

Supplementary Information

High-throughput computational screening of novel MA₂Z₄-type Janus structures with excellent photovoltaic and photocatalytic properties

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Calculation details

The formation energy is calculated as follows

$$E_f = \frac{E_{total} - \sum_i n_i \mu_i}{\sum_i n_i} \quad S(1)$$

where E_{total} represents the total energy of the structure in a unit cell, n_i represents the number of the i th atom, and μ_i is the cohesion energy contained in the i th atom. The formation energies obtained are shown in the following table S1.

Phonon dispersion calculations based on VASP-DFPT (Density Functional Perturbation Theory)^{1, 2} are used to investigate their dynamic stability (both MA₂Z₄ are 4 × 4 × 1 supercells). The phonon dispersion curve is shown in Figure S1S2.

The thermal stability of the MA₂Z₄ structure was evaluated by performing ab initio arithmetic molecular dynamics (AIMD)¹ simulations at 300 K, where sufficiently large supercells containing more than 100 atoms were used to reduce lattice translation constraints. The system was stabilized at 300 K for 5 ps with a time step of 2 fs and the Nosè algorithm was used to control the temperature.

Carrier mobility is estimated by means of the deformation potential (DP) theory defined below:

$$\mu_{2D} = \frac{2e\hbar^3 C_{2D}}{3k_B T |m^*|^2 E_i^2} \quad S(2)$$

where e , \hbar , k_B and T are the electron charge, the approximate Planck constant, the Boltzmann constant and the temperature (300 K), respectively. C_{2D} is the modulus of elasticity under uniaxial strain along the strain direction, calculated as follows:

$$C_{2D} = [\partial^2 E / \partial (\Delta a / a_0)^2] / S_0 \quad S(3)$$

where S_0 is the equilibrium area. E_i is the strain-induced band-edge energy of the CBM of the electron and the VBM of the hole, calculated as follows:

$$E_i = \partial E_{edge} / \partial (\Delta a / a_0) \quad S(4)$$

where E_{edge} is the band edge energy of CBM for electrons and VBM for holes induced by uniaxial strain. m^* is the effective mass of the carrier, calculated as follows:

$$m^* = \hbar^2 / (\partial^2 E / \partial k^2) \quad S(5)$$

The work function is the minimum amount of energy that must be supplied to cause an electron to immediately escape from a solid surface. The defining formula for the work function is:

$$W = -e\Phi - E_F \quad S(6)$$

where $-e$ is the charge of an electron, Φ is the electrostatic potential in the vacuum nearby the surface, and E_F is the Fermi level (electrochemical potential of electrons) inside the material.

The investigation of optical properties begins with the calculation of the material's dielectric function $\varepsilon(\omega)$ as follows³:

$$\varepsilon(\omega) = \varepsilon_1(\omega) + i\varepsilon_2(\omega) \quad S(7)$$

where $\varepsilon_1(\omega)$ and $\varepsilon_2(\omega)$ are the real and imaginary parts of the dielectric function, and ω is the photon frequency. The imaginary part of the dielectric function $\varepsilon_2(\omega)$ was obtained from the following equation:

$$\varepsilon_2(\omega) = \frac{4\pi^2 e^2}{\Omega} \lim_{q \rightarrow 0} \frac{1}{q^2} \times \sum_{c,v,k} 2w_k \delta(E_c - E_v - \omega) |\langle c | \mathbf{e} \cdot \mathbf{q} | v \rangle|^2 \quad S(8)$$

where $\langle c | \mathbf{e} \cdot \mathbf{q} | v \rangle$ is the integrated optical transitions from the valence states (v) to the conduction states (c), \mathbf{e} is the polarization direction of the photon and \mathbf{q} is the electron momentum operator. The integration over \mathbf{k} is performed by summation over special kpoints with a corresponding weighting factor w_k . The real part of the dielectric function $\varepsilon_1(\omega)$ can be determined from the Kramers-Kronig relation given by:

$$\varepsilon_1(\omega) = 1 + \frac{2}{\pi} P \int_0^\infty \frac{\varepsilon_2(\omega') \omega'}{\omega^2 - \omega'^2 + i\eta} d\omega' \quad S(9)$$

where P denotes the principle value and η is the complex shift parameter.

Absorption coefficient $\alpha(\omega)$ can be calculated from the real $\varepsilon_1(\omega)$ and the imaginary $\varepsilon_2(\omega)$ parts:

$$\alpha(\omega) = \sqrt{2} \omega \left(\sqrt{\varepsilon_1^2(\omega) + \varepsilon_2^2(\omega)} - \varepsilon_1(\omega) \right)^{\frac{1}{2}} \quad S(10)$$

Additionally, in order to obtain the more accurate optical absorption of 2D materials, the optical absorption rate was calculated as follows:

$$A = \frac{\text{Re } \tilde{\sigma}}{|1 + \tilde{\sigma}/2|^2} \quad S(11)$$

Where $R = \left| \frac{\tilde{\sigma}/2}{1 + \tilde{\sigma}/2} \right|^2$ is the normalized reflectance, $\tilde{\sigma}(\omega) = \sigma_{2D}(\omega)/\varepsilon_0 c$ is the normalized conductivity. $\sigma_{2D}(\omega)$ denotes the in-plane 2D optical conductivity, which directly related to the corresponding $\sigma_{3D}(\omega)$ component through the equation of $\sigma_{2D}(\omega) = L\sigma_{3D}(\omega)$, where L is the slab thickness in the simulation cell, and 3D optical conductivity was obtained from $\sigma_{3D}(\omega) = i[1 - \varepsilon(\omega)]\varepsilon_0 \omega$ base on the Maxwell equation. For $\varepsilon(\omega)$, ε_0 , and ω , they are the frequency-dependent complex dielectric function, permittivity of vacuum, and frequency of the incident wave, respectively.

For hydrogen evolution reaction (HER), the reaction equation at PH=0 is as follows:



where * denotes the active site on the surface of the structure, H* denotes the hydrogen atoms on the surface of the adsorbed structure. The calculation of Gibbs free energy (ΔG_{H^*}) under acidic conditions is as follows⁴:

$$\Delta G_{H^*} = \Delta E + \Delta E_{ZPE} - T\Delta S \quad S(14)$$

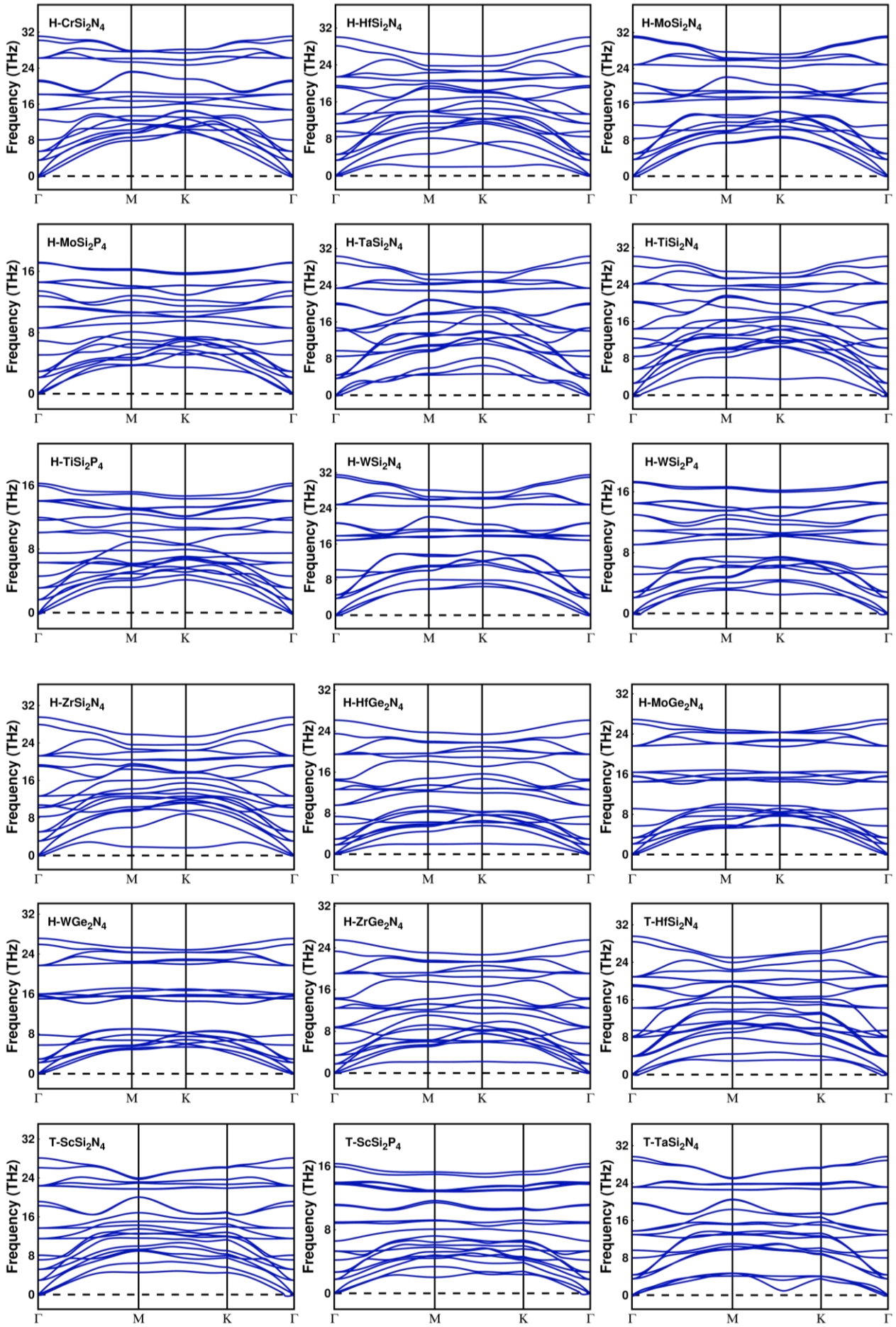
Therein ΔE denotes the energy difference between the hydrogen adsorption state and the independent state, ΔE_{ZPE} denotes the zero-point energy difference, ΔS denotes the entropy value difference, and T denotes the temperature (298.15 K).

The ΔG_{H^*} under the influence of different PH were calculated separately with the following equations:

$$\Delta G_{H^*} = G_{H^*} - 1/2G_{H_2} - G^* + 0.059 \times pH - eU \quad S(15)$$

where $0.059 \times pH$ is the free energy contribution under the effect of pH, eU denotes the influence of extra potential bias provided by the electrons or holes, and U is the electrode potential relative to the standard hydrogen electrode (SHE).

