

## Supporting Information

### Two-dimensional azulenoid kekulenes based metallic allotropes for energy storage applications

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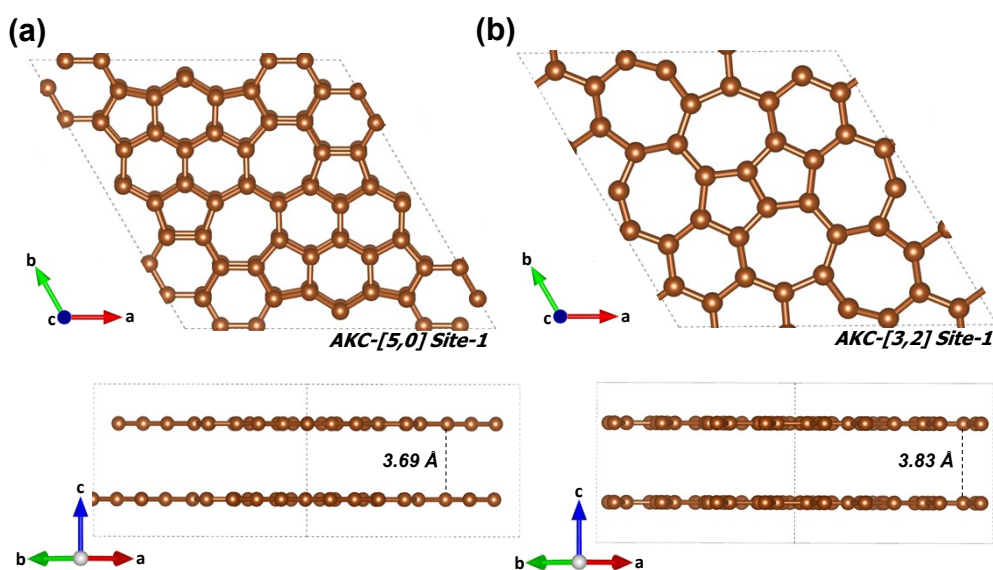
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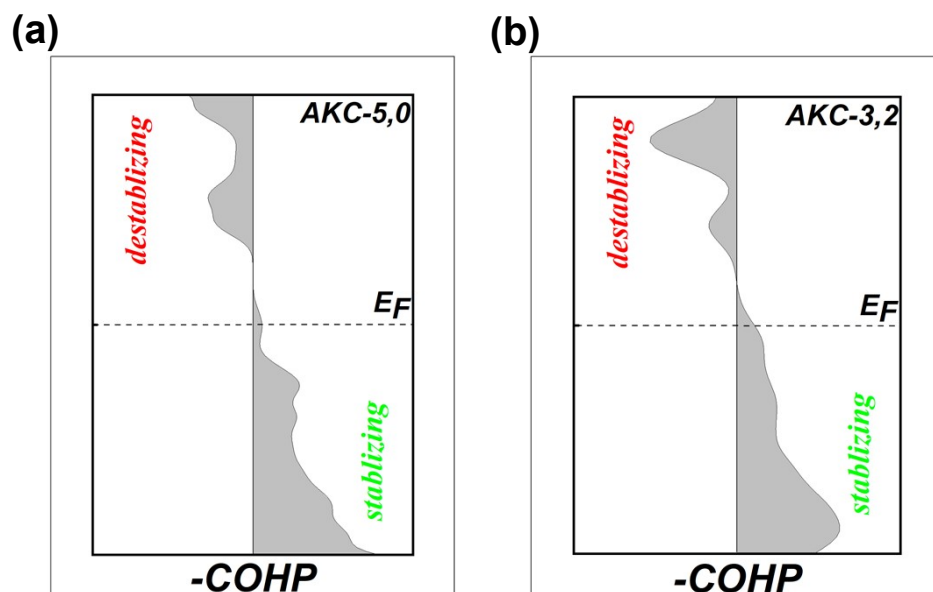
