

Supplementary Information

Guidelines for designing high-deformability materials for all-solid-state lithium-ion batteries

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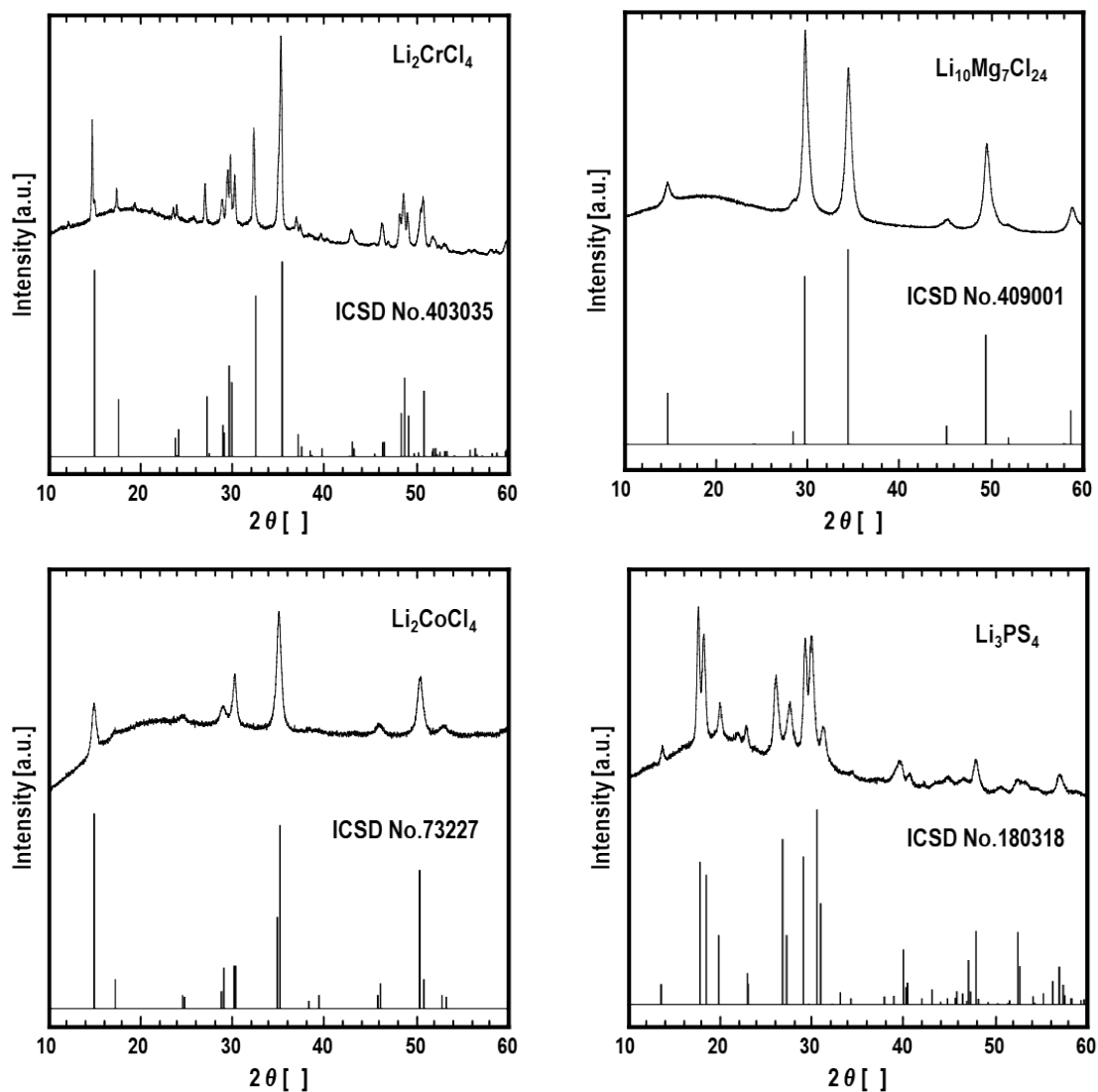


Fig. S1. XRD patterns of the four materials synthesised in this study (Li_2CrCl_4 , $\text{Li}_{10}\text{Mg}_7\text{Cl}_{24}$, Li_2CoCl_4 , and Li_3PS_4). The peaks for all four materials are consistent with those listed in the inorganic crystal structure database (ICSD), confirming that the target materials were successfully synthesised.

