

Supporting Information

**Crystal Structure, Stability and Li Superionic Conductivity of Pyrochlore-Type Solid Electrolyte  $\text{Li}_{2-x}\text{La}_{(1+x)/3}\text{Nb}_2\text{O}_6\text{F}$ : A First-Principles Calculation Study**

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### *Material synthesis*

The  $\text{Li}_{1.25}\text{La}_{0.58}\text{Nb}_2\text{O}_6\text{F}$  (LLNOF) solid electrolyte was prepared using the following synthesis conditions.  $\text{Li}_2\text{CO}_3$ ,  $\text{La}_2\text{O}_3$  and  $\text{Nb}_2\text{O}_5$  reactant powders in stoichiometric ratio were calcined at 773 K and then heated at 1473 K for 6 hours to synthesize the precursor  $\text{Li}_{0.5}\text{La}_{0.5}\text{Nb}_2\text{O}_6$ . Next, the synthesized  $\text{Li}_{0.5}\text{La}_{0.5}\text{Nb}_2\text{O}_6$  was mixed with  $\text{LaF}_3$  and  $\text{LiF}$ . Here, 91%-excess  $\text{LiF}$  was added. The mixture was then heated at 1273 K for 6 hours to synthesize the target LLNOF powder.

### *Cyclic voltammetry measurement*

The LLNOF electrolyte, acetylene black (AB) (conductive additive), and polyvinylidene fluoride (PVDF) (binder) were weighed in a mass ratio of 70:10:20 and then mixed with N-methyl-2-pyrrolidone (NMP) to form a paste. The paste was applied onto a copper foil and dried to make an electrode. The cyclic voltammetry evaluation was conducted using a 2032-type coin cell assembled with a Li anode. The electrolyte used was a solution of 1M  $\text{LiPF}_6$  dissolved in a mixture of ethylene carbonate (EC) and dimethyl carbonate (DEC) in a volume ratio of 1:1. The coin cells were assembled in an Ar atmosphere inside a glove box. Cyclic voltammetry measurements were performed using a potentiostat/galvanostat device, with a scan voltage range of 0.02 V to 3V and a scan rate of 10 mV/s at 25°C.

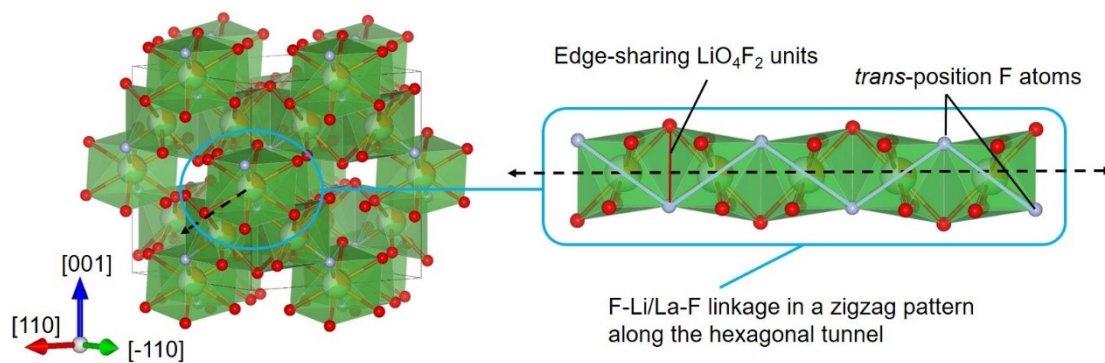


Figure S1. Visualization of the local structure of pyrochlore-type  $\text{Li}_{2-x}\text{La}_{(1+x)/3}\text{Nb}_2\text{O}_6\text{F}$  (LLNOF) showing the F-Li/La-F linkage in a zigzag pattern along the characteristic hexagonal tunnel. The octahedral  $\text{NbO}_6$  units are not displayed for clarity.

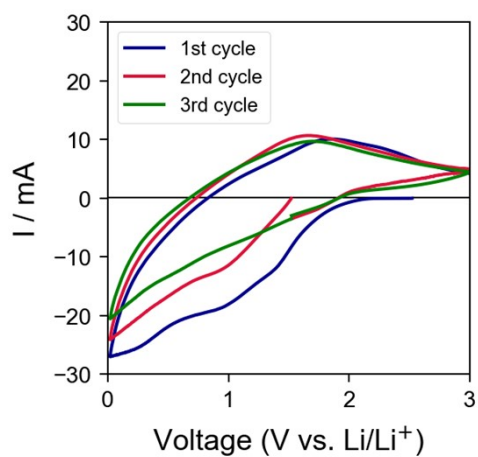


Figure S2. Cyclic voltammetry curves for the 1st, 2nd, and 3rd cycle of cell with LLNOF solid electrolyte.