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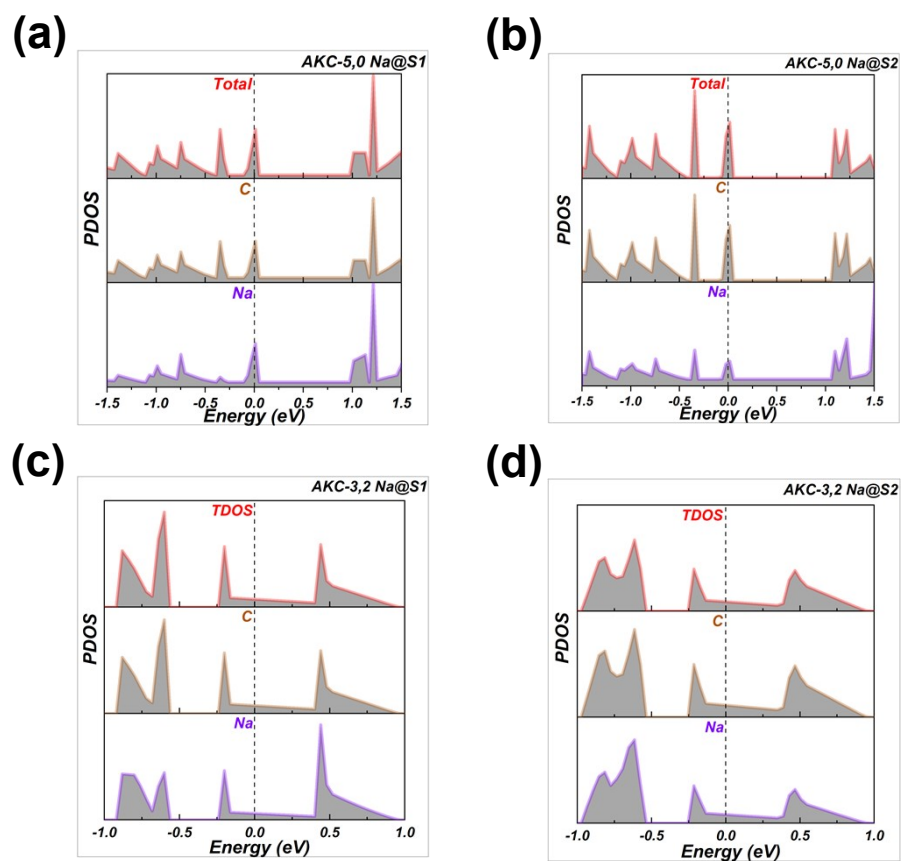
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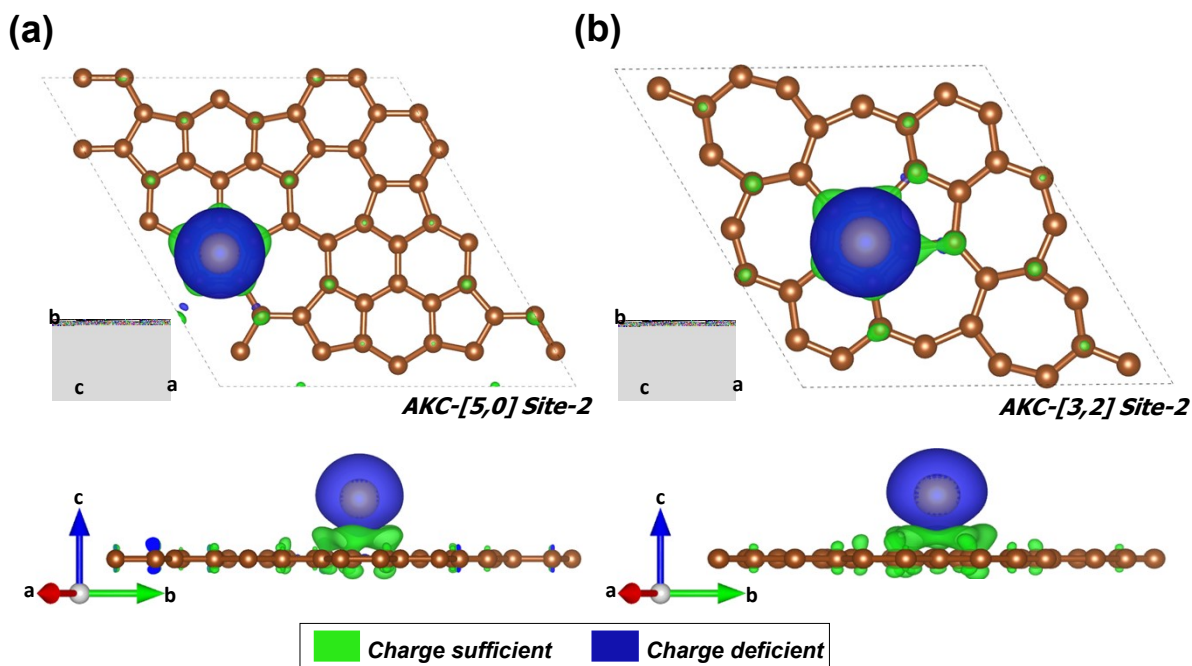
**Figure. S1** Top and side view of fully relaxed geometry of AA-stacking for metallic (a) AKC-5,0 and (b) AKC-3,2 carbon allotropes.