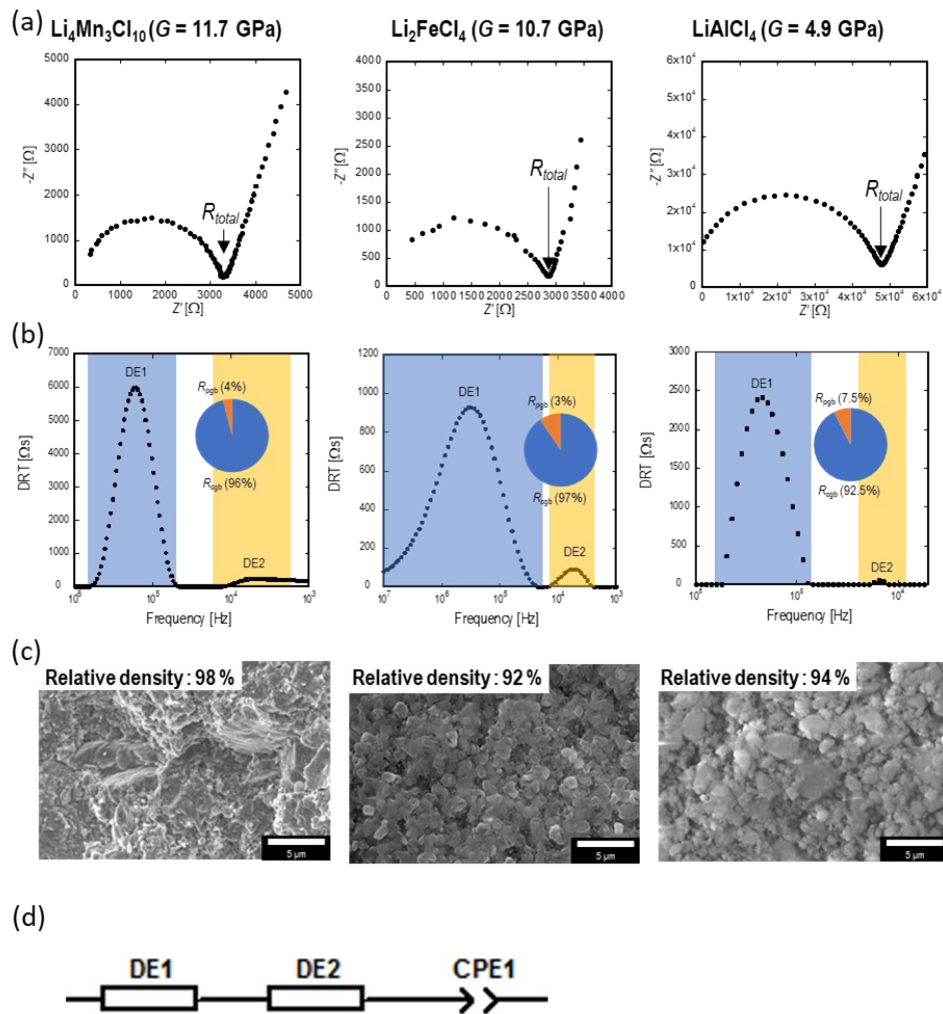


Fig. S2. Characterisation of pellets of the chlorides $\text{Li}_4\text{Mn}_3\text{Cl}_{10}$, Li_2FeCl_4 , and LiAlCl_4 . (a) AC impedance results (Nyquist plots). (b) DRT spectra. The pie chart shows the relative magnitudes of the crystallite grain boundary resistance R_{cgb} and particle grain boundary resistance R_{pgb} . (c) Cross-sectional SEM images of the pellets; the relative densities are indicated. (d) Equivalent circuit used for fitting.

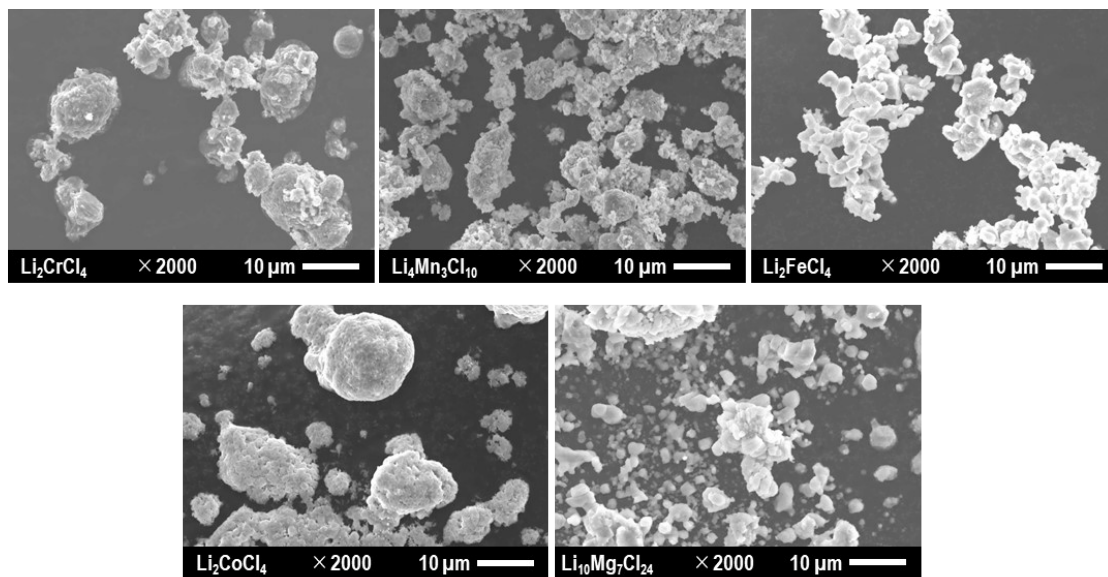


Fig. S3. Cross-sectional SEM images of Li_2CrCl_4 , $\text{Li}_4\text{Mn}_3\text{Cl}_{10}$, Li_2FeCl_4 , Li_2CoCl_4 , and $\text{Li}_{10}\text{Mg}_7\text{Cl}_{24}$ powders.

