	-0.373022000
		21	-2.056130000	-0.373028000
		21	0.000000000	-0.373022000
		21	0.000000000	1.802414000
		5	-0.000002000	-1.303279000
<b>a.5.B.1</b>	octet	21	1.616509000	1.496268000
		21	-1.617367000	1.495552000
		21	-1.616533000	-1.496211000
		21	1.616982000	-1.495718000
		21	0.000433000	0.000092000
		5	-0.000103000	0.000074000

<b>Isomer</b>	<b>Spin state</b>	<b>Coordinate</b>		
<b>c.6.B.1</b>	nonet	21	1.332383000	-0.430791000
		21	1.330788000	-1.251408000
		21	-1.325301000	1.279866000
		21	1.329365000	1.684446000
		21	-1.324058000	-1.722766000
		21	-1.326704000	0.440753000
<b>n.6.B.1</b>	octet	5	-0.069189000	-0.000420000
		21	-0.000005000	0.056264000
		21	-1.467466000	1.623413000
		21	1.485321000	-1.669130000
		21	1.466782000	1.624032000
		21	-1.484625000	-1.669761000
<b>a.6.B.1</b>	septet	21	-0.000005000	0.056264000
		5	-0.000005000	-0.088549000
		21	1.266439000	1.807870000
		21	1.280353000	-0.801352000
		21	1.294553000	-0.976035000
		21	-1.295702000	1.078329000
		21	-1.267148000	-1.796433000
		21	-1.278533000	0.687637000
		5	0.000158000	-0.000064000
				0.000189000



<b>Isomer</b>	<b>Spin state</b>	<b>Coordinate</b>		
<b>c.9.B.1</b>	doublet	21	-0.001064000	-1.759164000 -1.558603000
		21	-2.562464000	-1.421405000 -0.017611000
		21	-1.528424000	0.889771000 -1.595000000
		21	1.529456000	0.888004000 -1.595092000
		21	0.001753000	2.889722000 0.023959000
		21	2.560729000	-1.424376000 -0.017645000
		21	1.530486000	0.857951000 1.603153000
		21	-1.529448000	0.859768000 1.603085000
		21	-0.001048000	-1.788996000 1.553564000
		5	0.000106000	0.036646000 0.000796000
<b>n.9.B.1</b>	triplet	21	1.590123000	2.626289000 0.000000000
		21	-0.807676000	1.537555000 1.496177000
		21	1.750742000	-0.022736000 1.504189000
		21	1.750742000	-0.022736000 -1.504189000
		21	-0.807676000	1.537555000 -1.496177000
		21	-0.807676000	-1.305411000 -2.258427000
		21	0.692413000	-2.466290000 0.000000000
		21	-0.807676000	-1.305411000 2.258427000
		21	-2.515813000	-0.517775000 0.000000000
		5	-0.157503000	-0.256366000 0.000000000
<b>a.9.B.1</b>	quartet	21	0.881103000	-0.052292000 -2.105217000
		21	0.881096000	0.052601000 2.105210000
		21	-1.633407000	1.526246000 1.452181000
		21	-1.632465000	-1.452457000 1.526589000
		21	-1.632454000	-1.526712000 -1.452358000
		21	0.881234000	-2.105566000 0.052463000
		21	3.100002000	0.000684000 -0.000015000
		21	0.880734000	2.105521000 -0.052454000
		21	-1.633407000	1.451995000 -1.526399000
		5	-0.388233000	-0.000084000 0.000001000

<b>Isomer</b>	<b>Spin state</b>	<b>Coordinate</b>		
<b>c.10.B.1</b>	septet	21	-1.281929000	1.489121000
		21	-1.281938000	1.487626000
		21	1.281925000	-0.001021000
		21	-1.281940000	-1.489098000
		21	3.491863000	0.000024000
		21	-1.281929000	-1.487628000
		21	1.281931000	0.000994000
		21	1.281944000	-2.104934000
		21	1.281940000	2.104920000
		21	-3.491880000	0.000000000
<b>n.10.B.1</b>	doublet	5	0.000054000	-0.000014000
		21	1.279337000	1.482069000
		21	3.523437000	-0.000127000
		21	-1.302741000	0.001460000
		21	-1.259698000	-2.081919000
		21	-1.326422000	-0.001411000
		21	1.279316000	-1.484182000
		21	-3.520770000	0.000007000
		21	-1.259697000	2.081831000
		21	1.295094000	-1.490654000
<b>a.10.B.1</b>	quintet	21	1.295164000	1.492937000
		5	-0.012688000	-0.000041000
		21	-1.275265000	-1.519548000
		21	-3.534487000	0.000035000
		21	-1.275243000	1.519548000
		21	-1.275276000	-1.438622000
		21	1.275256000	0.057113000
		21	1.275234000	-2.091711000
		21	-1.275239000	1.438616000
		21	1.275274000	-0.057141000