Supporting Figures



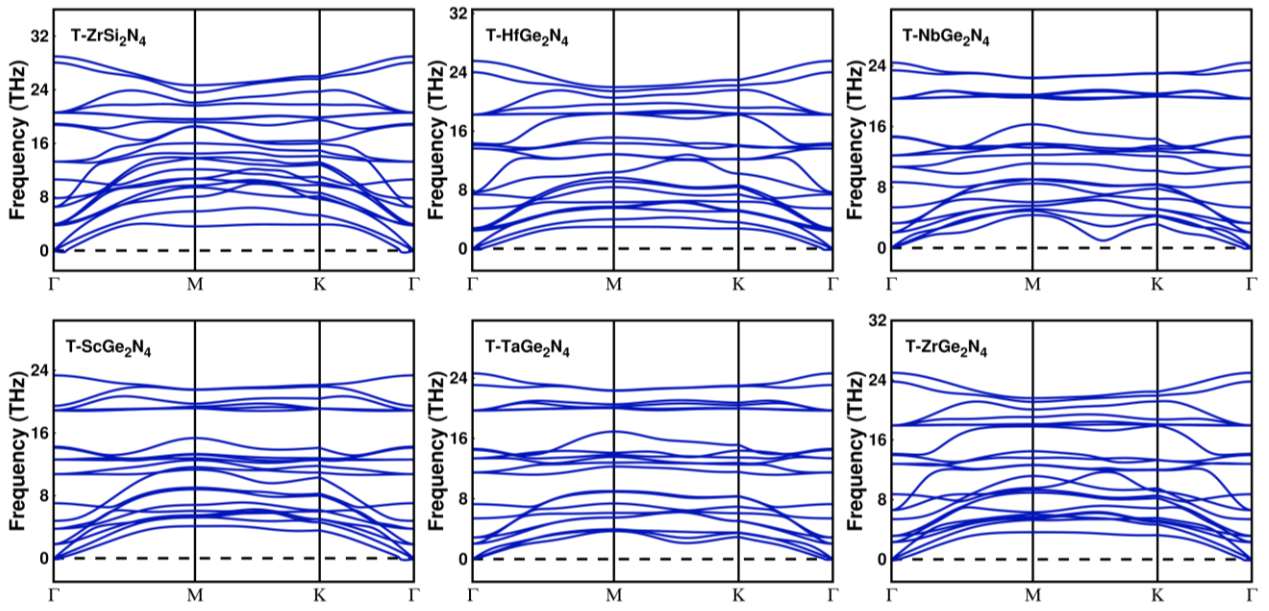
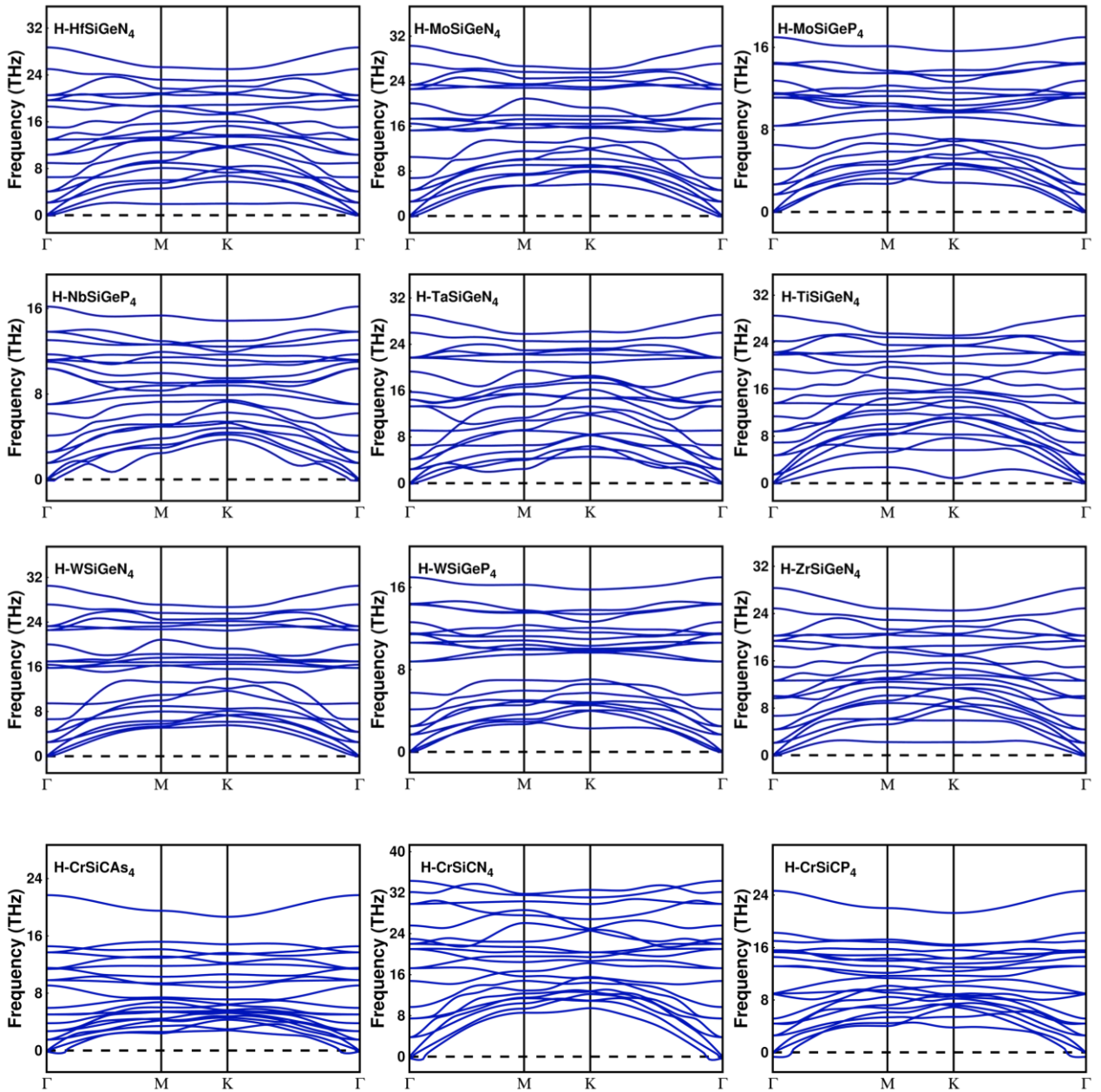
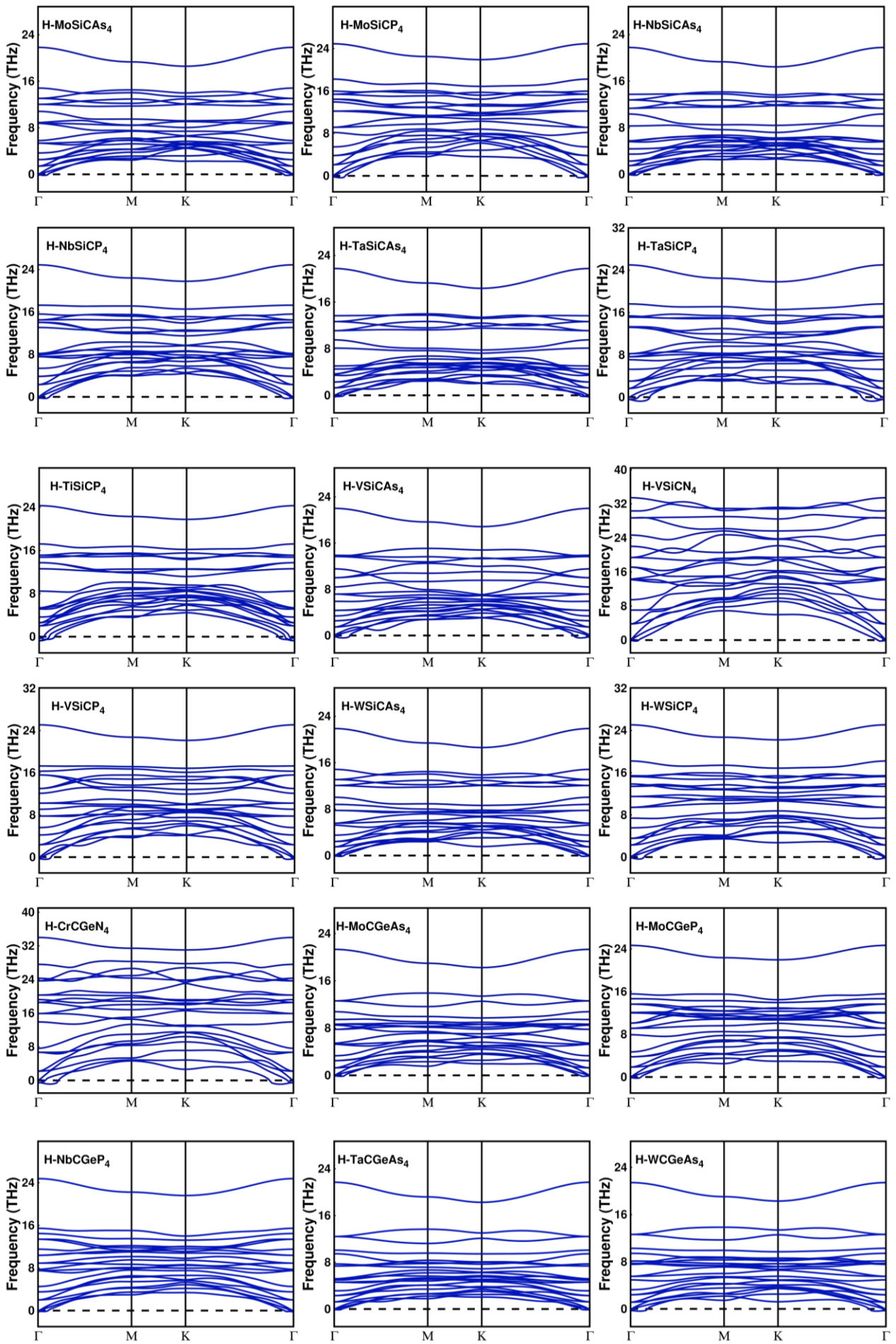


Fig. S1 Phonon dispersion curves for the symmetric structure of MA_2Z_4 .





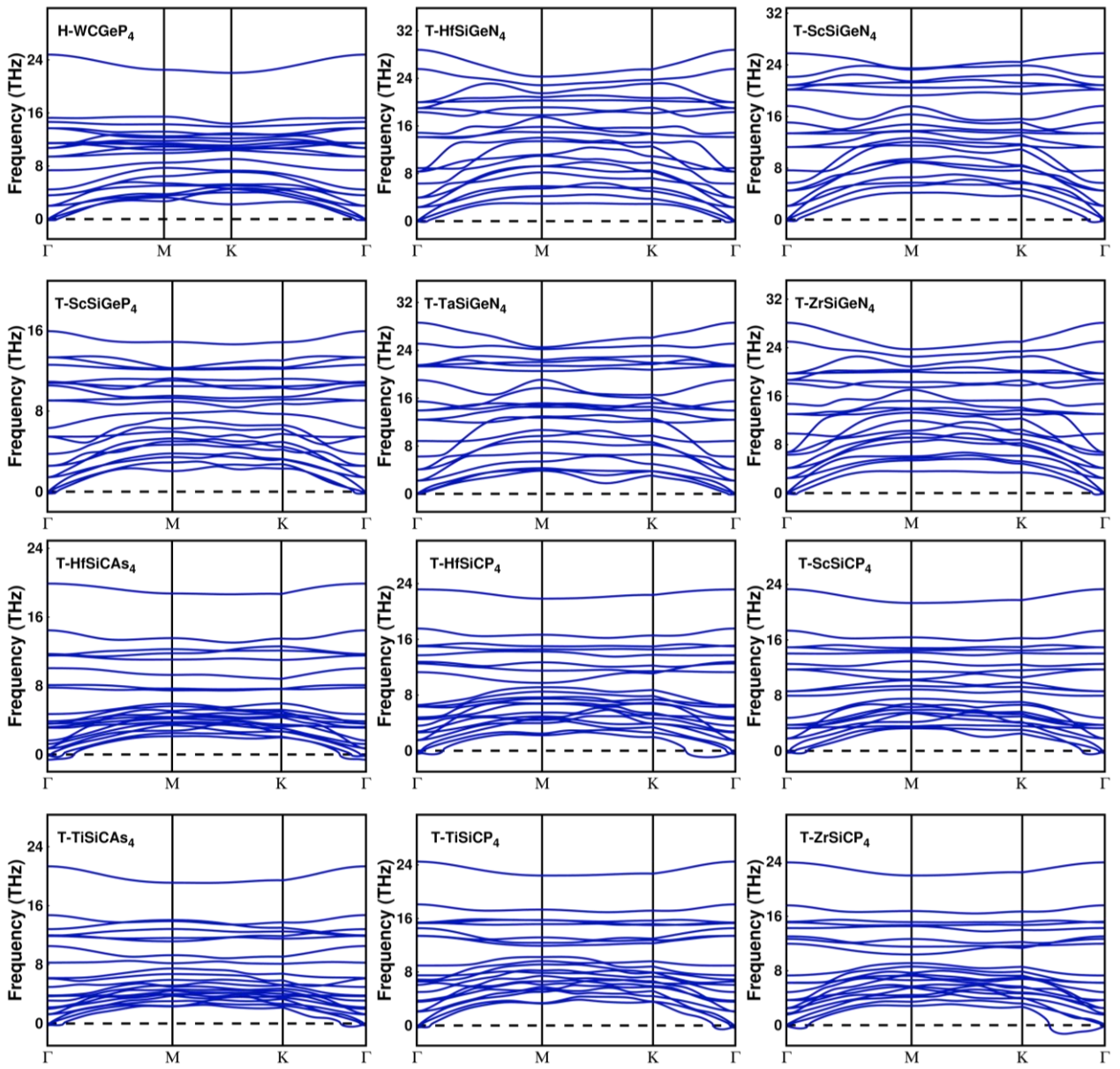
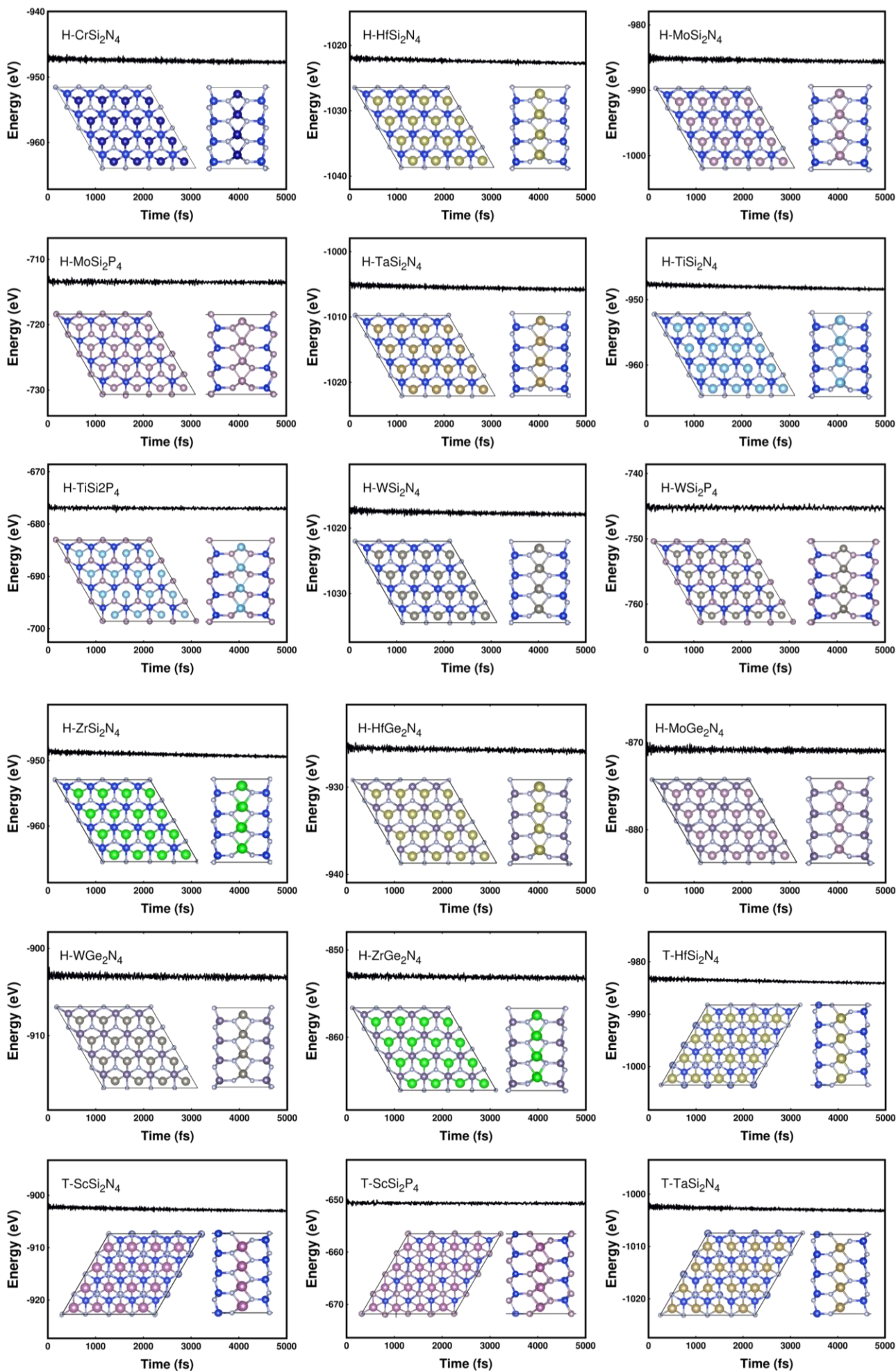


Fig. S2 Phonon dispersion curves for the asymmetric Janus structure of MA_2Z_4 .