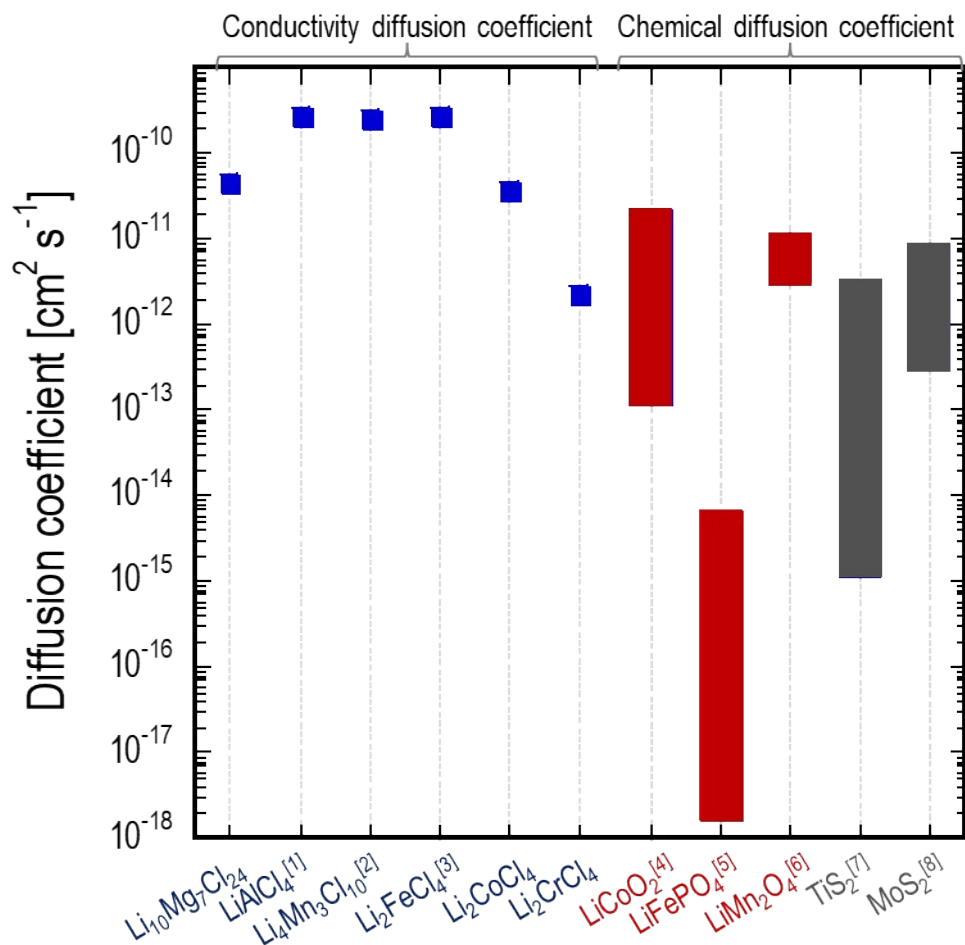


Fig. S4. Diffusion coefficients of the chloride materials (Li₁₀Mg₇Cl₂₄, LiAlCl₄,¹ Li₄Mn₃Cl₁₀,² Li₂FeCl₄,³ Li₂CoCl₄, and Li₂CrCl₄) computationally screened in this study, and typical oxide (LiCoO₂,⁴ LiFePO₄,⁵ and LiMn₂O₄⁶) and sulfide (TiS₂⁷ and MoS₂⁸) cathode materials. The chloride materials generally exhibit higher Li diffusivity than the typical oxide and sulfide cathode materials. Moreover, the chloride materials exhibit even larger Li chemical diffusion coefficients because those calculated from ionic conductivity assuming a thermodynamic factor of unity are often underestimated.

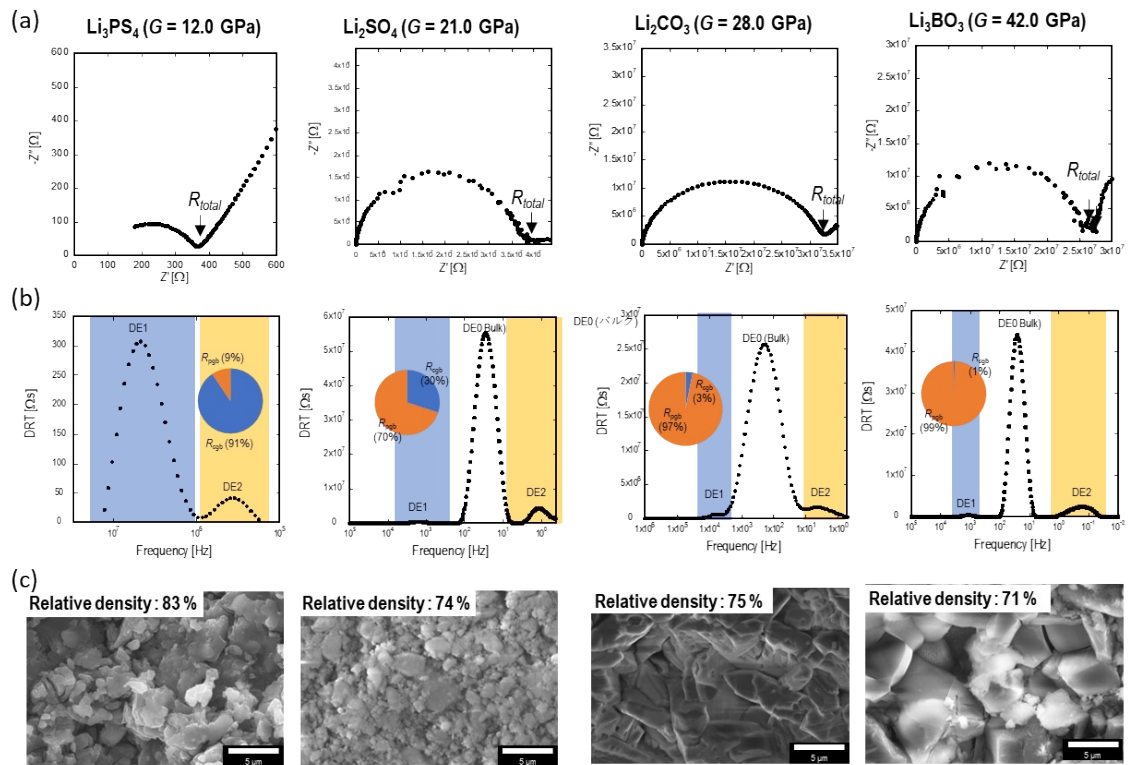


Fig. S5. Characterisation of pellets of the sulfide Li_3PS_4 and oxides Li_2SO_4 , Li_2CO_3 , and Li_3BO_3 . (a) AC impedance results (Nyquist plots). Measurements for Li_2SO_4 and Li_3BO_3 were performed at an elevated temperature (100 °C) owing to their high resistivity. (b) DRT spectra. The pie chart shows the ratio of crystallite grain boundary resistance R_{cgb} and particle grain boundary resistance R_{pgb} . (c) Cross-sectional SEM images of the pellets; the relative densities are indicated.