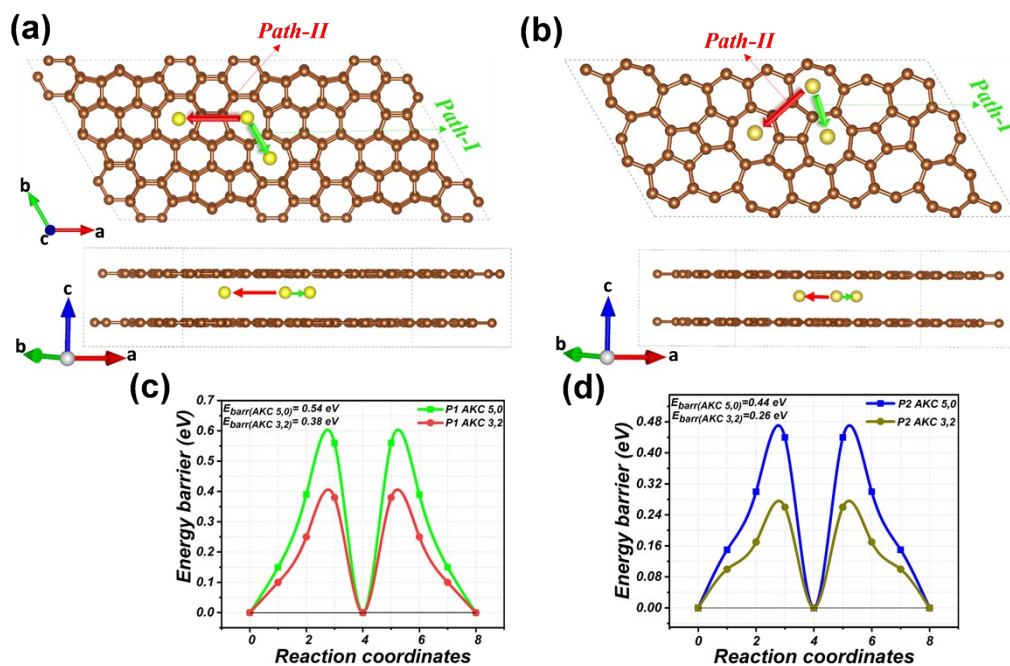
**Figure. S2** The crystal orbital Hamilton population (COHP) analysis for metallic (a) AKC-5,0 and (b) AKC-3,2 carbon allotropes.



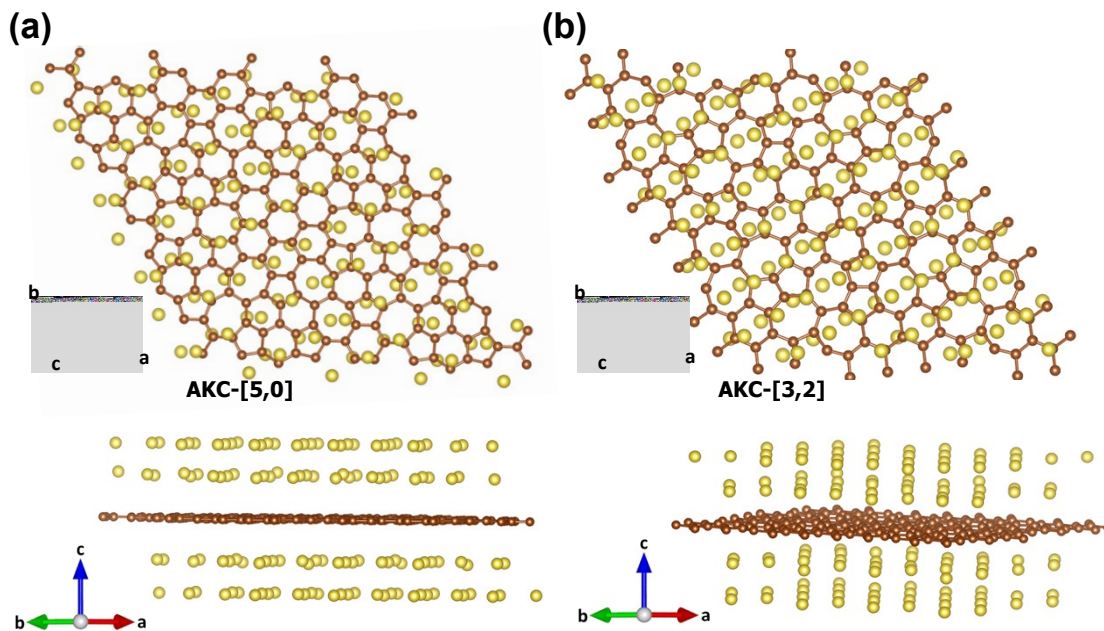
**Figure. S3** The partial density of states at the first two adsorption sites for metallic (a-b) AKC-5,0 and (c-d) AKC-3,2 carbon allotropes.