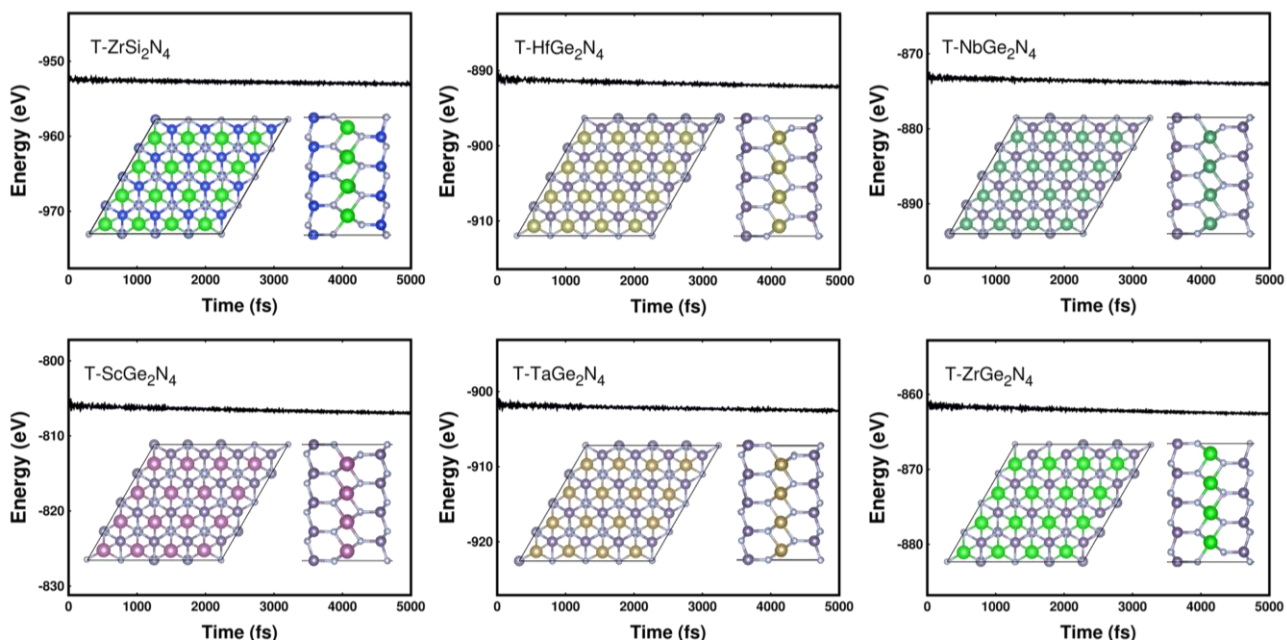
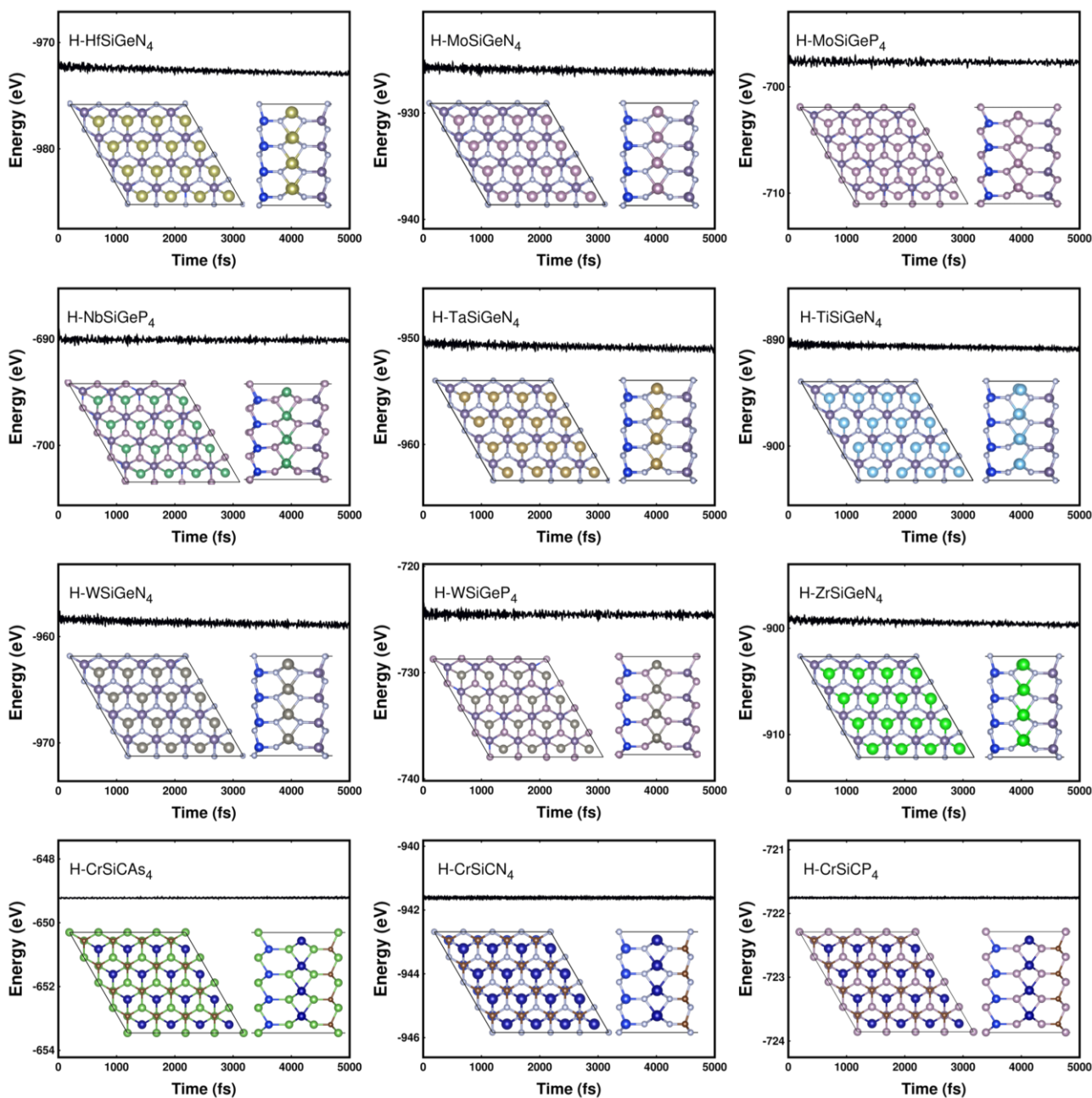
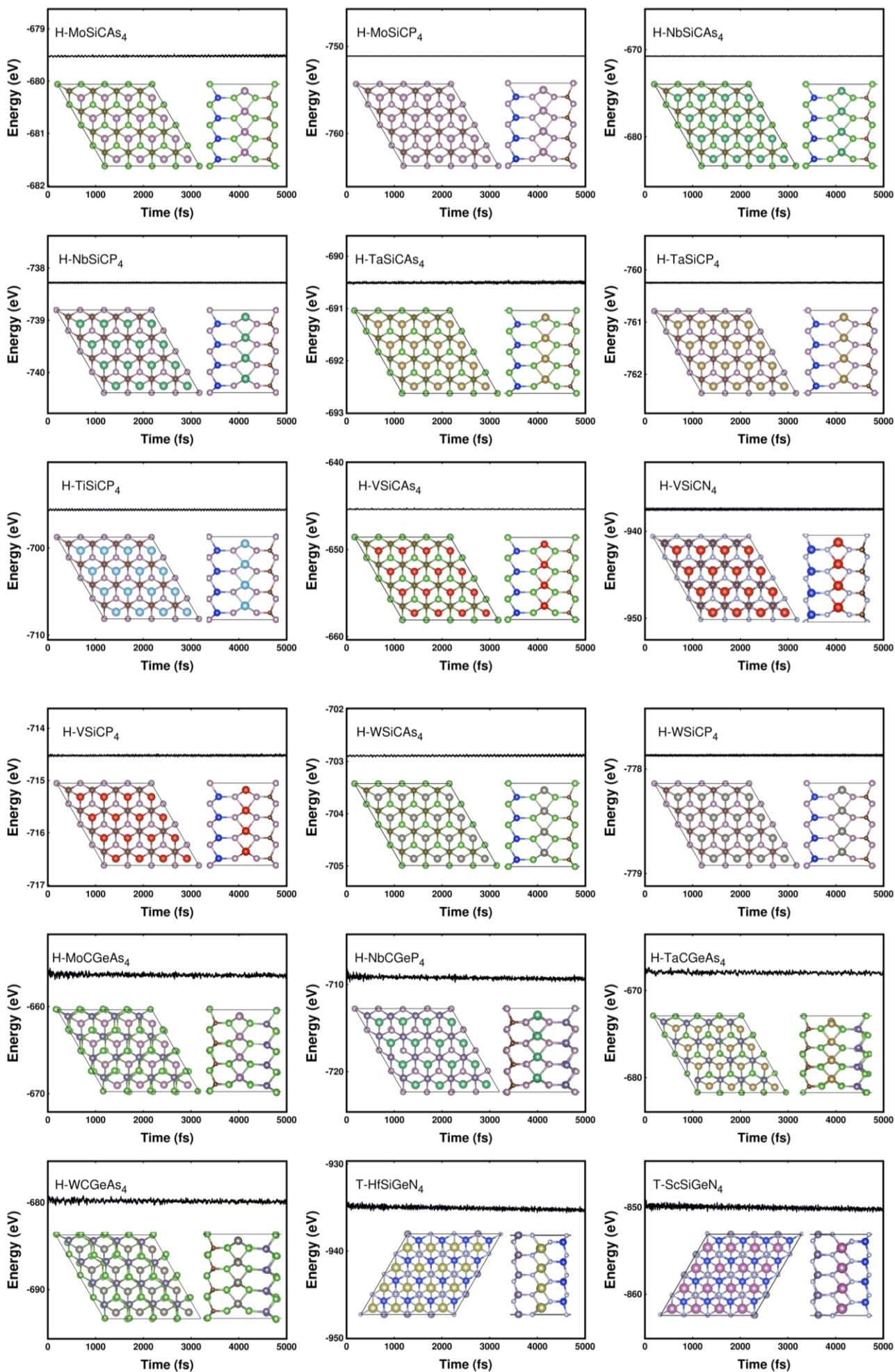


Fig. S3 Total potential energy and corresponding snapshots of symmetric MA_2Z_4 after 5 ps stabilization at 300 K obtained in AIMD simulations.





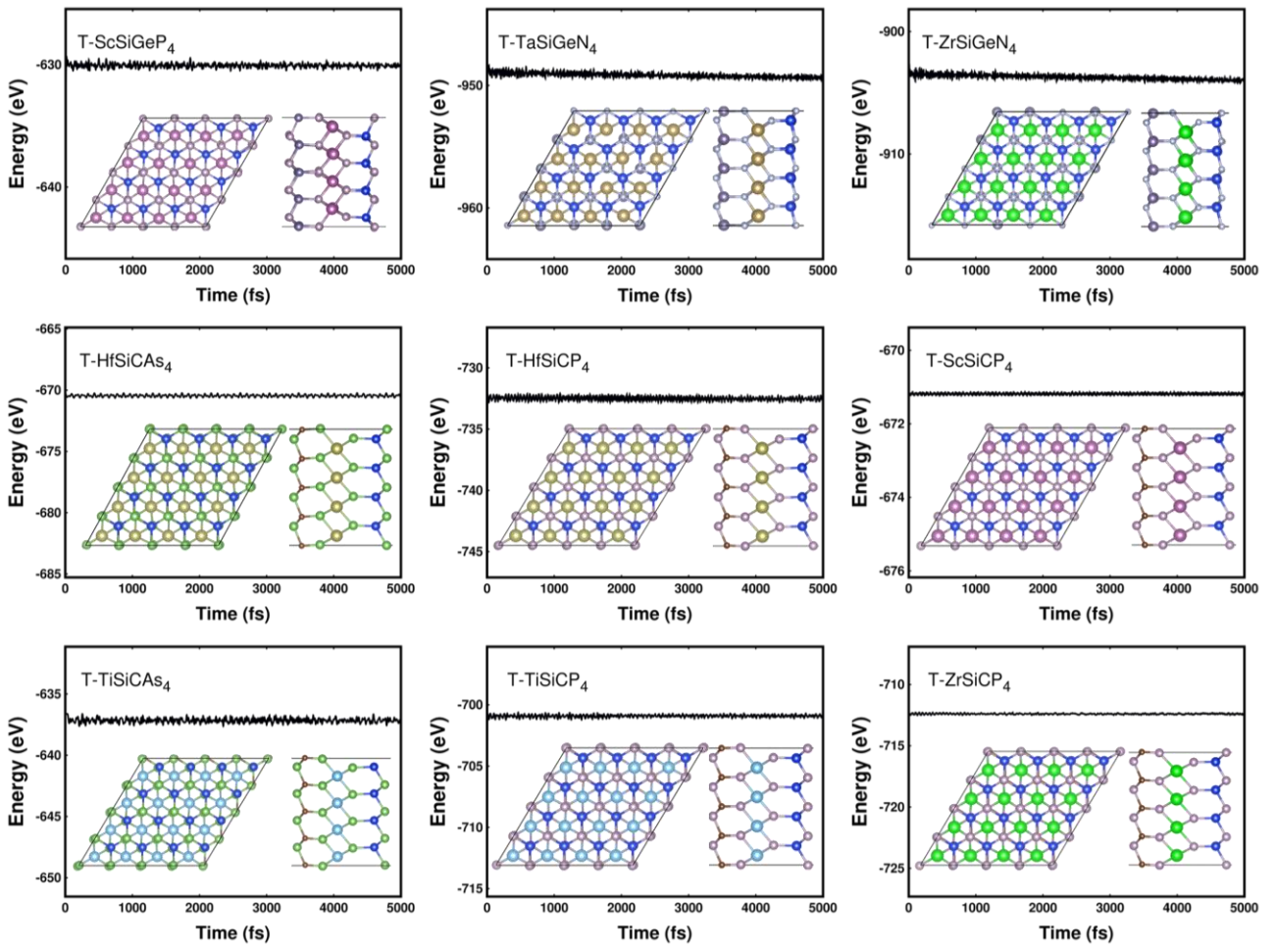
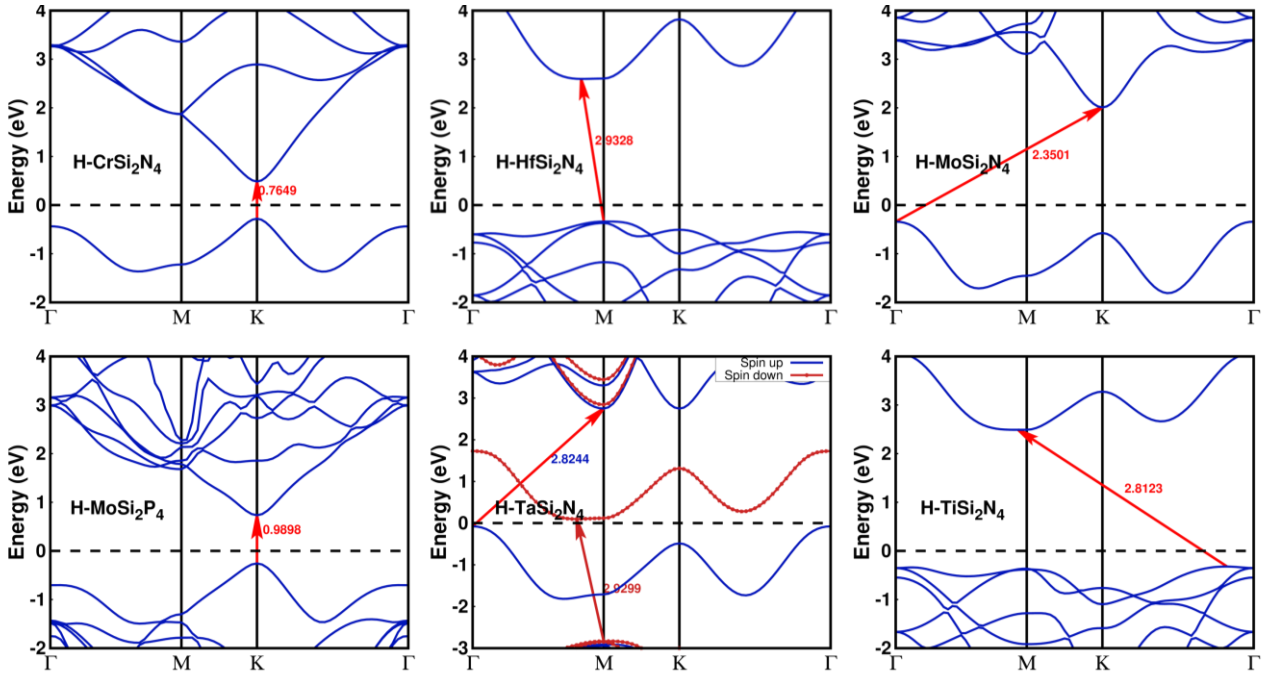


Fig. S4 The total potential energy and corresponding snapshots of the Janus MA_2Z_4 after stabilization at 300 K for 5 ps were obtained in the AIMD simulations.