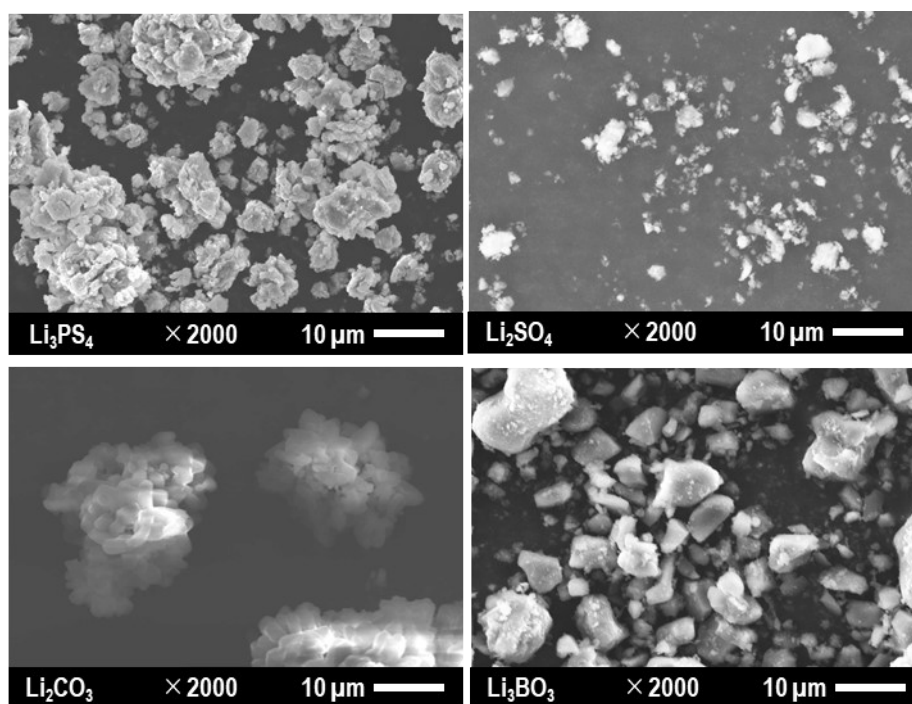


Fig. S6. Cross-sectional SEM images of the sulfide Li_3PS_4 and oxide Li_2SO_4 , Li_2CO_3 , and Li_3BO_3 powders.

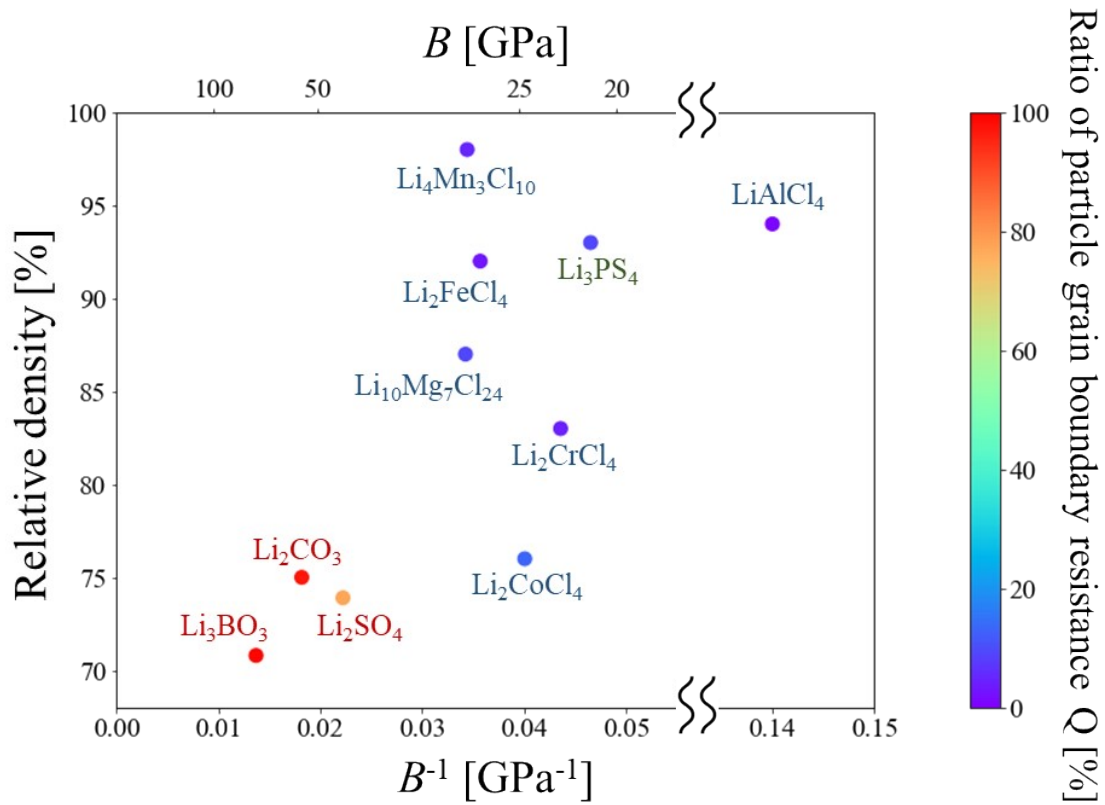


Fig. S7. Relationship among volumetric modulus B , relative density of the pellets, and ratio of particle grain boundary resistance to the total grain boundary resistance, Q , for the nine materials, including the six chlorides that were the focus of this study, that is, Li_2CoCl_4 , Li_2CrCl_4 , $\text{Li}_{10}\text{Mg}_7\text{Cl}_{24}$, $\text{Li}_4\text{Mn}_3\text{Cl}_{10}$, Li_2FeCl_4 , and LiAlCl_4 , as well as the oxides Li_2SO_4 , Li_2CO_3 , and Li_3BO_3 and the sulfide Li_3PS_4 .