<b>Isomer</b>	<b>Spin state</b>	<b>Coordinate</b>			
<b>c.11.B.1</b>	sextet	21	1.497614000	-0.351821000	2.073920000
		21	-0.162913000	2.112840000	1.490569000
		21	-1.422621000	-0.530377000	1.609954000
		21	-3.312117000	-1.893422000	-0.003359000
		21	0.399635000	-2.236058000	0.006683000
		21	-2.890823000	1.447900000	0.006798000
		21	-1.418964000	-0.526078000	-1.613131000
		21	3.457700000	-1.357678000	0.009327000
		21	2.434588000	1.540328000	-0.006436000
		21	-0.160657000	2.110297000	-1.498723000
		21	1.500296000	-0.370994000	-2.074928000
		5	0.328700000	0.231265000	-0.002835000
<b>n.11.B.1</b>	triplet	21	-1.501870000	-0.354248000	2.082680000
		21	-1.497629000	-0.358536000	-2.080960000
		21	0.179535000	2.104566000	-1.454542000
		21	1.399102000	-0.551457000	-1.602387000
		21	0.169284000	2.112852000	1.442318000
		21	3.363602000	-1.843155000	0.001309000
		21	-0.452205000	-2.235040000	0.006446000
		21	2.920541000	1.386818000	0.000594000
		21	1.392687000	-0.534674000	1.612045000
		21	-3.475730000	-1.329342000	-0.003890000
<b>a.11.B.1</b>	quartet	21	-2.416091000	1.553529000	-0.003490000
		5	-0.341158000	0.204486000	-0.000519000
		21	-1.423125000	-0.507235000	1.676808000
		21	-1.423129000	-0.507231000	-1.676809000
		21	-0.111692000	2.121533000	-1.505220000
		21	1.495614000	-0.367101000	-2.055988000
		21	-0.111694000	2.121528000	1.505226000
		21	3.429735000	-1.413485000	0.000006000
		21	0.341699000	-2.231877000	-0.000005000
		21	2.452412000	1.516138000	-0.000005000

<b>Isomer</b>	<b>Spin state</b>	<b>Coordinate</b>		
<b>c.12.B.1</b>	triplet	21	-3.989552000	-0.274172000
		21	-1.334410000	-0.253887000
		21	-2.316435000	2.284651000
		21	-1.359064000	-0.268549000
		21	-2.467635000	-2.677647000
		21	0.618650000	-2.145693000
		21	1.702331000	-0.475738000
		21	1.751972000	-0.375154000
		21	3.614690000	-1.614161000
		21	0.385406000	2.195504000
<b>n.12.B.1</b>	doublet	21	2.842755000	1.315444000
		21	0.399874000	2.224461000
		5	0.635967000	0.272752000
		21	3.974150000	-0.193743000
		21	2.309986000	2.289225000
		21	2.551041000	-2.646297000
		21	1.329356000	-0.267765000
		21	1.328821000	-0.267126000
<b>a.12.B.1</b>	triplet	21	-1.734539000	-0.429367000
		21	-3.595432000	-1.632389000
		21	-0.409929000	2.189124000
		21	-2.876237000	1.336028000
		21	-0.409396000	2.188284000
		21	-1.735115000	-0.427936000
		21	-0.574517000	-2.195294000
		5	-0.664394000	0.240474000
		21	2.751255000	-1.249512000
		21	2.751529000	1.785248000

21 2.751061000 -0.535558000 1.751996000  
 21 0.538619000 0.561781000 -1.836170000  
 21 -0.727085000 2.852529000 -0.658503000  
 21 -0.726397000 -1.995995000 -2.141061000  
 21 -2.483390000 0.518123000 -1.694688000  
 21 -2.482449000 -1.727686000 0.398783000  
 21 -2.482606000 1.208494000 1.296603000  
 21 -0.725996000 -0.856058000 2.799326000  
 21 0.538789000 -1.871319000 0.431652000  
 21 0.538319000 1.310006000 1.404284000  
 5 -1.014924000 -0.000218000 -0.000150000