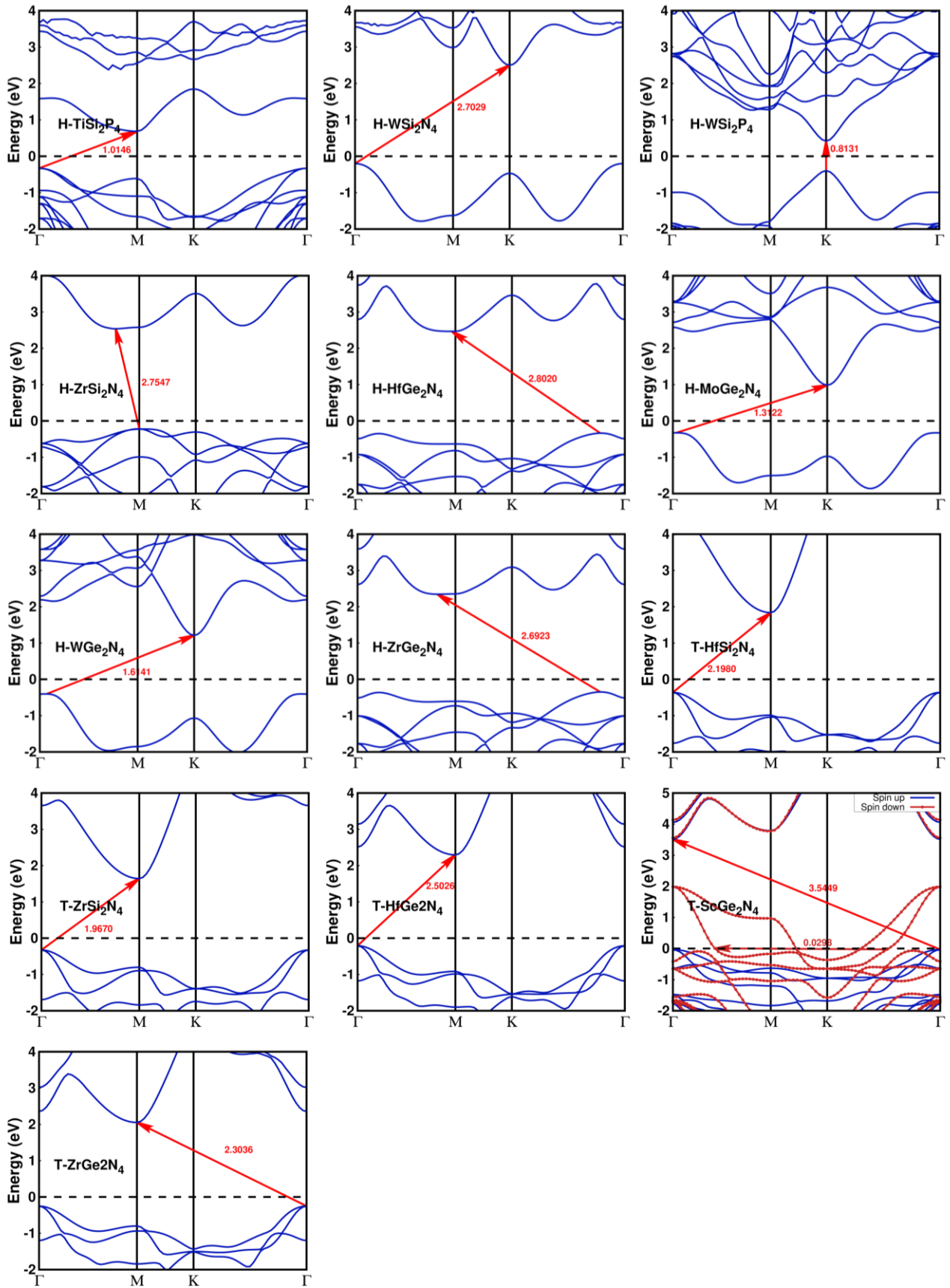
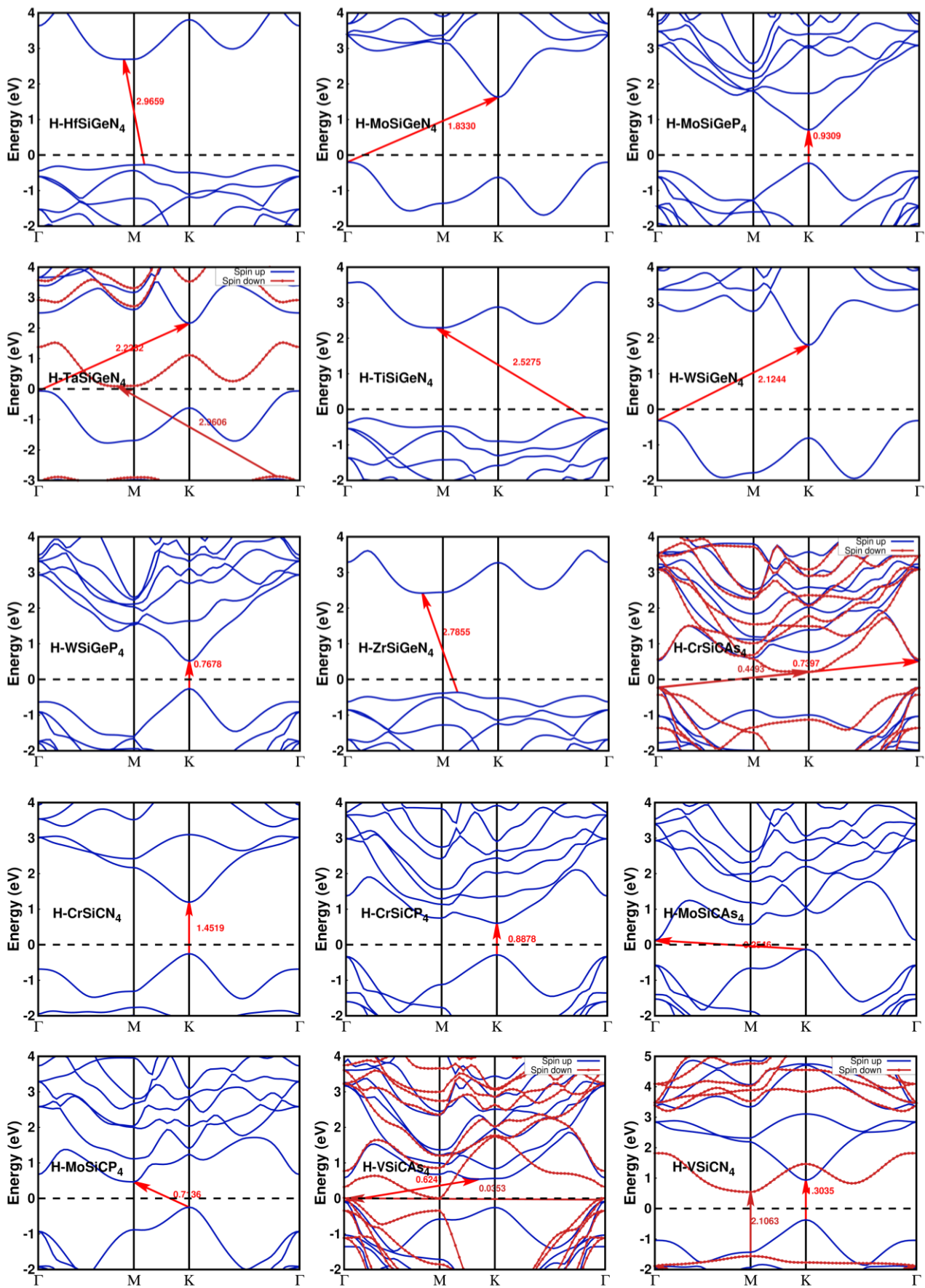


Fig. S5 Energy band structure diagrams of symmetric MA_2Z_4 structures.



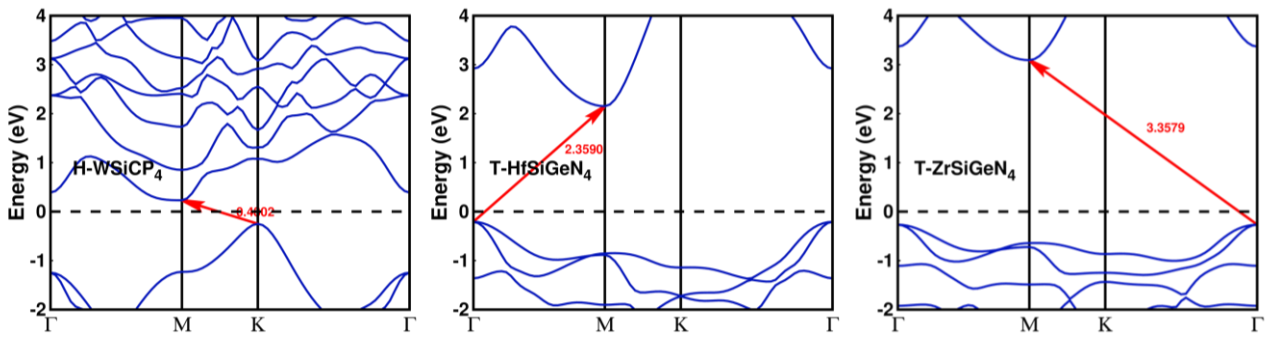
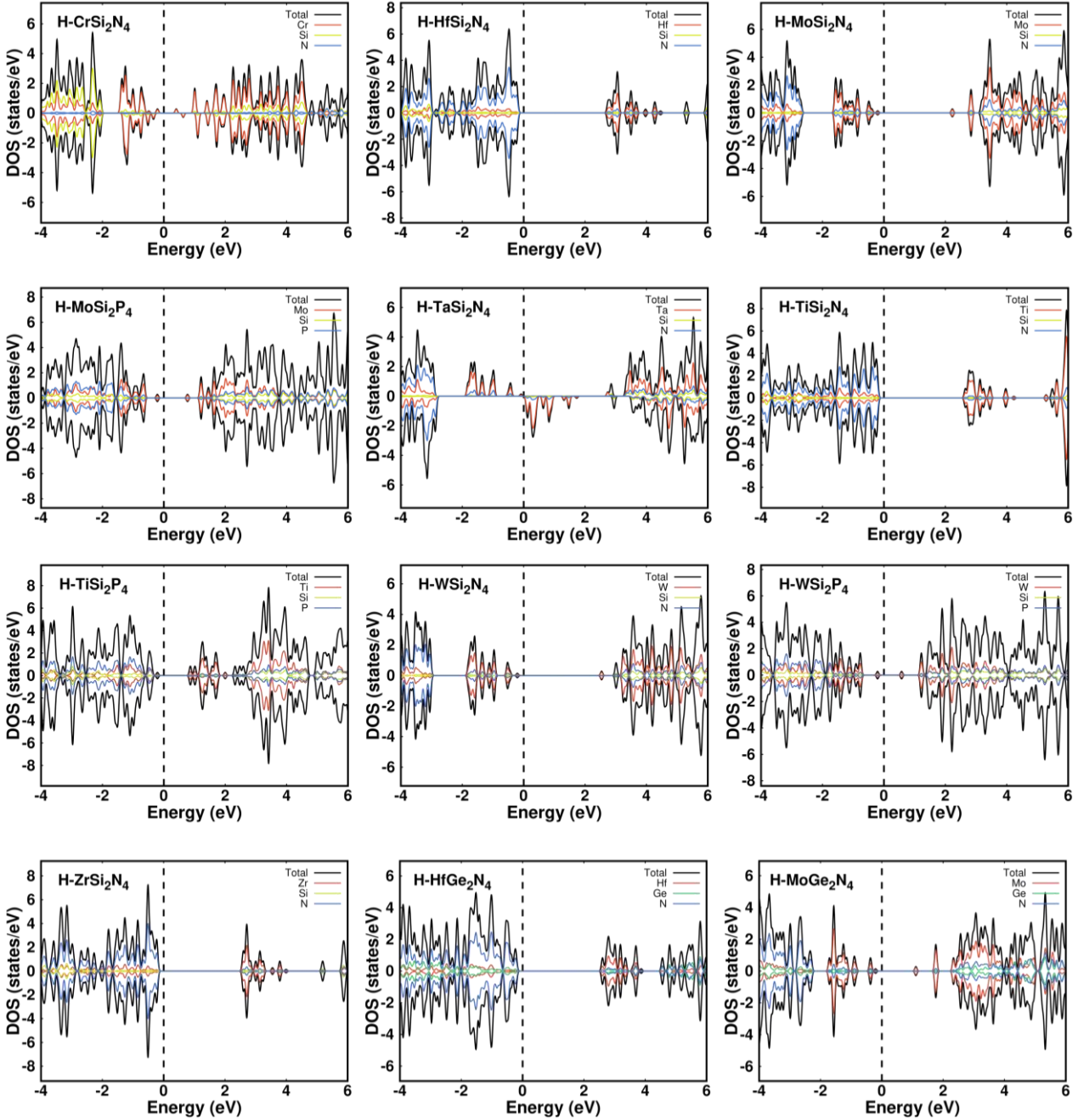


Fig. S6 Energy band structure diagrams of asymmetric Janus MA_2Z_4 structures.