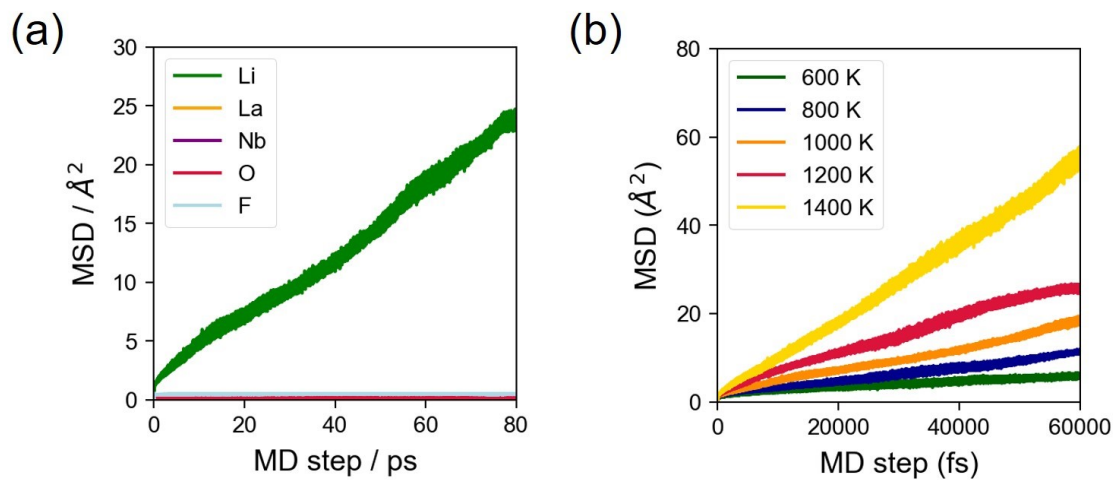


Figure S3. Mean squared displacement ( $MSD$ ) plots for (a) each atom types at 1000 K and (b) Li atoms in pyrochlore-type  $\text{Li}_{1.3125}\text{La}_{0.5625}\text{Nb}_2\text{O}_6\text{F}$  with the L1 structure (LLNOF-L1) from by NVT-AIMD calculations.

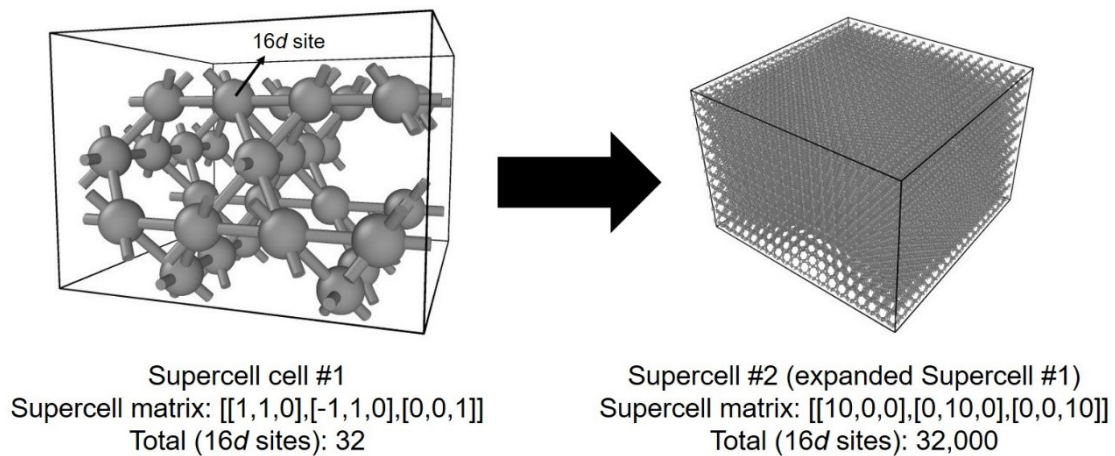


Figure S4. Supercell operation of the 16d-site cation sublattice in the  $\text{Li}_{2-x}\text{La}_{(1+x)/3}\text{Nb}_2\text{O}_6\text{F}$  crystal structure for use in the calculation of  $\text{Li}^+$  percolation threshold.