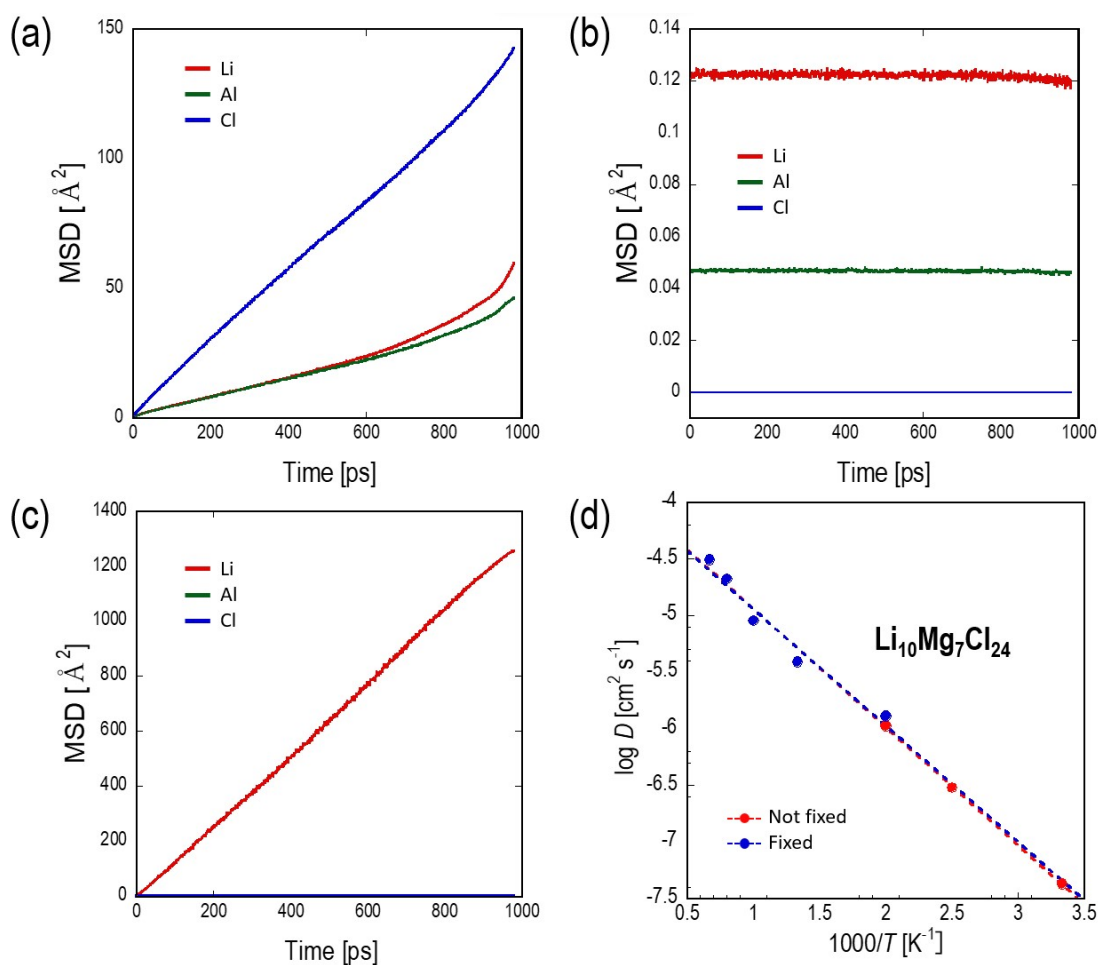


Fig. S8. Mean square displacement (MSD) plots from a representative Li-chloride molecular dynamics calculation (LiAlCl_4 , mp-22983) performed using a high-throughput force field.⁹ (a) MSD plot at 500 K obtained without fixing the anion positions. (b) MSD plots at 500 K obtained with the anion positions fixed. (c) MSD plot at 1000 K obtained with the anion positions fixed. (d) Arrhenius plots of diffusion coefficients obtained via molecular dynamics calculations using a high-throughput force field for a representative example of an LiCl material ($\text{Li}_{10}\text{Mg}_7\text{Cl}_{24}$, mp-530738). Red data points indicate the results of calculations at 300, 400, and 500 K obtained without fixing the anion positions. The blue data points show the results of calculations performed at 500, 750, 1000, 1250, and 1500 K obtained with the anion positions fixed.

Supplementary note: Li diffusivity evaluation via molecular dynamics (MD)

simulations

In this study, molecular dynamics (MD) simulations were performed with the skeletal structure fixed, that is, the coordinates of the chlorides were fixed. This was because the melting points of chloride materials are low; therefore, the skeletal structure may collapse at the high temperatures commonly utilised in MD calculations. For example, Fig. S8 shows the results of MD simulations for LiAlCl_4 . The melting point of LiAlCl_4 is 433 K. As can be observed in the mean square displacement (MSD) plot, LiAlCl_4 melts at 500 K with chlorine diffusion (Fig. S8(a)). Moreover, the frequency of Li diffusion events may not be sufficient to obtain statistics for calculating the Li diffusion coefficient at temperatures below 430 K. Therefore, the anion structure was fixed, and the Li diffusion coefficient was calculated via MD simulations at high temperatures. Fig. S8(c) shows the MSD plot from the MD calculation at 1000 K. Although no diffusion was observed for any element at 500 K (Fig. S8(b)), Li alone was observed to diffuse at 1000 K. The Li ion conductivity at 298 K calculated from the extrapolation of the Arrhenius plot in the high-temperature region with the ion positions fixed was $5.9 \times 10^{-7} \text{ S cm}^{-1}$, which is close to the experimental value ($1 \times 10^{-6} \text{ S cm}^{-1}$). Furthermore, in the Arrhenius plot of the $\text{Li}_{10}\text{Mg}_7\text{Cl}_{24}$ (mp-530738) diffusion coefficient (Fig. S6(d)), the straight line for the data obtained with the anion positions fixed is almost identical to that for the data obtained without fixing the anion positions. This indicates that fixing the anion positions does not significantly affect the diffusion coefficient. Therefore, in this study, the MD simulations were performed at five temperatures (500, 750, 1000, 1250, and 1500 K) with the chloride ion positions fixed. The Li diffusion coefficients were calculated from the MSD slopes of other samples. Samples with an MSD slope of

almost zero, even at 1500 K, were considered to have zero ionic conductivity.