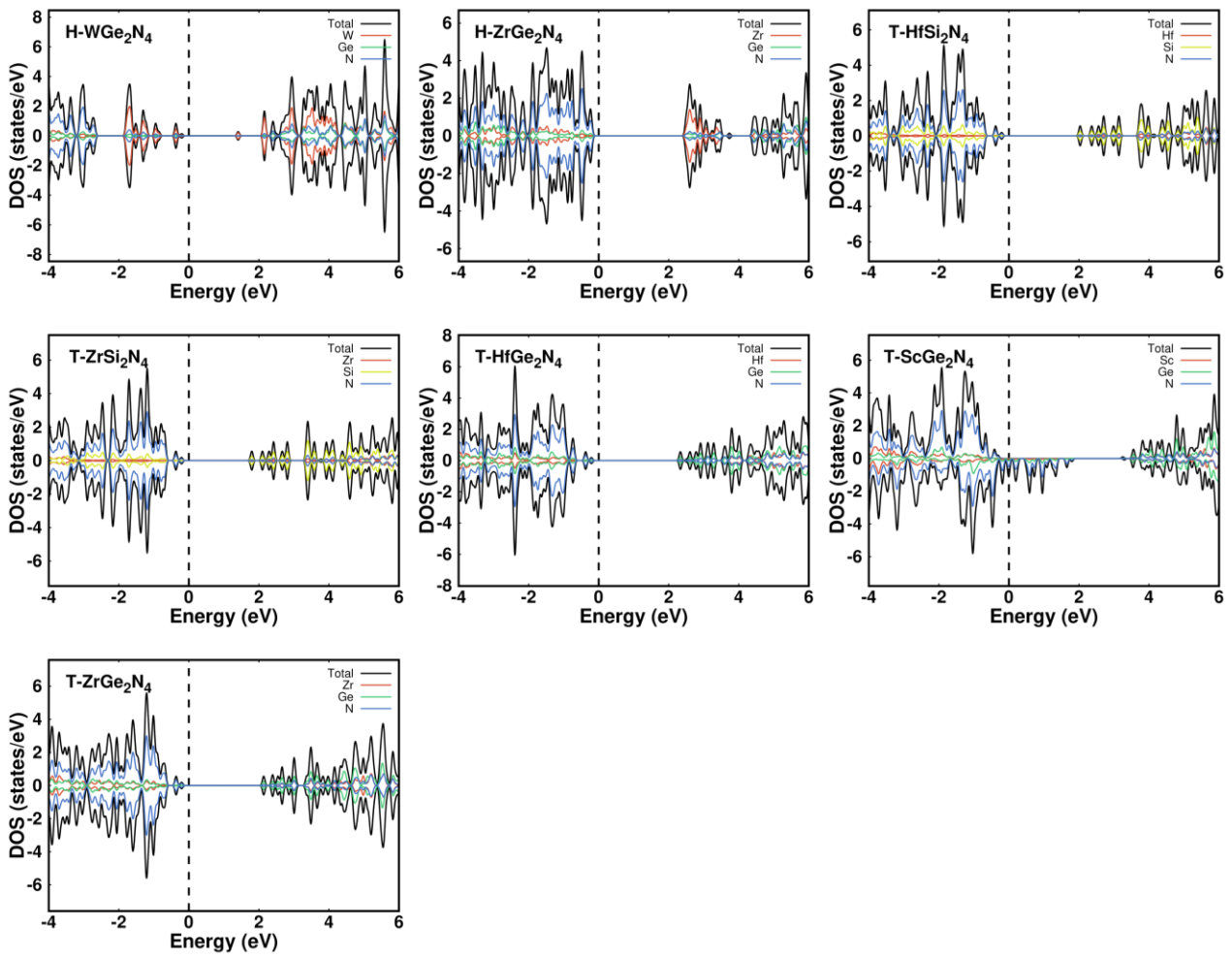
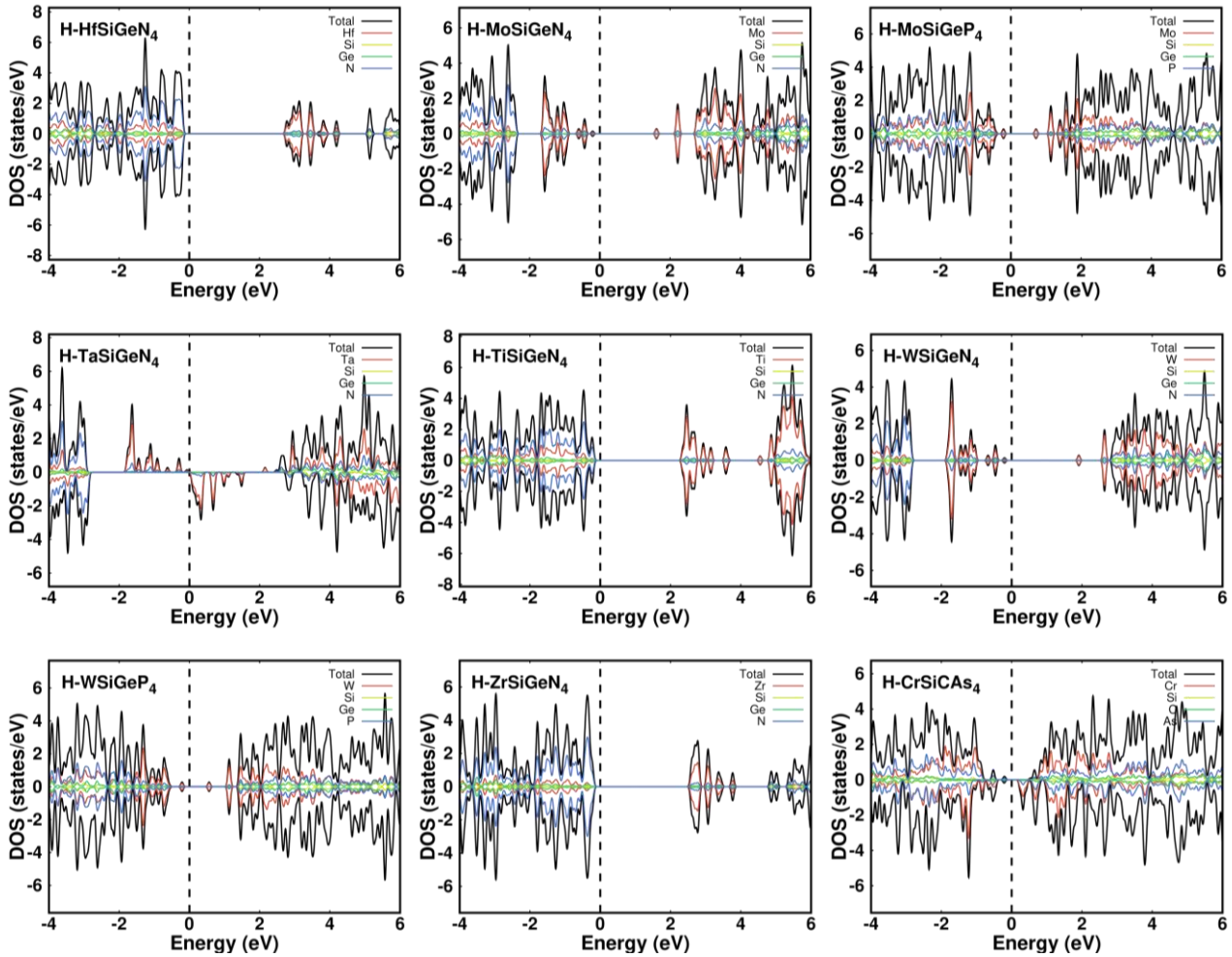


Fig. S7 TDOS and PDOS of symmetric MA_2Z_4 structure.



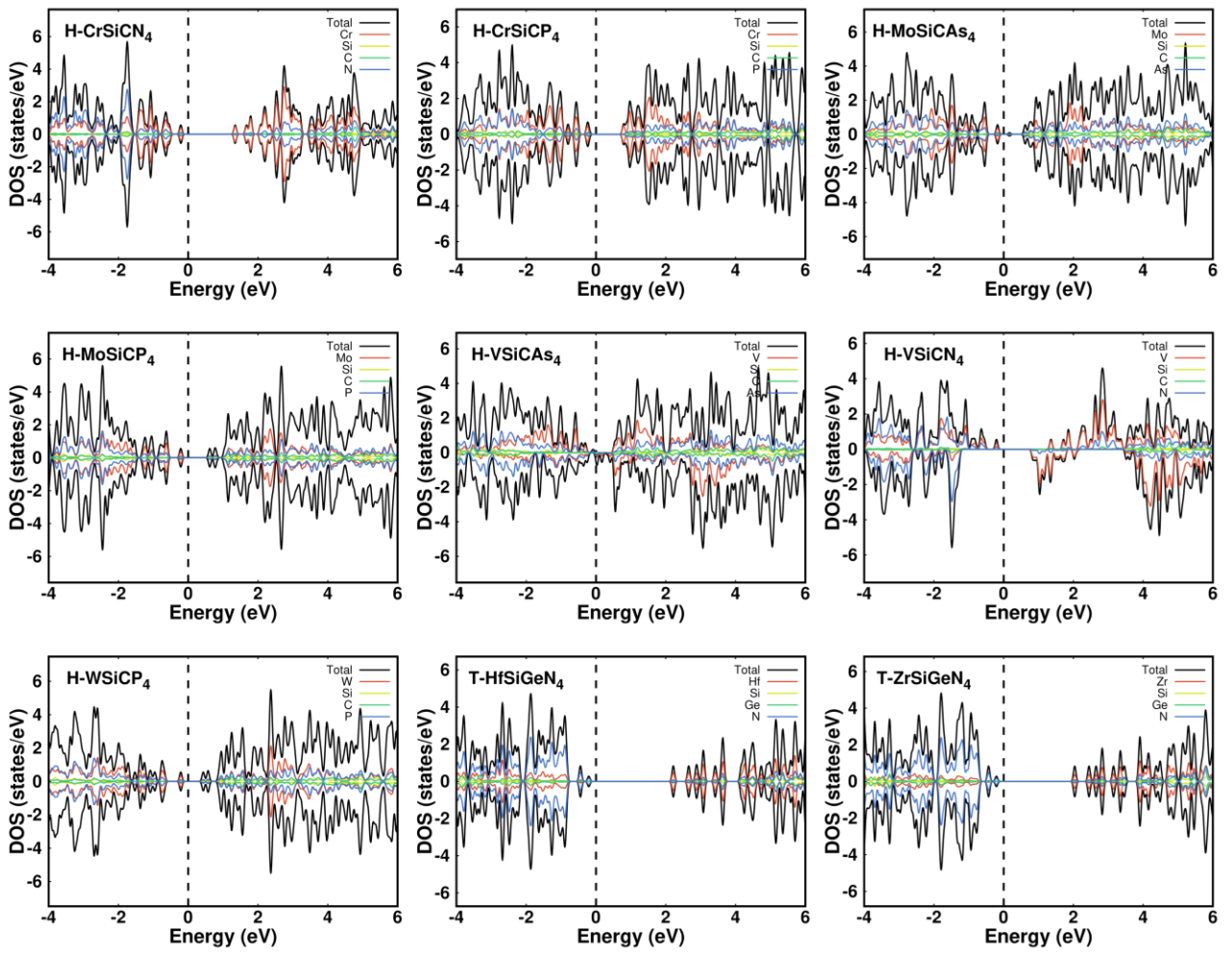
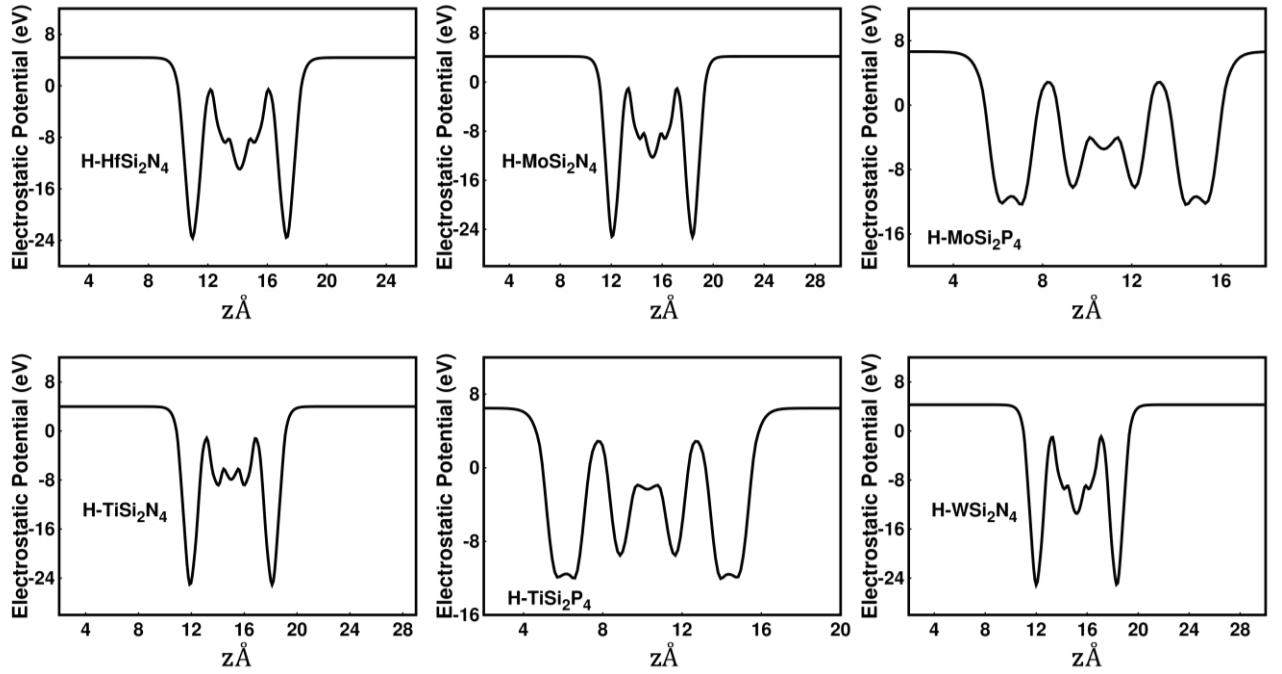


Fig. S8 TDOS and PDOS of asymmetric Janus MA_2Z_4 structures.