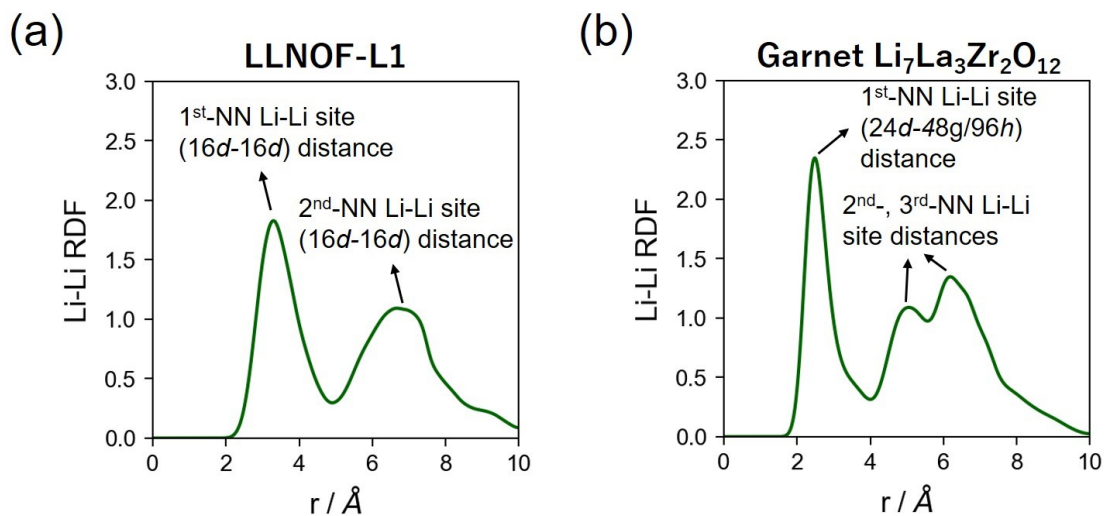


Figure S5. Li-Li radial distribution function (RDF) profiles derived from 1000-K NVT AIMD calculations for (a) pyrochlore-type  $\text{Li}_{1.3125}\text{La}_{0.5625}\text{Nb}_2\text{O}_6\text{F}$  with the L1 structure (LLNOF-L1) and (b) garnet-type cubic  $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ .

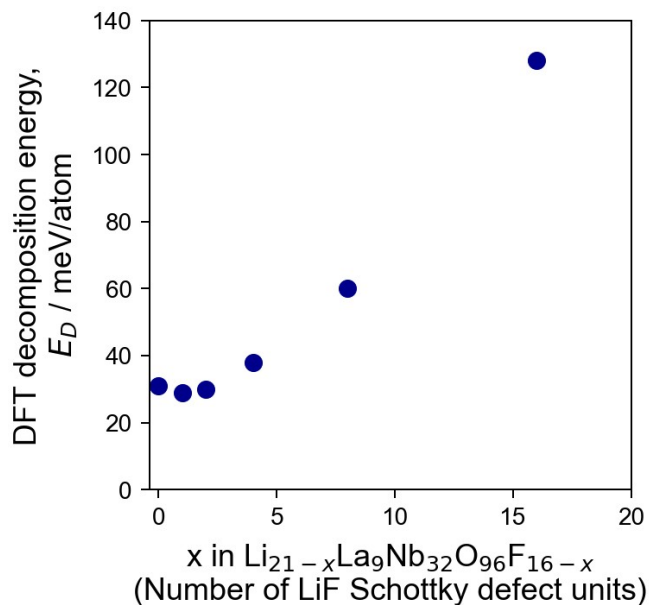


Figure S6. Plot for DFT decomposition energy as a function of the number of LiF Schottky defect units. The initial reference structure was based on  $\text{Li}_{1.3125}\text{La}_{0.5625}\text{Nb}_2\text{O}_6\text{F}$  composition (L1 structure, supercell formula is  $\text{Li}_{21}\text{La}_9\text{Nb}_{32}\text{O}_{96}\text{F}_{16}$  which is for  $x = 0$ ).

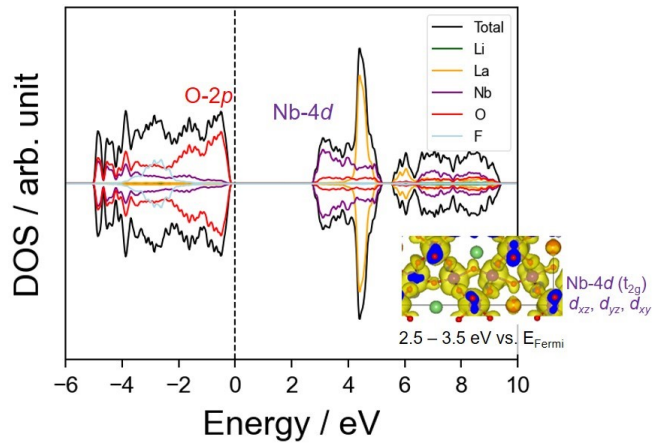


Figure S7. DFT-GGA electronic density of states (DOS) of pyrochlore-type  $\text{Li}_{1.3125}\text{La}_{0.5625}\text{Nb}_2\text{O}_6\text{F}$  (LLNOF-L1 structure). The Fermi energy is referenced as zero in the horizontal axis.

Table S1. Crystal structure coordinate data of LLNOF by XRD Rietveld analysis, as reported in Ref. 12. Space group:  $Fd\bar{3}m$  (cubic), lattice parameter  $a$ : 1.0445(1) nm, cell volume: 1.1396(1) nm<sup>3</sup>.