Table S1. Calculated values of Li diffusion coefficient $D_{Li,RT}$, energy above hull E_{Hull} , and shear modulus G for each of the Li–Cl compounds.

Material id	Chemical formula	$D_{Li,RT}$ [$\text{cm}^2 \text{s}^{-1}$]	E_{Hull} [eV atom $^{-1}$]	G [GPa]
mp-998591	LiSnCl ₃	1.55×10^{-36}	0.008448336	5.461882569
mp-998230	LiSnCl ₃	1.12×10^{-17}	0.018967877	6.755421796
mp-989583	Rb ₂ LiInCl ₆	4.08×10^{-11}	0	12.00356415
mp-989579	Rb ₂ LiTiCl ₆	9.14×10^{-13}	0.015591515	12.70132622
mp-989512	LiTi ₂ InCl ₆	2.47×10^{-10}	0	14.51342755
mp-686087	Li ₃ (Nb ₂ Cl ₃) ₈	3.09×10^{-11}	0.012968019	-
mp-686004	Li ₃ SeCl ₆	1.16×10^{-17}	0.012203	12.72936733
mp-685992	Li ₂ CrCl ₄	5.65×10^{-9}	0.073214274	12.92982901
mp-680167	LiMo ₆ Cl ₁₃	1.25×10^{-7}	0.01127676	2.976522323
mp-677135	Li ₂ CoCl ₄	0	1.648672956	20.28624775
mp-676752	Li ₂ FeCl ₄	5.11×10^{-9}	0.202861054	6.430357728
mp-676683	Li₂FeCl₄	8.77×10^{-9}	0.031559694	10.68975814
mp-676361	Li ₃ ErCl ₆	3.50×10^{-17}	0	14.43590228
mp-676210	LiTiCl ₃	6.89×10^{-11}	0.095064055	-20.4548349
mp-676109	Li ₃ InCl ₆	5.31×10^{-23}	0	12.51176384
mp-675460	LiTiCl ₃	1.87×10^{-7}	0.27596539	17.30447897
mp-606711	Cs ₃ LiCl ₄	8.73×10^{-7}	0.059343854	8.416746373
mp-571666	CsLi ₃ Cl ₄	2.58×10^{-21}	0.028389297	10.7010079
mp-571612	LiW ₆ CCl ₁₈	0	0.012219054	-
mp-571527	Cs ₂ LiInCl ₆	2.62×10^{-9}	0	10.28838333
mp-571390	Cs ₂ LiCl ₃	3.63×10^{-21}	0.024857768	9.841205638
mp-570869	LiNb ₃ InCl ₉	2.48×10^{-18}	0.002247427	10.41429913
mp-570512	LiWCl ₆	7.54×10^{-14}	0.012143757	-
mp-569117	CsLi ₂ Cl ₃	4.60×10^{-9}	0.019124206	9.933433151
mp-567652	Cs ₂ LiYCl ₆	4.67×10^{-6}	0	12.45602124
mp-567474	Li₂CrCl₄	6.57×10^{-9}	0.049856652	13.63073846
mp-532443	Li ₅ V ₅ Cl ₁₆	2.49×10^{-8}	0.180230588	11.18693553
mp-531376	Li₄Mn₃Cl₁₀	5.45×10^{-8}	0.00403793	11.77195623
mp-530738	Li₁₀Mg₇Cl₂₄	4.35×10^{-8}	0.020200601	12.71821553
mp-505391	Li ₆ CoCl ₈	1.05×10^{-31}	0.030864541	19.90232217

mp-38684	Li ₂ MgCl ₄	4.10×10^{-11}	0.006588491	12.76243794
mp-38008	Li ₂ CdCl ₄	8.22×10^{-6}	0.010504225	11.08787898
mp-36330	Li ₂ VCl ₄	2.03×10^{-10}	0.011353206	12.39279916
mp-34457	Li ₂ CoCl ₄	6.91×10^{-11}	0.141976284	18.731053
mp-34148	Li ₂ MnCl ₄	8.66×10^{-15}	0.006057414	11.91999236
mp-29985	LiNb ₆ Cl ₁₉	1.96×10^{-17}	0	5.889648047
mp-29582	Li ₂ CrCl ₄	1.91×10^{-10}	0.046454547	10.3183314
mp-29344	LiGaCl ₃	5.83×10^{-18}	0	10.35414277
mp-29250	Li ₆ VCl ₈	0	0.012617101	19.91762251
mp-28828	Li ₆ FeCl ₈	2.60×10^{-14}	0.092345903	19.03395232
mp-28463	LiNb ₃ Cl ₈	1.72×10^{-9}	0	12.25143066
mp-28341	LiGaCl ₄	9.24×10^{-10}	0	4.231483787
mp-28243	RbLiCl ₂	2.30×10^{-18}	0.002885881	9.422648507
mp-28122	LiGdCl ₄	0	0.00259213	10.43546087
mp-28068	LiDy ₂ Cl ₅	1.96×10^{-19}	0.190573681	15.61583524
mp-23416	Li ₂ ZnCl ₄	4.41×10^{-15}	0.012703998	12.51940231
mp-23364	CsLiCl ₂	6.16×10^{-7}	0.012217325	8.678754387
mp-23361	Li ₅ CrCl ₈	1.45×10^{-8}	0.011215566	15.582161
mp-22983	LiAlCl₄	1.54×10^{-11}	0	4.947485309
mp-22980	Li₂CoCl₄	5.72×10^{-12}	0.017858303	17.37988247
mp-22961	Li ₂ ZnCl ₄	0	0.017143571	16.64195843
mp-1222796	Li ₂ CoCl ₄	4.74×10^{-10}	0.156567239	20.73531746
mp-1222745	Li ₂ FeCl ₄	0	0.1518639	12.77729035
mp-1211124	Li ₆ NiCl ₈	6.22×10^{-17}	0	20.11273463
mp-1210931	LiFeCl ₄	1.39×10^{-9}	0	5.778377258
mp-1210835	Li ₂ BeCl ₄	6.47×10^{-15}	0.00851579	14.83897918
mp-1206553	Rb ₂ LiRuCl ₆	9.83×10^{-11}	0	3.510010077
mp-1206403	Rb ₂ LiVCl ₆	9.50×10^{-23}	0.02154604	14.31397569
mp-1206399	Rb ₂ LiVCl ₆	5.89×10^{-11}	0	-0.906828953
mp-1206187	Rb ₂ LiRhCl ₆	1.47×10^{-10}	0	5.051879921
mp-1205883	Rb ₂ LiHoCl ₆	3.02×10^{-9}	0.002265448	12.70792524
mp-1205649	LiSc(TlCl ₃) ₂	0	0	14.72005544
mp-1198972	Li ₆ Zr ₆ HCl ₁₈	7.60×10^{-31}	0.020682633	16.04785159
mp-1190687	CsLi ₂ Cl ₃	6.56×10^{-22}	0.001272549	7.136903266