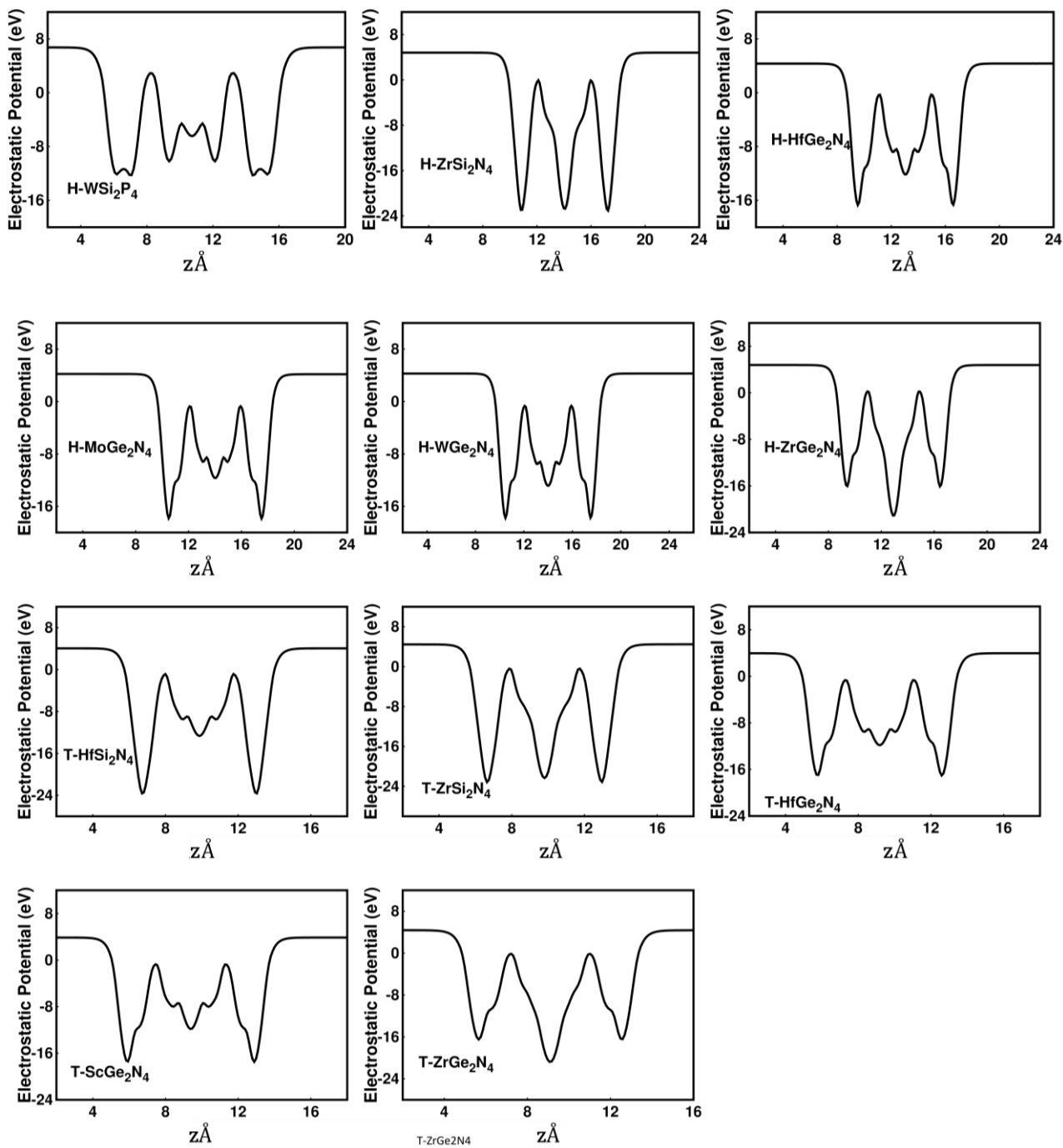
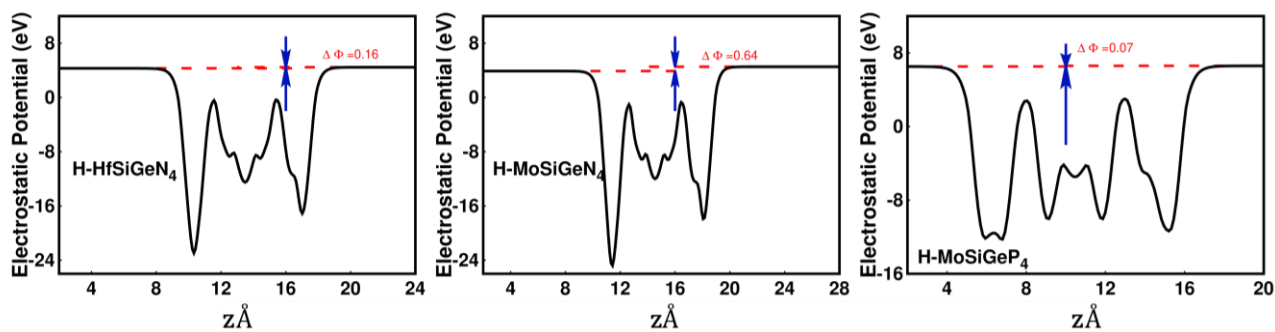


Fig. S9 Work function of symmetric structures.



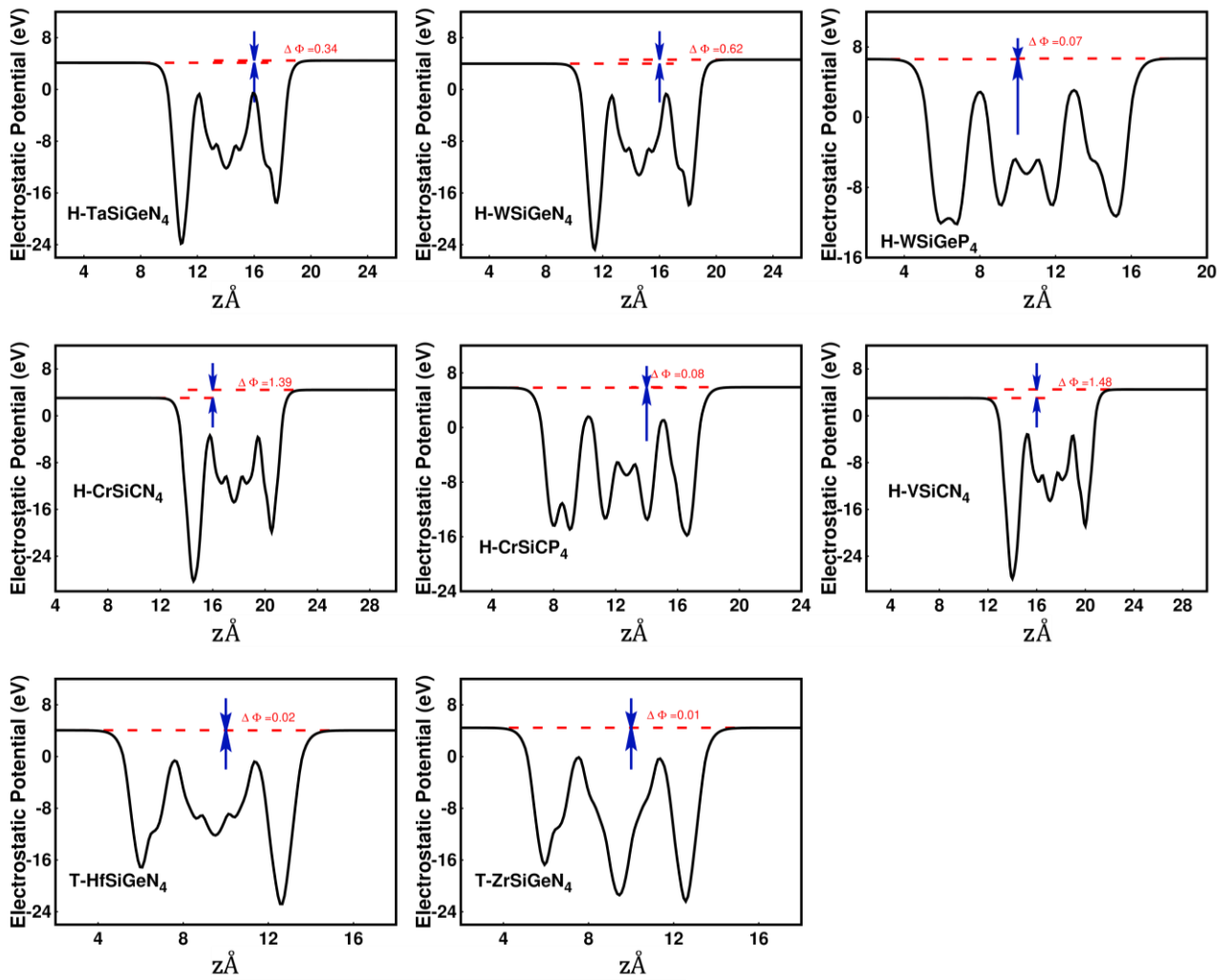


Fig. S10 work function of the Janus structures.

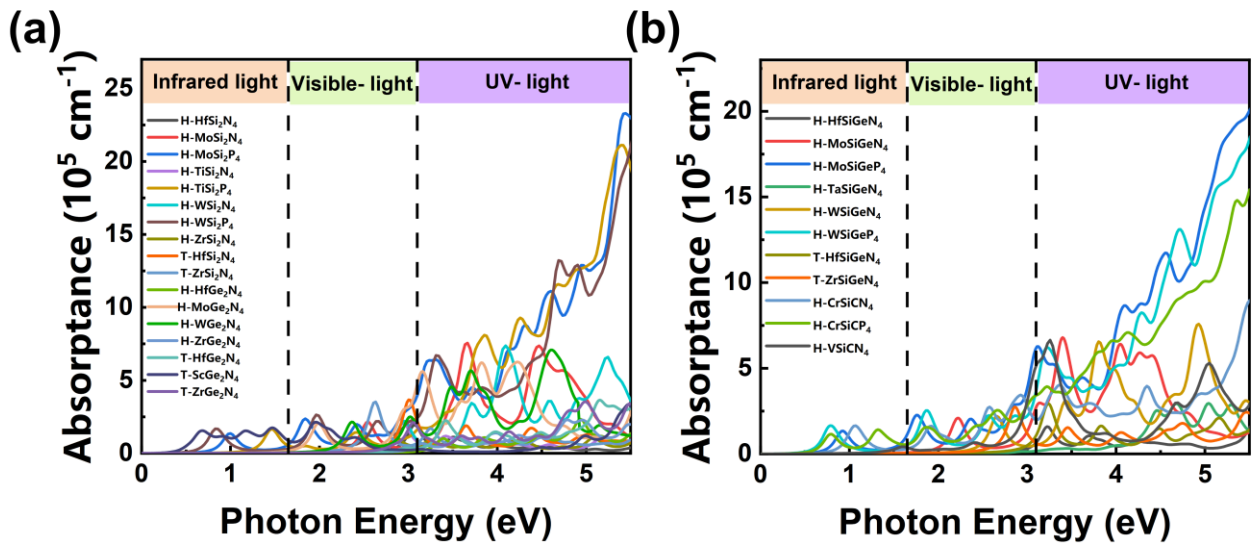


Fig. S11 Light absorption coefficients of Janus MA_2Z_4 and symmetric MA_2Z_4 .

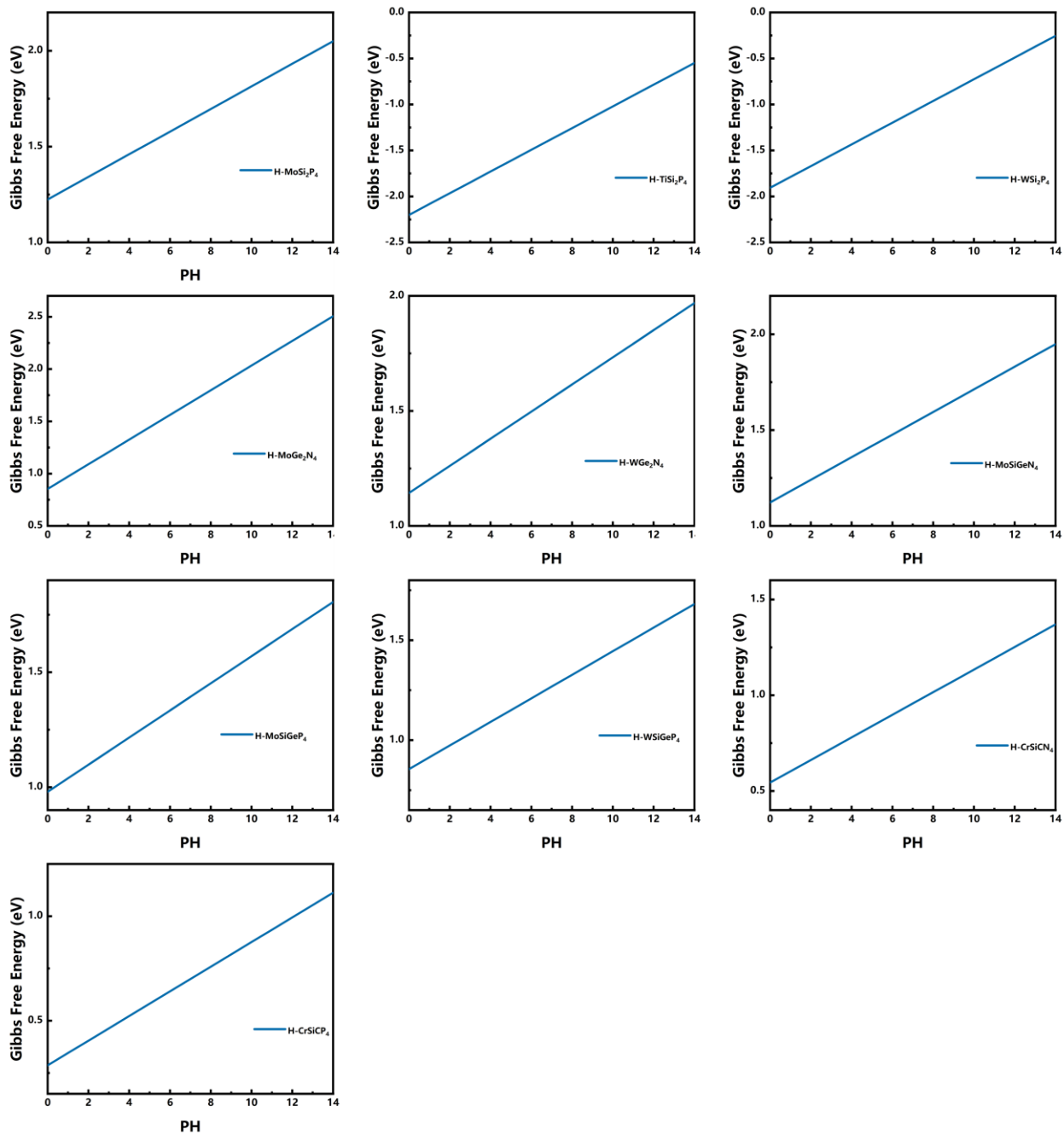


Fig. S12 HER adsorption energy at different PH.