Atom	Site	Occupancy (g)	Coordinates		
			x	y	z
La	16d	0.2771(6)	1/2	1/2	1/2
Li	16d	0.365(15)	x(La)	y(La)	z(La)
Nb	16c	1.0	0	0	0
O	48f	1.0	0.3151(2)	1/8	1/8
F	8b	0.989(8)	3/8	3/8	3/8

Table S2. Summary of DFT-predicted decomposition reactions related to the voltage stability window of pyrochlore-type  $\text{Li}_{1.3125}\text{La}_{0.5625}\text{Nb}_2\text{O}_6\text{F}$  with the L1 structure (LLNOF-L1).

Voltage / V vs. Li/Li <sup>+</sup>	Decomposition reaction
0 – 0.54	$\text{Li}_{21}\text{La}_9\text{Nb}_{32}(\text{O}_6\text{F})_{16} + 160 \text{ Li} \rightarrow 4.5 \text{ La}_2\text{O}_3 + 16 \text{ LiF} + 82.5 \text{ Li}_2\text{O} + 32 \text{ Nb}$
0.54 – 0.62	$\text{Li}_{21}\text{La}_9\text{Nb}_{32}(\text{O}_6\text{F})_{16} + 64 \text{ Li} \rightarrow 4.5 \text{ La}_2\text{O}_3 + 32 \text{ LiNbO}_2 + 16 \text{ LiF} + 18.5 \text{ Li}_2\text{O}$
0.62 – 0.96	$\text{Li}_{21}\text{La}_9\text{Nb}_{32}(\text{O}_6\text{F})_{16} + 49.2 \text{ Li} \rightarrow 3.7 \text{ Li}_8\text{Nb}_2\text{O}_9 + 4.5 \text{ La}_2\text{O}_3 + 24.6 \text{ LiNbO}_2 + 16 \text{ LiF}$
0.96 – 0.99	$\text{Li}_{21}\text{La}_9\text{Nb}_{32}(\text{O}_6\text{F})_{16} + 45.5 \text{ Li} \rightarrow 4.5 \text{ La}_2\text{O}_3 + 22.75 \text{ LiNbO}_2 + 9.25 \text{ Li}_3\text{NbO}_4 + 16 \text{ LiF}$
0.99 – 1.33	$\text{Li}_{21}\text{La}_9\text{Nb}_{32}(\text{O}_6\text{F})_{16} + 41 \text{ Li} \rightarrow 20.5 \text{ LiNbO}_2 + 11.5 \text{ Li}_3\text{NbO}_4 + 7 \text{ LiF} + 9 \text{ LaOF}$
1.33 – 1.74	$\text{Li}_{21}\text{La}_9\text{Nb}_{32}(\text{O}_6\text{F})_{16} + 32 \text{ Li} \rightarrow 16 \text{ LiNbO}_2 + 9 \text{ LaNbO}_4 + 7 \text{ Li}_3\text{NbO}_4 + 16 \text{ LiF}$
1.74 – 1.92	$\text{Li}_{21}\text{La}_9\text{Nb}_{32}(\text{O}_6\text{F})_{16} + 18 \text{ Li} \rightarrow 14 \text{ LiNbO}_3 + 9 \text{ LiNbO}_2 + 9 \text{ LaNbO}_4 + 16 \text{ LiF}$
1.92 – 2.35	$\text{Li}_{21}\text{La}_9\text{Nb}_{32}(\text{O}_6\text{F})_{16} + 2.571 \text{ Li} \rightarrow 7.571 \text{ LiNbO}_3 + 1.286 \text{ Nb}_{12}\text{O}_{29} + 9 \text{ LaNbO}_4 + 16 \text{ LiF}$
2.35 – 2.49	$\text{Li}_{21}\text{La}_9\text{Nb}_{32}(\text{O}_6\text{F})_{16} + 0.8889 \text{ Li} \rightarrow 5.889 \text{ LiNb}_3\text{O}_8 + 0.4444 \text{ Nb}_{12}\text{O}_{29} + 9 \text{ LaNbO}_4 + 16 \text{ LiF}$
2.49 – 3.92	$\text{Li}_{21}\text{La}_9\text{Nb}_{32}(\text{O}_6\text{F})_{16} \rightarrow 5 \text{ LiNb}_3\text{O}_8 + 9 \text{ LaNbO}_4 + 4 \text{ Nb}_2\text{O}_5 + 16 \text{ LiF}$
3.92 – 3.93	$\text{Li}_{21}\text{La}_9\text{Nb}_{32}(\text{O}_6\text{F})_{16} \rightarrow 9 \text{ LaNbO}_4 + 11.5 \text{ Nb}_2\text{O}_5 + 16 \text{ LiF} + 1.25 \text{ O}_2 + 5 \text{ Li}$
3.93 –	$\text{Li}_{21}\text{La}_9\text{Nb}_{32}(\text{O}_6\text{F})_{16} \rightarrow 3.667 \text{ LaNbO}_4 + 14.17 \text{ Nb}_2\text{O}_5 + 5.333 \text{ LaF}_3 + 5.25 \text{ O}_2 + 21 \text{ Li}$

Table S3. Summary of DFT-predicted decomposition reactions related to the voltage stability window of  $\text{Li}_3\text{Nb}_3\text{O}_8$  which is one of the decomposition phases of pyrochlore-type  $\text{Li}_{1.3125}\text{La}_{0.5625}\text{Nb}_2\text{O}_6\text{F}$  with the L1 structure (LLNOF-L1).