mp-1189625	Cs ₂ LiScCl ₆	4.85×10^{-8}	0	11.30032817
mp-1188344	CsLiCl ₂	1.36×10^{-8}	0	7.253265462
mp-1120734	Cs ₃ LiCl ₄	6.76×10^{-13}	0.214779303	6.123746748
mp-1114583	Rb ₂ LiYCl ₆	0	0.00494897	12.22078602
mp-1114579	Rb ₂ LiTaCl ₆	2.24×10^{-14}	0.112382972	14.53427949
mp-1114571	Rb ₂ LiNdCl ₆	1.65×10^{-16}	0.032174464	11.06247265
mp-1114567	Rb ₂ LiLaCl ₆	3.02×10^{-9}	0.042283446	9.016485169
mp-1114566	Rb ₂ LiErCl ₆	4.43×10^{-23}	0.000185609	13.06959628
mp-1114565	Rb ₂ LiDyCl ₆	1.06×10^{-8}	0.003880535	12.595736
mp-1114562	Rb ₂ LiBiCl ₆	5.54×10^{-8}	0	11.24792255
mp-1114431	Rb ₂ LiTbCl ₆	2.60×10^{-13}	0.005710754	12.42760706
mp-1114429	Rb ₂ LiScCl ₆	1.48×10^{-9}	0	13.92881696
mp-1114428	Rb ₂ LiSbCl ₆	8.99×10^{-24}	0	11.77810497
mp-1114423	Rb ₂ LiMoCl ₆	2.08×10^{-21}	0	13.60593862
mp-1114421	Rb ₂ LiLuCl ₆	2.93×10^{-16}	0	16.93907393
mp-1114417	Rb ₂ LiCeCl ₆	0	0.084097757	9.833513203
mp-1114414	Rb ₂ LiAuCl ₆	0	0.124259526	7.598634616
mp-1114176	K ₂ LiTaCl ₆	9.53×10^{-8}	0.144685504	13.74853025
mp-1113945	Na ₂ LiAuCl ₆	4.21×10^{-14}	0.233189439	3.954990039
mp-1113921	Na ₂ LiErCl ₆	8.49×10^{-29}	0.118538205	12.25557094
mp-1113912	Na ₂ LiInCl ₆	2.52×10^{-12}	0.131522275	11.56953232
mp-1113903	Na ₂ LiScCl ₆	0	0.103259453	13.46057812
mp-1113898	Na ₂ LiTlCl ₆	2.21×10^{-15}	0.137094961	11.27047756
mp-1113840	Na ₂ LiLaCl ₆	2.32×10^{-9}	0.176806233	9.645898997
mp-1113839	Na ₂ LiDyCl ₆	5.75×10^{-18}	0.11895373	11.77114339
mp-1113837	Na ₂ LiBiCl ₆	7.14×10^{-33}	0.121728747	10.16847696
mp-1113742	Na ₂ LiYCl ₆	0	0.125927748	12.22403797
mp-1113318	Na ₂ LiTbCl ₆	2.24×10^{-10}	0.122539436	11.92362953
mp-1113317	Na ₂ LiSbCl ₆	2.26×10^{-7}	0.145280272	9.91495411
mp-1113316	Na ₂ LiLuCl ₆	1.05×10^{-15}	0.112977848	13.13890121
mp-1113026	Cs ₂ LiAuCl ₆	0	0.126226952	9.229461978
mp-1113018	Cs ₂ LiDyCl ₆	1.90×10^{-9}	0	12.5318003
mp-1113012	Cs ₂ LiMoCl ₆	1.76×10^{-10}	0.031926	12.64319487
mp-1113004	Cs ₂ LiScCl ₆	0	0.011216129	13.45870136