Supporting Tables

Table S1 Formation energy of H phase symmetric MA₂Z₄ structures

Structure	E_f (eV)	Structure	E_f (eV)	Structure	E_f (eV)
H-CrSi ₂ As ₄	-1.53621	H-CrGe ₂ As ₄	-1.63928	H-CrC ₂ As ₄	-1.56927
H-CrSi ₂ N ₄	-4.55043	H-CrGe ₂ N ₄	-3.73512	H-CrC ₂ N ₄	-3.6433
H-CrSi ₂ P ₄	-1.53206	H-CrGe ₂ P ₄	-1.54771	H-CrC ₂ P ₄	-1.86761
H-CrSi ₂ S ₄	-2.1434	H-CrGe ₂ S ₄	-2.17696	H-CrC ₂ S ₄	-1.40492
H-CrSi ₂ Se ₄	-1.42037	H-CrGe ₂ Se ₄	-1.51632	H-CrC ₂ Se ₄	-0.65914
H-CrSi ₂ Te ₄	-1.07655	H-CrGe ₂ Te ₄	-1.20285	H-CrC ₂ Te ₄	-0.36513
H-HfSi ₂ As ₄	-1.7447	H-HfGe ₂ As ₄	-1.85079	H-HfC ₂ As ₄	-1.69599
H-HfSi ₂ N ₄	-4.89378	H-HfGe ₂ N ₄	-4.63656	H-HfC ₂ N ₄	-3.29147
H-HfSi ₂ P ₄	-1.5682	H-HfGe ₂ P ₄	-2.00537	H-HfC ₂ P ₄	-1.86402
H-HfSi ₂ S ₄	-2.55749	H-HfGe ₂ S ₄	-3.04349	H-HfC ₂ S ₄	-1.64121
H-HfSi ₂ Se ₄	-1.85125	H-HfGe ₂ Se ₄	-2.37868	H-HfC ₂ Se ₄	-0.92946
H-HfSi ₂ Te ₄	-1.46648	H-HfGe ₂ Te ₄	-2.01203	H-HfC ₂ Te ₄	-0.657
H-MoSi ₂ As ₄	-1.52403	H-MoGe ₂ As ₄	-1.62908	H-MoC ₂ As ₄	-1.54983
H-MoSi ₂ N ₄	-4.64147	H-MoGe ₂ N ₄	-3.87599	H-MoC ₂ N ₄	-3.4213
H-MoSi ₂ P ₄	-2.13252	H-MoGe ₂ P ₄	-1.46724	H-MoC ₂ P ₄	-1.80966
H-MoSi ₂ S ₄	-2.23908	H-MoGe ₂ S ₄	-2.27387	H-MoC ₂ S ₄	-1.39711
H-MoSi ₂ Se ₄	-1.5073	H-MoGe ₂ Se ₄	-1.59396	H-MoC ₂ Se ₄	-0.68717
H-MoSi ₂ Te ₄	-1.12603	H-MoGe ₂ Te ₄	-1.24886	H-MoC ₂ Te ₄	-0.40269
H-ScSi ₂ As ₄	-1.42546	H-ScGe ₂ As ₄	-1.52309	H-ScC ₂ As ₄	-1.39678
H-ScSi ₂ N ₄	-4.28884	H-ScGe ₂ N ₄	-3.616	H-ScC ₂ N ₄	-2.94745
H-ScSi ₂ P ₄	-1.25203	H-ScGe ₂ P ₄	-1.26996	H-ScC ₂ P ₄	-1.54435
H-ScSi ₂ S ₄	-2.23919	H-ScGe ₂ S ₄	-2.27827	H-ScC ₂ S ₄	-1.34176
H-ScSi ₂ Se ₄	-1.62636	H-ScGe ₂ Se ₄	-0.908611	H-ScC ₂ Se ₄	-0.66479
H-ScSi ₂ Te ₄	-1.20581	H-ScGe ₂ Te ₄	-1.36069	H-ScC ₂ Te ₄	-0.34624
H-TaSi ₂ As ₄	-1.73217	H-TaGe ₂ As ₄	-1.82522	H-TaC ₂ As ₄	-1.69654
H-TaSi ₂ N ₄	-4.89502	H-TaGe ₂ N ₄	-4.1775	H-TaC ₂ N ₄	-3.46986
H-TaSi ₂ P ₄	-1.60968	H-TaGe ₂ P ₄	-1.64091	H-TaC ₂ P ₄	-1.92664
H-TaSi ₂ S ₄	-2.48561	H-TaGe ₂ S ₄	-2.54342	H-TaC ₂ S ₄	-1.52162
H-TaSi ₂ Se ₄	-1.74104	H-TaGe ₂ Se ₄	-1.84757	H-TaC ₂ Se ₄	-0.8384
H-TaSi ₂ Te ₄	-1.3351	H-TaGe ₂ Te ₄	-1.48409	H-TaC ₂ Te ₄	-0.57411
H-TiSi ₂ As ₄	-1.61005	H-TiGe ₂ As ₄	-1.71538	H-TiC ₂ As ₄	-1.58024
H-TiSi ₂ N ₄	-4.69403	H-TiGe ₂ N ₄	-3.99473	H-TiC ₂ N ₄	-3.43092
H-TiSi ₂ P ₄	-2.11829	H-TiGe ₂ P ₄	-1.5269	H-TiC ₂ P ₄	-1.79553
H-TiSi ₂ S ₄	-2.19883	H-TiGe ₂ S ₄	-2.36603	H-TiC ₂ S ₄	-1.46633
H-TiSi ₂ Se ₄	-1.58424	H-TiGe ₂ Se ₄	-1.69752	H-TiC ₂ Se ₄	-0.74335
H-TiSi ₂ Te ₄	-1.2341	H-TiGe ₂ Te ₄	-1.38386	H-TiC ₂ Te ₄	-0.48188
H-VSi ₂ As ₄	-1.78022	H-VGe ₂ As ₄	-1.8758	H-VC ₂ As ₄	-1.78553
H-VSi ₂ N ₄	-4.84383	H-VGe ₂ N ₄	-4.07183	H-VC ₂ N ₄	-3.77692
H-VSi ₂ P ₄	-1.73466	H-VGe ₂ P ₄	-1.73928	H-VC ₂ P ₄	-2.05502
H-VSi ₂ S ₄	-2.3912	H-VGe ₂ S ₄	-2.44091	H-VC ₂ S ₄	-1.52521
H-VSi ₂ Se ₄	-1.67258	H-VGe ₂ Se ₄	-1.77744	H-VC ₂ Se ₄	-0.86367
H-VSi ₂ Te ₄	-1.32609	H-VGe ₂ Te ₄	-1.47082	H-VC ₂ Te ₄	-0.61326

H-WSi ₂ As ₄	-1.79064	H-WGe ₂ As ₄	-1.89099	H-WC ₂ As ₄	-1.7846
H-WSi ₂ N ₄	-4.9912	H-WGe ₂ N ₄	-4.19632	H-WC ₂ N ₄	-3.70007
H-WSi ₂ P ₄	-2.40938	H-WGe ₂ P ₄	-1.74217	H-WC ₂ P ₄	-2.06607
H-WSi ₂ S ₄	-2.52713	H-WGe ₂ S ₄	-2.54921	H-WC ₂ S ₄	-1.66244
H-WSi ₂ Se ₄	-1.776	H-WGe ₂ Se ₄	-1.85316	H-WC ₂ Se ₄	-0.94815
H-WSi ₂ Te ₄	-1.35792	H-WGe ₂ Te ₄	-1.47774	H-WC ₂ Te ₄	-0.45626
H-NbSi ₂ As ₄	-1.44653	H-NbGe ₂ As ₄	-1.54459	H-NbC ₂ As ₄	-1.4537
H-NbSi ₂ N ₄	-4.56341	H-NbGe ₂ N ₄	-3.85025	H-NbC ₂ N ₄	-3.18256
H-NbSi ₂ P ₄	-1.32455	H-NbGe ₂ P ₄	-1.35434	H-NbC ₂ P ₄	-1.66902
H-NbSi ₂ S ₄	-2.20329	H-NbGe ₂ S ₄	-2.26193	H-NbC ₂ S ₄	-1.27631
H-NbSi ₂ Se ₄	-1.47859	H-NbGe ₂ Se ₄	-1.58625	H-NbC ₂ Se ₄	-0.58924
H-NbSi ₂ Te ₄	-1.10014	H-NbGe ₂ Te ₄	-1.25018	H-NbC ₂ Te ₄	-0.34493
H-ZrSi ₂ As ₄	-1.59347	H-ZrGe ₂ As ₄	-1.69801	H-ZrC ₂ As ₄	-1.57142
H-ZrSi ₂ N ₄	-4.66275	H-ZrGe ₂ N ₄	-4.03093	H-ZrC ₂ N ₄	-3.05984
H-ZrSi ₂ P ₄	-1.40312	H-ZrGe ₂ P ₄	-1.44849	H-ZrC ₂ P ₄	-1.71953
H-ZrSi ₂ S ₄	-2.38198	H-ZrGe ₂ S ₄	-2.48195	H-ZrC ₂ S ₄	-1.50525
H-ZrSi ₂ Se ₄	-1.69436	H-ZrGe ₂ Se ₄	-1.83438	H-ZrC ₂ Se ₄	-0.80868
H-ZrSi ₂ Te ₄	-1.14951	H-ZrGe ₂ Te ₄	-1.48824	H-ZrC ₂ Te ₄	-0.54328

Table S2 Formation energy of T phase symmetric MA₂Z₄ structures

Structure	E_f (eV)	Structure	E_f (eV)	Structure	E_f (eV)
T-CrSi ₂ As ₄	-1.5511	T-CrGe ₂ As ₄	-1.6508	T-CrC ₂ As ₄	-1.537
T-CrSi ₂ N ₄	-4.49288	T-CrGe ₂ N ₄	-3.78382	T-CrC ₂ N ₄	-3.468
T-CrSi ₂ P ₄	-1.98958	T-CrGe ₂ P ₄	-1.5433	T-CrC ₂ P ₄	-1.82064
T-CrSi ₂ S ₄	-2.12426	T-CrGe ₂ S ₄	-2.12045	T-CrC ₂ S ₄	-1.46269
T-CrSi ₂ Se ₄	-1.34752	T-CrGe ₂ Se ₄	-1.14884	T-CrC ₂ Se ₄	-0.61724
T-CrSi ₂ Te ₄	-0.70589	T-CrGe ₂ Te ₄	-0.94443	T-CrC ₂ Te ₄	-0.33027
T-HfSi ₂ As ₄	-1.74432	T-HfGe ₂ As ₄	-1.85592	T-HfC ₂ As ₄	-1.70519
T-HfSi ₂ N ₄	-4.93828	T-HfGe ₂ N ₄	-4.35005	T-HfC ₂ N ₄	-3.30124
T-HfSi ₂ P ₄	-1.19925	T-HfGe ₂ P ₄	-0.3817	T-HfC ₂ P ₄	-1.87501
T-HfSi ₂ S ₄	-2.59429	T-HfGe ₂ S ₄	-2.67479	T-HfC ₂ S ₄	-1.78399
T-HfSi ₂ Se ₄	-1.87271	T-HfGe ₂ Se ₄	-1.84263	T-HfC ₂ Se ₄	-0.91709
T-HfSi ₂ Te ₄	-1.24485	T-HfGe ₂ Te ₄	-1.20623	T-HfC ₂ Te ₄	-0.65717
T-MoSi ₂ As ₄	-1.52782	T-MoGe ₂ As ₄	-1.64113	T-MoC ₂ As ₄	-1.5132
T-MoSi ₂ N ₄	-4.50542	T-MoGe ₂ N ₄	-3.79711	T-MoC ₂ N ₄	-3.28271
T-MoSi ₂ P ₄	-2.04001	T-MoGe ₂ P ₄	-1.47312	T-MoC ₂ P ₄	-1.7565
T-MoSi ₂ S ₄	-2.12877	T-MoGe ₂ S ₄	-2.16953	T-MoC ₂ S ₄	-1.37282
T-MoSi ₂ Se ₄	-1.36358	T-MoGe ₂ Se ₄	-1.49855	T-MoC ₂ Se ₄	-0.60782
T-MoSi ₂ Te ₄	-0.87196	T-MoGe ₂ Te ₄	-0.95342	T-MoC ₂ Te ₄	-0.36418
T-ScSi ₂ As ₄	-1.43117	T-ScGe ₂ As ₄	-1.54375	T-ScC ₂ As ₄	-1.40608
T-ScSi ₂ N ₄	-4.36035	T-ScGe ₂ N ₄	-3.75179	T-ScC ₂ N ₄	-2.95526
T-ScSi ₂ P ₄	-1.97251	T-ScGe ₂ P ₄	-1.27643	T-ScC ₂ P ₄	-1.55778
T-ScSi ₂ S ₄	-2.30833	T-ScGe ₂ S ₄	-2.27294	T-ScC ₂ S ₄	-1.40089
T-ScSi ₂ Se ₄	-1.54098	T-ScGe ₂ Se ₄	-1.53522	T-ScC ₂ Se ₄	-0.72684
T-ScSi ₂ Te ₄	-0.94383	T-ScGe ₂ Te ₄	-0.90861	T-ScC ₂ Te ₄	-0.34375