Voltage / V vs. Li/Li <sup>+</sup>	Decomposition reaction
0 – 0.54	$4 \text{ LiNb}_3\text{O}_8 + 60 \text{ Li} \rightarrow 32 \text{ Li}_2\text{O} + 12 \text{ Nb}$
0.54 – 0.62	$4 \text{ LiNb}_3\text{O}_8 + 24 \text{ Li} \rightarrow 12 \text{ LiNbO}_2 + 8 \text{ Li}_2\text{O}$
0.62 – 0.96	$4 \text{ LiNb}_3\text{O}_8 + 17.6 \text{ Li} \rightarrow 1.6 \text{ Li}_8\text{Nb}_2\text{O}_9 + 8.8 \text{ LiNbO}_2$
0.96 – 1.74	$4 \text{ LiNb}_3\text{O}_8 + 16 \text{ Li} \rightarrow 4 \text{ Li}_3\text{NbO}_4 + 8 \text{ LiNbO}_2$
1.74 – 1.92	$4 \text{ LiNb}_3\text{O}_8 + 8 \text{ Li} \rightarrow 8 \text{ LiNbO}_3 + 4 \text{ LiNbO}_2$

1.92 – 2.35	$4 \text{LiNb}_3\text{O}_8 + 1.143 \text{Li} \rightarrow 5.143 \text{LiNbO}_3 + 0.5714 \text{Nb}_{12}\text{O}_{29}$
2.35 – 3.92	$4 \text{LiNb}_3\text{O}_8 \rightarrow 4 \text{LiNb}_3\text{O}_8$
3.92 –	$4 \text{LiNb}_3\text{O}_8 \rightarrow 6 \text{Nb}_2\text{O}_5 + \text{O}_2 + 4 \text{Li}$

Table S4. Summary of DFT-predicted decomposition reactions related to the voltage stability window of LiF which is one of the decomposition phases of pyrochlore-type  $\text{Li}_{1.3125}\text{La}_{0.5625}\text{Nb}_2\text{O}_6\text{F}$  with the L1 structure (LLNOF-L1).

Voltage / V vs. Li/Li <sup>+</sup>	Decomposition reaction
0 – 6.36	$\text{LiF} \rightarrow \text{LiF}$
6.36 –	$\text{LiF} \rightarrow 0.5 \text{F}_2 + \text{Li}$

Table S5. Summary of DFT-predicted decomposition reactions related to the voltage stability window of  $\text{LaNbO}_4$  which is one of the decomposition phases of pyrochlore-type  $\text{Li}_{1.3125}\text{La}_{0.5625}\text{Nb}_2\text{O}_6\text{F}$  with the L1 structure (LLNOF-L1).

Voltage / V vs. Li/Li <sup>+</sup>	Decomposition reaction
0 – 0.54	$2 \text{LaNbO}_4 + 10 \text{Li} \rightarrow 5 \text{Li}_2\text{O} + \text{La}_2\text{O}_3 + 2 \text{Nb}$
0.54 – 0.62	$2 \text{LaNbO}_4 + 4 \text{Li} \rightarrow 2 \text{LiNbO}_2 + \text{Li}_2\text{O} + \text{La}_2\text{O}_3$
0.62 – 0.96	$2 \text{LaNbO}_4 + 3.2 \text{Li} \rightarrow 1.6 \text{LiNbO}_2 + 0.2 \text{Li}_8\text{Nb}_2\text{O}_9 + \text{La}_2\text{O}_3$
0.96 – 1.06	$2 \text{LaNbO}_4 + 3 \text{Li} \rightarrow 0.5 \text{Li}_3\text{NbO}_4 + 1.5 \text{LiNbO}_2 + \text{La}_2\text{O}_3$
1.06 – 1.30	$2 \text{LaNbO}_4 + 2 \text{Li} \rightarrow 0.3333 \text{Li}_3\text{NbO}_4 + 0.6667 \text{La}_3\text{NbO}_7 + \text{LiNbO}_2$
1.30 –	$2 \text{LaNbO}_4 \rightarrow 2 \text{LaNbO}_4$

Table S6. Summary of DFT-predicted decomposition reactions related to the voltage stability window of  $\text{Nb}_2\text{O}_5$  which is one of the decomposition phases of pyrochlore-type  $\text{Li}_{1.3125}\text{La}_{0.5625}\text{Nb}_2\text{O}_6\text{F}$  with the L1 structure (LLNOF-L1).

