## **Supplementary Information**

## Design principle for anode stable solid-state electrolytes

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## Supporting note 1. Screened compositional spaces:

To enumerate all possible Li(Na) metal oxide perovskites (Li(Na)-PRX) with prototype formula being  $\text{Li}_{r}(A, \text{Vac})_{1-r}(M_1M_2)_1O_3$ , where A and  $M_1, M_2$  are cations of different sizes. We focus on a subset of the broader perovskite family where these A sites, including mixture of  $Li^+$ with Na<sup>+</sup>, K<sup>+</sup>, Rb<sup>+</sup>, Cs<sup>+</sup>, Mg<sup>2+</sup>, Ca<sup>2+</sup>, Sr<sup>2+</sup>, Ba<sup>2+</sup>, Pb<sup>2+</sup>, Sc<sup>3+</sup>, In<sup>3+</sup>, Y<sup>3+</sup>, La<sup>3+</sup>, Pr<sup>3+</sup>, Nd<sup>3+</sup>, Sm<sup>3+</sup>, Gd<sup>3+</sup>, Er<sup>3+</sup>, Eu<sup>3+</sup>, Dy<sup>3+</sup>, represent a screening of alkali and alkaline earth metals, as well as some lanthanides and transition metals, offering a range of ionic radii and charge states to tune the properties of the perovskite. The M<sub>1</sub>, M<sub>2</sub> species, which include Mg<sup>2+</sup>, Zn<sup>2+</sup>, Ca<sup>2+</sup>, Sc<sup>3+</sup>, In<sup>3+</sup>, Ga<sup>3+</sup>, Al<sup>3+</sup>, Ge<sup>4+</sup>, Ti<sup>4+</sup>, Sn<sup>4+</sup>, Zr<sup>4+</sup>, Hf<sup>4+</sup>, Nb<sup>5+</sup>, Sb<sup>5+</sup>, Ta<sup>5+</sup>, Mo<sup>6+</sup>, W<sup>6+</sup>, Te<sup>6+</sup>, are primarily transition metals and metalloids. These elements typically have smaller ionic radii compared to the A species and occupy the octahedral sites in the perovskite structure. The overall structure of Li(Na) disordered rocksalt-type metal oxides (Li(Na)-DRX) materials with the prototype formula of Li being  $\operatorname{Li}_{1+x+\delta}(M_1M_2)_{1-x}O_2$  is derived from the perovskite architecture by the choice of cations and the stoichiometry. For Li(Na) metal halides (Li(Na)-MH), we consider the following metal species M: Mg<sup>2+</sup>, Ca<sup>2+</sup>, Zn<sup>2+</sup>, La<sup>3+</sup>, Al<sup>3+</sup>, Ga<sup>3+</sup>, In<sup>3+</sup>, Sc<sup>3+</sup>, Y<sup>3+</sup>, Ge<sup>4+</sup>, Hf<sup>4+</sup>, Zr<sup>4+</sup>, Ti<sup>4+</sup>, Sn<sup>4+</sup>, Nb<sup>5+</sup>, Ta<sup>5+</sup>, Sb<sup>5+</sup>. Overall, we have examined of 16,644 compositions across three typical structures: 3,846 compositions for Li(Na)-PRX, 1,238 compositions for Li(Na)-DRX and 11,560 compositions for Li(Na)-MH, respectively.

Facets	$\mu_{Li/Na}$ (eV/atom)	$\mu_{Zn}$ (eV/atom)	$\mu_0$ (eV/atom)
Li10Zn4O9-Li6ZnO4-Zn	-3.220	-1.260	-8.582
Li <sub>6</sub> ZnO <sub>4</sub> -Li <sub>2</sub> O-Zn	-3.078	-1.260	-8.794
Li <sub>2</sub> O-Zn-LiZn <sub>3</sub>	-2.593	-1.260	-9.764
Li <sub>2</sub> O-LiZn <sub>3</sub> -LiZn	-2.223	-1.383	-10.505
Li <sub>2</sub> O-LiZn-Li	-1.909	-1.697	-11.132
$Na_{10}Zn_4O_9$ - $Na_6ZnO_4$ - $NaZn_{13}$	-1.579	-1.298	-8.821
Na <sub>6</sub> ZnO <sub>4</sub> -Na <sub>2</sub> O-NaZn <sub>13</sub>	-1.444	-1.308	-9.021
Na <sub>2</sub> O-NaZn <sub>13</sub> -Na	-1.323	-1.318	-9.264

**Table S1.** The chemical potentials for all elements in facets of phase diagram for Li-Zn-O and Na-Zn-O systems.

Table S2. The formation energy of competing phases in phase diagram of Li-Zn-O and Na-Zn-O.

Competing phases	Formation energy	Competing phases	Formation energy
	(eV/atom)		(eV/atom)
$Li_{10}Zn_4O_9$	-1.992	Na <sub>10</sub> Zn <sub>4</sub> O <sub>9</sub>	-1.634
Li <sub>6</sub> ZnO <sub>4</sub>	-2.036	Na <sub>6</sub> ZnO <sub>4</sub>	-1.552
Li <sub>2</sub> O	-2.062	Na <sub>2</sub> O	-1.439
LiZn <sub>3</sub>	-0.171	NaZn <sub>13</sub>	-0.054
LiZn	-0.219		

Facets	$\mu_{Li/Na}$ (eV/atom)	$\mu_{Sb}$ (eV/atom)	$\mu_{Br}$ (eV/atom)
Sb-LiBr-Li <sub>2</sub> Sb	-2.865	-4.129	-4.353
Li <sub>3</sub> Sb -LiBr -Li <sub>2</sub> Sb	-2.717	-4.425	-4.501
Li <sub>3</sub> Sb-LiBr-Li	-1.909	-6.849	-5.355
Sb-NaBr-NaSb	-2.160	-4.129	-4.489
NaSb-NaBr-Na <sub>3</sub> Sb	-1.856	-4.433	-4.793
Na <sub>3</sub> Sb-NaBr-Na	-1.326	-6.034	-5.326

**Table S3.** The chemical potentials for all elements in facets of phase diagram for Li-Sb-Br andNa-Sb-Br.