mp-1112999	Cs ₂ LiTiCl ₆	9.73×10^{-11}	0.017419603	12.60102971
mp-1112669	Cs ₂ LiTbCl ₆	3.25×10^{-11}	0	12.4310478
mp-1112613	Cs ₂ LiErCl ₆	6.71×10^{-6}	0	12.78116225
mp-1111932	K ₂ LiScCl ₆	4.51×10^{-14}	0	13.99036943
mp-1111678	K ₂ LiAuCl ₆	0	0.140470215	6.06137832
mp-1111675	K ₂ LiCeCl ₆	2.49×10^{-6}	0.056584505	56.37672967
mp-1111672	K ₂ LiInCl ₆	1.42×10^{-12}	0.02724929	12.00041516
mp-1111666	K ₂ LiMoCl ₆	3.86×10^{-11}	0.037788106	13.48223181
mp-1111664	K ₂ LiSbCl ₆	1.02×10^{-19}	0.039358543	11.00633077
mp-1111660	K ₂ LiTiCl ₆	2.01×10^{-18}	0.036989102	12.27761852
mp-1111654	K ₂ LiYCl ₆	2.89×10^{-5}	0.026140421	11.7428968
mp-1111288	Li ₃ InCl ₆	1.86×10^{-9}	0.266298984	11.24132776
mp-1111284	Li ₃ ScCl ₆	0	0.244241486	13.03989689
mp-1111273	K ₂ LiEuCl ₆	2.68×10^{-25}	0.042051628	4.393139049
mp-1111262	Li ₂ ScCuCl ₆	1.20×10^{-14}	0.273103071	10.03021651
mp-1111261	K ₂ LiBiCl ₆	0	0	6.57466444
mp-1111259	K ₂ LiDyCl ₆	1.75×10^{-9}	0.025984887	12.1829594
mp-1111257	K ₂ LiLaCl ₆	2.36×10^{-21}	0.071879093	10.23133184
mp-1111256	K ₂ LiErCl ₆	1.97×10^{-18}	0.020649807	12.82853398
mp-1111149	Li ₃ SbCl ₆	1.34×10^{-10}	0.293585337	10.37733826
mp-1111130	K ₂ LiTbCl ₆	1.82×10^{-7}	0.032657765	11.8677904
mp-1111126	K ₂ LiLuCl ₆	3.26×10^{-11}	0	12.40319891
mp-1111123	Li ₃ InCuCl ₆	1.08×10^{-8}	0.259715712	9.716304577
mp-1111120	Li ₂ CuSbCl ₆	3.09×10^{-11}	0.288497732	9.226022992

Table S2. Conductivity diffusion coefficients obtained from AC impedance measurements for six chlorides (Li_2CoCl_4 , Li_2CrCl_4 , $\text{Li}_{10}\text{Mg}_7\text{Cl}_{24}$, $\text{Li}_4\text{Mn}_3\text{Cl}_{10}$, Li_2FeCl_4 , and LiAlCl_4).

Chemical formula	$D_{\text{Li, RT}}$ [cm^2s^{-1}]
$\text{Li}_{10}\text{Mg}_7\text{Cl}_{24}$	4.8×10^{-11}
LiAlCl_4	2.8×10^{-10}
Li_2CrCl_4	2.3×10^{-12}
$\text{Li}_4\text{Mn}_3\text{Cl}_{10}$	2.6×10^{-10}
Li_2FeCl_4	2.8×10^{-10}
Li_2CoCl_4	3.8×10^{-11}

Table S3. Resistance decomposition results for the chlorides Li_2CoCl_4 , Li_2CrCl_4 , $\text{Li}_{10}\text{Mg}_7\text{Cl}_{24}$, $\text{Li}_4\text{Mn}_3\text{Cl}_{10}$, Li_2FeCl_4 , and LiAlCl_4 . DE-*R*, DT-*T*, and DE-*C* indicate the resistance, relaxation time, and capacitance, respectively, obtained from DRT analysis. *d*, C_{cb} , and *Q* indicate the crystallite size calculated using the Halder–Wagner method, capacitance of the crystallite grain boundary estimated using the Brickwork model, and resistance ratio of the particle grain boundary.

Compound	DE1- <i>R</i> / Ω	DE1- <i>T</i> / s	DE1- <i>C</i> / F	DE2- <i>R</i> / Ω	DE2- <i>T</i> / s	DE2- <i>C</i> / F	<i>d</i> / Å	C_{cb} / F	<i>Q</i> / %
Li_2CoCl_4	2.6×10^4	3.6×10^{-6}	1.4×10^{-10}	4.2×10^3	3.6×10^{-4}	8.5×10^{-8}	111	1.1×10^{-10}	13
Li_2CrCl_4	2.2×10^5	2.9×10^{-5}	1.3×10^{-10}	9.7×10^3	4.0×10^{-3}	4.1×10^{-7}	290	2.9×10^{-10}	4
$\text{Li}_{10}\text{Mg}_7\text{Cl}_{24}$	6.9×10^4	8.8×10^{-6}	1.3×10^{-10}	6.8×10^3	1.8×10^{-3}	2.6×10^{-7}	115	1.2×10^{-10}	9
$\text{Li}_4\text{Mn}_3\text{Cl}_{10}$	3.2×10^3	9.6×10^{-7}	3.0×10^{-10}	1.9×10^2	5.8×10^{-5}	3.1×10^{-7}	152	1.5×10^{-10}	4

Table S4. Resistance decomposition results for the sulfide Li_3PS_4 and oxides Li_2SO_4 , Li_2CO_3 , and Li_3BO_3 . DE-*R*, DT-*T*, and DE-*C* indicate the resistance, relaxation time, and capacitance, respectively, obtained from DRT analysis. *d*, C_{cb} , and *Q* indicate the crystallite size calculated using the Halder–Wagner method, capacitance of the crystallite grain boundary estimated using the Brickwork model, and resistance ratio of the particle grain boundary.

Compound	DE1- <i>R</i> / Ω	DE1- <i>T</i> / s	DE1- <i>C</i> / F	DE2- <i>R</i> / Ω	DE2- <i>T</i> / s	DE2- <i>C</i> / F	<i>d</i> / Å	C_{cb} / F	<i>Q</i> / %
Li_3PS_4	2.6×10^2	2.4×10^{-8}	9.2×10^{-11}	27	5.7×10^{-7}	2.1×10^{-8}	98	9.8×10^{-11}	9
Li_2SO_4	8.4×10^5	1.3×10^{-3}	1.6×10^{-9}	2.8×10^6	9.7×10^{-2}	3.6×10^{-8}	320	3.2×10^{-10}	77
Li_2CO_3	1.3×10^4	2.5×10^{-6}	2.0×10^{-10}	7.2×10^5	2.2×10^{-2}	3.1×10^{-8}	355	3.6×10^{-10}	97
Li_3BO_3	2.6×10^4	1.0×10^{-5}	3.9×10^{-10}	4.2×10^6	2.4×10^{-2}	5.7×10^{-9}	325	3.3×10^{-10}	99

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