Voltage / V vs. Li/Li <sup>+</sup>	Decomposition reaction
0 – 0.54	$14 \text{Nb}_2\text{O}_5 + 140 \text{Li} \rightarrow 70 \text{Li}_2\text{O} + 28 \text{Nb}$
0.54 – 0.62	$14 \text{Nb}_2\text{O}_5 + 56 \text{Li} \rightarrow 28 \text{LiNbO}_2 + 14 \text{Li}_2\text{O}$
0.62 – 0.96	$14 \text{Nb}_2\text{O}_5 + 44.8 \text{Li} \rightarrow 2.8 \text{Li}_8\text{Nb}_2\text{O}_9 + 22.4 \text{LiNbO}_2$
0.96 – 1.74	$14 \text{Nb}_2\text{O}_5 + 42 \text{Li} \rightarrow 7 \text{Li}_3\text{NbO}_4 + 21 \text{LiNbO}_2$
1.74 – 1.92	$14 \text{Nb}_2\text{O}_5 + 28 \text{Li} \rightarrow 14 \text{LiNbO}_3 + 14 \text{LiNbO}_2$
1.92 – 2.35	$14 \text{Nb}_2\text{O}_5 + 4 \text{Li} \rightarrow 4 \text{LiNbO}_3 + 2 \text{Nb}_{12}\text{O}_{29}$



2.35 – 2.49	$14 \text{ Nb}_2\text{O}_5 + 3.111 \text{ Li} \rightarrow 3.111 \text{ LiNb}_3\text{O}_8 + 1.556 \text{ Nb}_{12}\text{O}_{29}$
2.49 –	$14 \text{ Nb}_2\text{O}_5 \rightarrow 14 \text{ Nb}_2\text{O}_5$

Table S7. Summary of DFT-predicted decomposition reactions related to the voltage stability window of garnet-type cubic  $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$ .

Voltage / V vs. Li/Li <sup>+</sup>	Decomposition reaction
0 – 0.04	$4 \text{ Li}_7\text{La}_3\text{Zr}_2\text{O}_{12} + 28 \text{ Li} \rightarrow 2 \text{ Zr}_4\text{O} + 28 \text{ Li}_2\text{O} + 6 \text{ La}_2\text{O}_3$
0.04 – 0.05	$4 \text{ Li}_7\text{La}_3\text{Zr}_2\text{O}_{12} + 26.67 \text{ Li} \rightarrow 2.667 \text{ Zr}_3\text{O} + 27.33 \text{ Li}_2\text{O} + 6 \text{ La}_2\text{O}_3$
0.05 – 2.90	$4 \text{ Li}_7\text{La}_3\text{Zr}_2\text{O}_{12} \rightarrow 4 \text{ Li}_6\text{Zr}_2\text{O}_7 + 2 \text{ Li}_2\text{O} + 6 \text{ La}_2\text{O}_3$
2.90 – 3.16	$4 \text{ Li}_7\text{La}_3\text{Zr}_2\text{O}_{12} \rightarrow 4 \text{ Li}_6\text{Zr}_2\text{O}_7 + \text{Li}_2\text{O}_2 + 6 \text{ La}_2\text{O}_3 + 2 \text{ Li}$
3.16 – 3.24	$4 \text{ Li}_7\text{La}_3\text{Zr}_2\text{O}_{12} \rightarrow 7 \text{ Li}_2\text{O}_2 + 4 \text{ La}_2\text{Zr}_2\text{O}_7 + 2 \text{ La}_2\text{O}_3 + 14 \text{ Li}$
3.24 – 3.72	$4 \text{ Li}_7\text{La}_3\text{Zr}_2\text{O}_{12} \rightarrow 1.75 \text{ LiO}_8 + 4 \text{ La}_2\text{Zr}_2\text{O}_7 + 2 \text{ La}_2\text{O}_3 + 26.25 \text{ Li}$
3.72 –	$4 \text{ Li}_7\text{La}_3\text{Zr}_2\text{O}_{12} \rightarrow 4 \text{ La}_2\text{Zr}_2\text{O}_7 + 2 \text{ La}_2\text{O}_3 + 7 \text{ O}_2 + 28 \text{ Li}$

Table S8. Summary of DFT-predicted decomposition reactions related to the voltage stability window of  $\text{Li}_6\text{Zr}_2\text{O}_7$  which is one of the decomposition phases of garnet-type  $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$  (LLZO).