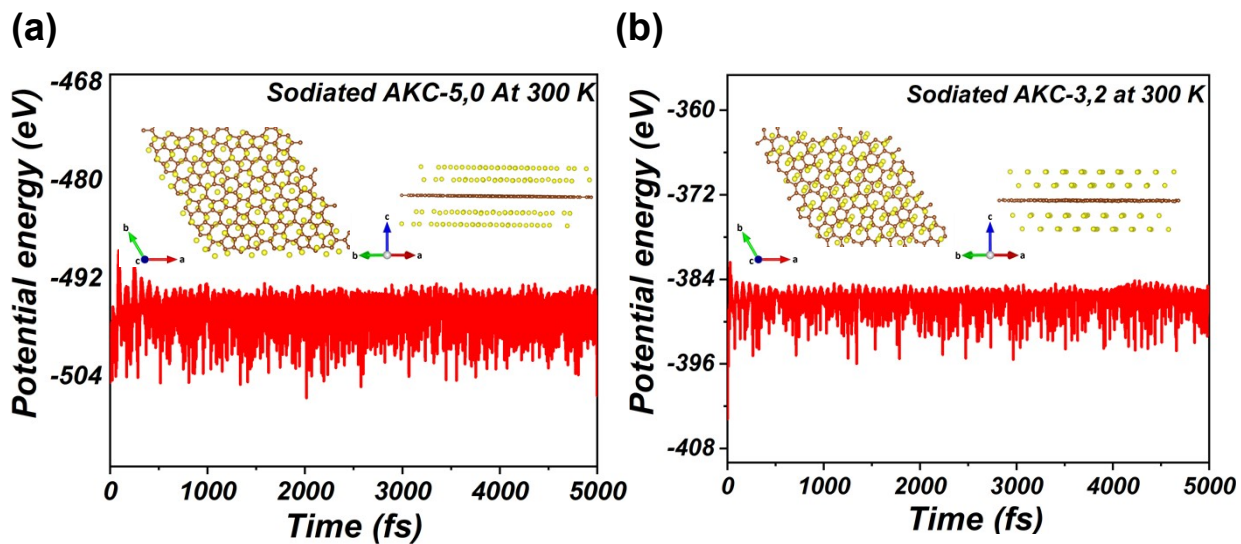
**Figure. S4** Results for charge density difference at the second most stable adsorption site of metallic (a) AKC-5,0 and (b) AKC-3,2 allotropes for sodium ion. The green and blue boxes represent the charge sufficient and charge deficient.



**Figure. S5** The two different diffusion pathways for sodium ions over (a-b) bilayer AKC-5,0 and bilayer AKC-3,2 allotropes and (c-d) their respective diffusion profiles.



**Figure. S6** Top and side view of fully sodiated metallic (a) AKC-5,0 and (b) AKC-3,2 carbon allotropes



**Figure. S7** The fluctuation in potential energy for the fully sodiated metallic (a) AKC-5,0 and (b) AKC-3,2 allotropes with structural distortion calculated at 300 K.

**Table. S1** The vibration frequency, zero point energy and energy contribution of Na-ion at T.S for monolayer AKC-5,0 and AKC-3,2 allotropes.

|                                   | <i>AKC-3,2</i>     |                   | <i>AKC-5,0</i>    |                   |
|-----------------------------------|--------------------|-------------------|-------------------|-------------------|
|                                   | <i>Path-1</i>      | <i>Path-2</i>     | <i>Path-1</i>     | <i>Path-2</i>     |
| <i>Frequency</i>                  | <i>117.34 cm-1</i> | <i>78.98 cm-1</i> | <i>40.86 cm-1</i> | <i>53.76 cm-1</i> |
| <i>Zero point energy</i>          | <i>0.0186 eV</i>   | <i>0.0140 eV</i>  | <i>0.0152 eV</i>  | <i>0.0161 eV</i>  |
| <i>Energy contribution at T.S</i> | <i>0.077 eV</i>    | <i>0.024 eV</i>   | <i>0.0896 eV</i>  | <i>0.0882 eV</i>  |