Voltage / V vs. Li/Li <sup>+</sup>	Decomposition reaction
0 – 0.04	$2 \text{ Li}_6\text{Zr}_2\text{O}_7 + 14 \text{ Li} \rightarrow \text{Zr}_4\text{O} + 13 \text{ Li}_2\text{O}$
0.04 – 0.05	$2 \text{ Li}_6\text{Zr}_2\text{O}_7 + 13.33 \text{ Li} \rightarrow 1.333 \text{ Zr}_3\text{O} + 12.67 \text{ Li}_2\text{O}$
0.05 – 3.21	$2 \text{ Li}_6\text{Zr}_2\text{O}_7 \rightarrow 2 \text{ Li}_6\text{Zr}_2\text{O}_7$
3.21 – 3.24	$2 \text{ Li}_6\text{Zr}_2\text{O}_7 \rightarrow 4 \text{ Li}_2\text{ZrO}_3 + \text{Li}_2\text{O}_2 + 2 \text{ Li}$
3.24 – 3.39	$2 \text{ Li}_6\text{Zr}_2\text{O}_7 \rightarrow 4 \text{ Li}_2\text{ZrO}_3 + 0.25 \text{ LiO}_8 + 3.75 \text{ Li}$
3.39 – 3.72	$2 \text{ Li}_6\text{Zr}_2\text{O}_7 \rightarrow 0.75 \text{ LiO}_8 + 4 \text{ ZrO}_2 + 11.25 \text{ Li}$
3.72 –	$2 \text{ Li}_6\text{Zr}_2\text{O}_7 \rightarrow 4 \text{ ZrO}_2 + 3 \text{ O}_2 + 12 \text{ Li}$

Table S9. Summary of DFT-predicted decomposition reactions related to the voltage stability window of  $\text{Li}_2\text{O}$  which is one of the reductive decomposition phases of garnet-type  $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$  (LLZO).

Voltage / V vs. Li/Li <sup>+</sup>	Decomposition reaction
0 – 2.90	$\text{Li}_2\text{O} \rightarrow \text{Li}_2\text{O}$
2.90 – 3.24	$\text{Li}_2\text{O} \rightarrow 0.5 \text{ Li}_2\text{O}_2 + \text{Li}$

3.24 – 3.72	$\text{Li}_2\text{O} \rightarrow 0.125 \text{LiO}_8 + 1.875 \text{Li}$
3.72 –	$\text{Li}_2\text{O} \rightarrow 0.5 \text{O}_2 + 2 \text{Li}$

Table S10. Summary of DFT-predicted decomposition reactions related to the voltage stability window of  $\text{La}_2\text{O}_3$  which is one of the reductive decomposition phases of garnet-type  $\text{Li}_7\text{La}_3\text{Zr}_2\text{O}_{12}$  (LLZO).

Voltage / V vs. $\text{Li}/\text{Li}^+$	Decomposition reaction
0 –	$\text{La}_2\text{O}_3 \rightarrow \text{La}_2\text{O}_3$

Table S11. Summary of DFT-predicted decomposition reactions related to the voltage stability window of garnet-type  $\text{Li}_5\text{La}_3\text{Ta}_2\text{O}_{12}$  (LLTO).

Voltage / V vs. $\text{Li}/\text{Li}^+$	Decomposition reaction
0 – 0.35	$4 \text{Li}_5\text{La}_3\text{Ta}_2\text{O}_{12} + 40 \text{Li} \rightarrow 30 \text{Li}_2\text{O} + 6 \text{La}_2\text{O}_3 + 8 \text{Ta}$
0.35 – 0.55	$4 \text{Li}_5\text{La}_3\text{Ta}_2\text{O}_{12} + 10 \text{Li} \rightarrow 6 \text{Li}_5\text{TaO}_5 + 6 \text{La}_2\text{O}_3 + 2 \text{Ta}$
0.55 – 0.65	$4 \text{Li}_5\text{La}_3\text{Ta}_2\text{O}_{12} + 2.5 \text{Li} \rightarrow 7.5 \text{Li}_3\text{TaO}_4 + 6 \text{La}_2\text{O}_3 + 0.5 \text{Ta}$
0.65 – 3.23	$4 \text{Li}_5\text{La}_3\text{Ta}_2\text{O}_{12} \rightarrow 6.667 \text{Li}_3\text{TaO}_4 + 1.333 \text{La}_3\text{TaO}_7 + 4 \text{La}_2\text{O}_3$
3.23 – 3.24	$4 \text{Li}_5\text{La}_3\text{Ta}_2\text{O}_{12} \rightarrow 4 \text{La}_3\text{TaO}_7 + 2 \text{Li}_2\text{O}_2 + 4 \text{Li}_3\text{TaO}_4 + 4 \text{Li}$
3.24 – 3.47	$4 \text{Li}_5\text{La}_3\text{Ta}_2\text{O}_{12} \rightarrow 0.5 \text{LiO}_8 + 4 \text{La}_3\text{TaO}_7 + 4 \text{Li}_3\text{TaO}_4 + 7.5 \text{Li}$
3.47 – 3.72	$4 \text{Li}_5\text{La}_3\text{Ta}_2\text{O}_{12} \rightarrow 1.25 \text{LiO}_8 + 2 \text{La}_3\text{TaO}_7 + 6 \text{LaTaO}_4 + 18.75 \text{Li}$
3.72 –	$4 \text{Li}_5\text{La}_3\text{Ta}_2\text{O}_{12} \rightarrow 2 \text{La}_3\text{TaO}_7 + 6 \text{LaTaO}_4 + 5 \text{O}_2 + 20 \text{Li}$

Table S12. Summary of DFT-predicted decomposition reactions related to the voltage stability window of  $\text{Li}_3\text{TaO}_4$  which is one of the reductive decomposition phases of garnet-type  $\text{Li}_5\text{La}_3\text{Ta}_2\text{O}_{12}$  (LLTO).

Voltage / V vs. $\text{Li}/\text{Li}^+$	Decomposition reaction
0 – 0.35	$\text{Li}_3\text{TaO}_4 + 5 \text{Li} \rightarrow 4 \text{Li}_2\text{O} + \text{Ta}$
0.35 – 0.55	$\text{Li}_3\text{TaO}_4 + \text{Li} \rightarrow 0.8 \text{Li}_5\text{TaO}_5 + 0.2 \text{Ta}$
0.55 – 3.59	$\text{Li}_3\text{TaO}_4 \rightarrow \text{Li}_3\text{TaO}_4$
3.59 – 3.72	$\text{Li}_3\text{TaO}_4 \rightarrow \text{LiTaO}_3 + 0.125 \text{LiO}_8 + 1.875 \text{Li}$

3.72 – 3.94	$\text{Li}_3\text{TaO}_4 \rightarrow \text{LiTaO}_3 + 0.5 \text{O}_2 + 2 \text{Li}$
3.94 – 4.03	$\text{Li}_3\text{TaO}_4 \rightarrow 0.3333 \text{LiTa}_3\text{O}_8 + 0.6667 \text{O}_2 + 2.667 \text{Li}$
4.03 –	$\text{Li}_3\text{TaO}_4 \rightarrow 0.5 \text{Ta}_2\text{O}_5 + 0.75 \text{O}_2 + 3 \text{Li}$

Table S13. Summary of DFT-predicted decomposition reactions related to the voltage stability window of  $\text{Li}_5\text{TaO}_5$  which is one of the reductive decomposition phases of  $\text{Li}_3\text{TaO}_4$ .

Voltage / V vs. Li/Li <sup>+</sup>	Decomposition reaction
0 – 0.35	$\text{Li}_5\text{TaO}_5 + 5 \text{Li} \rightarrow 5 \text{Li}_2\text{O} + \text{Ta}$
0.35 – 3.10	$\text{Li}_5\text{TaO}_5 \rightarrow \text{Li}_5\text{TaO}_5$
3.10 – 3.24	$\text{Li}_5\text{TaO}_5 \rightarrow 0.5 \text{Li}_2\text{O}_2 + \text{Li}_3\text{TaO}_4 + \text{Li}$
3.24 – 3.59	$\text{Li}_5\text{TaO}_5 \rightarrow \text{Li}_3\text{TaO}_4 + 0.125 \text{LiO}_8 + 1.875 \text{Li}$
3.59 – 3.72	$\text{Li}_5\text{TaO}_5 \rightarrow \text{LiTaO}_3 + 0.25 \text{LiO}_8 + 3.75 \text{Li}$
3.72 – 3.94	$\text{Li}_5\text{TaO}_5 \rightarrow \text{LiTaO}_3 + \text{O}_2 + 4 \text{Li}$
3.94 – 4.03	$\text{Li}_5\text{TaO}_5 \rightarrow 0.3333 \text{LiTa}_3\text{O}_8 + 1.167 \text{O}_2 + 4.667 \text{Li}$
4.03 –	$\text{Li}_5\text{TaO}_5 \rightarrow 0.5 \text{Ta}_2\text{O}_5 + 1.25 \text{O}_2 + 5 \text{Li}$

Table S14. Summary of DFT-predicted decomposition reactions related to the voltage stability window of  $\text{La}_3\text{TaO}_7$  which is one of the reductive decomposition phases of  $\text{Li}_3\text{TaO}_4$ .

Voltage / V vs. Li/Li <sup>+</sup>	Decomposition reaction
0 – 0.35	$\text{La}_3\text{TaO}_7 + 5 \text{Li} \rightarrow 2.5 \text{Li}_2\text{O} + 1.5 \text{La}_2\text{O}_3 + \text{Ta}$
0.35 – 0.55	$\text{La}_3\text{TaO}_7 + 2.5 \text{Li} \rightarrow 0.5 \text{Li}_5\text{TaO}_5 + 1.5 \text{La}_2\text{O}_3 + 0.5 \text{Ta}$
0.55 – 0.65	$\text{La}_3\text{TaO}_7 + 1.875 \text{Li} \rightarrow 0.625 \text{Li}_3\text{TaO}_4 + 1.5 \text{La}_2\text{O}_3 + 0.375 \text{Ta}$
0.65 –	$\text{La}_3\text{TaO}_7 \rightarrow \text{La}_3\text{TaO}_7$