T-TaSi ₂ As ₄	-1.72198	T-TaGe ₂ As ₄	-1.89299	T-TaC ₂ As ₄	-1.69568
T-TaSi ₂ N ₄	-4.85765	T-TaGe ₂ N ₄	-4.20077	T-TaC ₂ N ₄	-3.42461
T-TaSi ₂ P ₄	-2.28187	T-TaGe ₂ P ₄	-2.13653	T-TaC ₂ P ₄	-1.91821
T-TaSi ₂ S ₄	-2.46455	T-TaGe ₂ S ₄	-0.5596	T-TaC ₂ S ₄	-1.64813
T-TaSi ₂ Se ₄	-1.6546	T-TaGe ₂ Se ₄	-1.79115	T-TaC ₂ Se ₄	-0.83719
T-TaSi ₂ Te ₄	-1.19429	T-TaGe ₂ Te ₄	-1.0918	T-TaC ₂ Te ₄	-0.57685
T-TiSi ₂ As ₄	-1.81111	T-TiGe ₂ As ₄	-1.72396	T-TiC ₂ As ₄	-1.61246
T-TiSi ₂ N ₄	-4.79721	T-TiGe ₂ N ₄	-4.12206	T-TiC ₂ N ₄	-3.42972
T-TiSi ₂ P ₄	-1.69661	T-TiGe ₂ P ₄	-1.53292	T-TiC ₂ P ₄	-1.83015
T-TiSi ₂ S ₄	-2.36102	T-TiGe ₂ S ₄	-2.48353	T-TiC ₂ S ₄	-1.62283
T-TiSi ₂ Se ₄	-1.57864	T-TiGe ₂ Se ₄	-1.75388	T-TiC ₂ Se ₄	-0.75634
T-TiSi ₂ Te ₄	-1.07956	T-TiGe ₂ Te ₄	-1.06497	T-TiC ₂ Te ₄	-0.43615
T-VSi ₂ As ₄	-1.79358	T-VGe ₂ As ₄	-1.89761	T-VC ₂ As ₄	-1.78014
T-VSi ₂ N ₄	-4.85948	T-VGe ₂ N ₄	-4.13912	T-VC ₂ N ₄	-3.70041
T-VSi ₂ P ₄	-1.77239	T-VGe ₂ P ₄	-1.76557	T-VC ₂ P ₄	-2.04167
T-VSi ₂ S ₄	-2.4109	T-VGe ₂ S ₄	-2.38913	T-VC ₂ S ₄	-1.68442
T-VSi ₂ Se ₄	-1.65409	T-VGe ₂ Se ₄	-1.78961	T-VC ₂ Se ₄	-0.86798
T-VSi ₂ Te ₄	-1.22613	T-VGe ₂ Te ₄	-1.26821	T-VC ₂ Te ₄	-0.64419
T-WSi ₂ As ₄	-1.85038	T-WGe ₂ As ₄	-1.90214	T-WC ₂ As ₄	-1.74249
T-WSi ₂ N ₄	-4.80486	T-WGe ₂ N ₄	-4.09966	T-WC ₂ N ₄	-3.55408
T-WSi ₂ P ₄	-2.30652	T-WGe ₂ P ₄	-2.15299	T-WC ₂ P ₄	-2.00976
T-WSi ₂ S ₄	-2.39804	T-WGe ₂ S ₄	-2.43973	T-WC ₂ S ₄	-1.56022
T-WSi ₂ Se ₄	-1.6157	T-WGe ₂ Se ₄	-1.67523	T-WC ₂ Se ₄	-0.86096
T-WSi ₂ Te ₄	-1.18264	T-WGe ₂ Te ₄	-1.16778	T-WC ₂ Te ₄	-0.51633
T-NbSi ₂ As ₄	-1.45194	T-NbGe ₂ As ₄	-1.56846	T-NbC ₂ As ₄	-1.4479
T-NbSi ₂ N ₄	-4.53975	T-NbGe ₂ N ₄	-3.87861	T-NbC ₂ N ₄	-3.14413
T-NbSi ₂ P ₄	-1.32485	T-NbGe ₂ P ₄	-1.69598	T-NbC ₂ P ₄	-1.65539
T-NbSi ₂ S ₄	-2.18617	T-NbGe ₂ S ₄	-1.78242	T-NbC ₂ S ₄	-1.42672
T-NbSi ₂ Se ₄	-1.50848	T-NbGe ₂ Se ₄	-1.39576	T-NbC ₂ Se ₄	-0.58621
T-NbSi ₂ Te ₄	-1.51507	T-NbGe ₂ Te ₄	-0.79837	T-NbC ₂ Te ₄	-0.38353
T-ZrSi ₂ As ₄	-1.60182	T-ZrGe ₂ As ₄	-1.7262	T-ZrC ₂ As ₄	-1.58788
T-ZrSi ₂ N ₄	-4.69926	T-ZrGe ₂ N ₄	-4.12463	T-ZrC ₂ N ₄	-3.08332
T-ZrSi ₂ P ₄	-1.4071	T-ZrGe ₂ P ₄	-1.44973	T-ZrC ₂ P ₄	-1.73552
T-ZrSi ₂ S ₄	-2.48172	T-ZrGe ₂ S ₄	-2.49479	T-ZrC ₂ S ₄	-1.67933
T-ZrSi ₂ Se ₄	-1.61098	T-ZrGe ₂ Se ₄	-1.68485	T-ZrC ₂ Se ₄	-0.79306
T-ZrSi ₂ Te ₄	-1.18479	T-ZrGe ₂ Te ₄	-1.07389	T-ZrC ₂ Te ₄	-0.50584

Table S3 Formation energy of asymmetric H-MA₂Z₄ Janus structures

Structure	E_f (eV)	Structure	E_f (eV)	Structure	E_f (eV)
H-CrSiGeAs ₄	-1.36623	H-CrCGeAs ₄	-1.59844	H-CrSiCA ₄	-1.66695
H-CrSiGeN ₄	-4.10545	H-CrCGeN ₄	-3.42759	H-CrSiCN ₄	-3.95802
H-CrSiGeP ₄	-1.52787	H-CrCGeP ₄	-1.66665	H-CrSiCP ₄	-1.85087
H-CrSiGeS ₄	-2.14441	H-CrCGeS ₄	-1.69714	H-CrSiCS ₄	-1.67321
H-CrSiGeSe ₄	-1.45521	H-CrCGeSe ₄	-1.02063	H-CrSiCSe ₄	-1.00171
H-CrSiGeTe ₄	-1.06429	H-CrCGeTe ₄	-0.8259	H-CrSiCTe ₄	-0.69743

H-HfSiGeAs ₄	-1.80188	H-HfCGeAs ₄	-1.78439	H-HfSiCAs ₄	-1.85057
H-HfSiGeN ₄	-4.55369	H-HfCGeN ₄	-3.66795	H-HfSiCN ₄	-4.04652
H-HfSiGeP ₄	-1.58375	H-HfCGeP ₄	-1.83137	H-HfSiCP ₄	-1.94328
H-HfSiGeS ₄	-2.60136	H-HfCGeS ₄	-2.15277	H-HfSiCS ₄	-2.10656
H-HfSiGeSe ₄	-1.91645	H-HfCGeSe ₄	-1.46882	H-HfSiCSe ₄	-1.39863
H-HfSiGeTe ₄	-1.54028	H-HfCGeTe ₄	-1.14284	H-HfSiCTe ₄	-1.06871
H-MoSiGeAs ₄	-1.58236	H-MoCGeAs ₄	-1.63811	H-MoSiCAs ₄	-1.70428
H-MoSiGeN ₄	-4.23105	H-MoCGeN ₄	-3.44157	H-MoSiCN ₄	-3.92125
H-MoSiGeP ₄	-2.04205	H-MoCGeP ₄	-1.75658	H-MoSiCP ₄	-1.87895
H-MoSiGeS ₄	-2.2499	H-MoCGeS ₄	-1.76548	H-MoSiCS ₄	-1.77623
H-MoSiGeSe ₄	-1.54721	H-MoCGeSe ₄	-1.09144	H-MoSiCSe ₄	-1.06706
H-MoSiGeTe ₄	-1.18682	H-MoCGeTe ₄	-0.77586	H-MoSiCTe ₄	-0.73034
H-NbSiGeAs ₄	-1.50375	H-ScCGeAs ₄	-1.46302	H-ScSiCAs ₄	-1.53061
H-NbSiGeN ₄	-4.1886	H-ScCGeN ₄	-3.21557	H-ScSiCN ₄	-3.58331
H-NbSiGeP ₄	-1.3337	H-ScCGeP ₄	-1.405	H-ScSiCP ₄	-1.57326
H-NbSiGeS ₄	-2.22911	H-ScCGeS ₄	-1.85511	H-ScSiCS ₄	-1.75155
H-NbSiGeSe ₄	-1.5304	H-ScCGeSe ₄	-1.20225	H-ScSiCSe ₄	-1.13049
H-NbSiGeTe ₄	-1.17419	H-ScCGeTe ₄	-0.89171	H-ScSiCTe ₄	-0.8138
H-ScSiGeAs ₄	-1.48104	H-TaCGeAs ₄	-1.79874	H-TaSiCAs ₄	-1.85904
H-ScSiGeN ₄	-3.93607	H-TaCGeN ₄	-3.66914	H-TaSiCN ₄	-4.10121
H-ScSiGeP ₄	-1.25656	H-TaCGeP ₄	-1.79773	H-TaSiCP ₄	-2.01707
H-ScSiGeS ₄	-2.30731	H-TaCGeS ₄	-2.06128	H-TaSiCS ₄	-2.03189
H-ScSiGeSe ₄	-1.62742	H-TaCGeSe ₄	-1.31135	H-TaSiCSe ₄	-1.27265
H-ScSiGeTe ₄	-1.28841	H-TaCGeTe ₄	-1.01779	H-TaSiCTe ₄	-0.94233
H-TaSiGeAs ₄	-1.78539	H-TiCGeAs ₄	-1.63682	H-TiSiCAs ₄	-1.69721
H-TaSiGeN ₄	-4.51876	H-TiCGeN ₄	-3.5046	H-TiSiCN ₄	-3.95433
H-TaSiGeP ₄	-1.62439	H-TiCGeP ₄	-1.6395	H-TiSiCP ₄	-1.7968
H-TaSiGeS ₄	-2.51037	H-TiCGeS ₄	-1.92019	H-TiSiCS ₄	-1.88852
H-TaSiGeSe ₄	-1.79234	H-TiCGeSe ₄	-1.23887	H-TiSiCSe ₄	-1.17979
H-TaSiGeTe ₄	-1.40845	H-TiCGeTe ₄	-0.92773	H-TiSiCTe ₄	-0.85283
H-TiSiGeAs ₄	-1.65926	H-VCGeAs ₄	-1.81125	H-VSiCAs ₄	-1.88248
H-TiSiGeN ₄	-4.30737	H-VCGeN ₄	-3.68159	H-VSiCN ₄	-4.17761
H-TiSiGeP ₄	-1.50932	H-VCGeP ₄	-1.85986	H-VSiCP ₄	-2.03935
H-TiSiGeS ₄	-2.27897	H-VCGeS ₄	-2.01622	H-VSiCS ₄	-1.99869
H-TiSiGeSe ₄	-1.6376	H-VCGeSe ₄	-1.31813	H-VSiCSe ₄	-1.26749
H-TiSiGeTe ₄	-1.21804	H-VCGeTe ₄	-1.02639	H-VSiCTe ₄	-0.95792
H-VSiGeAs ₄	-1.82414	H-WCGeAs ₄	-1.88417	H-WSiCAs ₄	-1.94967
H-VSiGeN ₄	-4.42516	H-WCGeN ₄	-3.78308	H-WSiCN ₄	-4.26092
H-VSiGeP ₄	-1.73073	H-WCGeP ₄	-2.03259	H-WSiCP ₄	-2.15376
H-VSiGeS ₄	-2.40363	H-WCGeS ₄	-2.05362	H-WSiCS ₄	-2.063
H-VSiGeSe ₄	-1.71578	H-WCGeSe ₄	-1.36187	H-WSiCSe ₄	-1.33768
H-VSiGeTe ₄	-3.171	H-WCGeTe ₄	-1.01684	H-WSiCTe ₄	-0.96323
H-WSiGeAs ₄	-1.84705	H-NbCGeAs ₄	-1.50099	H-NbSiCAs ₄	-1.60596
H-WSiGeN ₄	-4.58006	H-NbCGeN ₄	-3.34495	H-NbSiCN ₄	-3.77865
H-WSiGeP ₄	-2.31957	H-NbCGeP ₄	-1.6288	H-NbSiCP ₄	-1.74694
H-WSiGeS ₄	-2.3799	H-NbCGeS ₄	-1.80353	H-NbSiCS ₄	-1.77366

H-WSiGeSe ₄	-1.81506	H-NbCGeSe ₄	-1.10172	H-NbSiCSe ₄	-1.04456
H-WSiGeTe ₄	-1.41998	H-NbCGeTe ₄	-0.78532	H-NbSiCTe ₄	-0.71373
H-ZrSiGeAs ₄	-1.65061	H-ZrCGeAs ₄	-1.64529	H-ZrSiCAs ₄	-1.72663
H-ZrSiGeN ₄	-4.32969	H-ZrCGeN ₄	-3.44086	H-ZrSiCN ₄	-3.80896
H-ZrSiGeP ₄	-2.10452	H-ZrCGeP ₄	-1.59924	H-ZrSiCP ₄	-1.80263
H-ZrSiGeS ₄	-2.41149	H-ZrCGeS ₄	-1.99426	H-ZrSiCS ₄	-1.94607
H-ZrSiGeSe ₄	-1.76241	H-ZrCGeSe ₄	-1.32332	H-ZrSiCSe ₄	-1.25506
H-ZrSiGeTe ₄	-1.40952	H-ZrCGeTe ₄	-1.03285	H-ZrSiCTe ₄	-0.95487

Table S4 Formation energy of asymmetric T-MA₂Z₄ Janus structures

Structure	E_f (eV)	Structure	E_f (eV)	Structure	E_f (eV)
T-CrSiGeAs ₄	-1.59324	T-CrCGeAs ₄	-1.56369	T-CrSiCAs ₄	-1.62663
T-CrSiGeN ₄	-4.07856	T-CrCGeN ₄	-3.41207	T-CrSiCN ₄	-3.83853
T-CrSiGeP ₄	-1.88767	T-CrCGeP ₄	-1.65354	T-CrSiCP ₄	-1.79108
T-CrSiGeS ₄	-2.08851	T-CrCGeS ₄	-1.89621	T-CrSiCS ₄	-1.83343
T-CrSiGeSe ₄	-1.45314	T-CrCGeSe ₄	-1.14886	T-CrSiCSe ₄	-0.97089
T-CrSiGeTe ₄	-0.89211	T-CrCGeTe ₄	-0.76139	T-CrSiCTe ₄	-0.74577
T-HfSiGeAs ₄	-1.812	T-HfCGeAs ₄	-1.83824	T-HfSiCAs ₄	-1.89724
T-HfSiGeN ₄	-4.61513	T-HfCGeN ₄	-3.6932	T-HfSiCN ₄	-4.06455
T-HfSiGeP ₄	-1.58474	T-HfCGeP ₄	-1.87852	T-HfSiCP ₄	-1.98977
T-HfSiGeS ₄	-2.63783	T-HfCGeS ₄	-2.26249	T-HfSiCS ₄	-2.20809
T-HfSiGeSe ₄	-1.91767	T-HfCGeSe ₄	-1.4733	T-HfSiCSe ₄	-1.43856
T-HfSiGeTe ₄	-1.25119	T-HfCGeTe ₄	-0.98712	T-HfSiCTe ₄	-0.9848
T-MoSiGeAs ₄	-1.83865	T-MoCGeAs ₄	-1.58361	T-MoSiCAs ₄	-1.64624
T-MoSiGeN ₄	-4.08388	T-MoCGeN ₄	-3.30393	T-MoSiCN ₄	-3.77869
T-MoSiGeP ₄	-1.94876	T-MoCGeP ₄	-1.62043	T-MoSiCP ₄	-1.80545
T-MoSiGeS ₄	-2.13487	T-MoCGeS ₄	-1.76009	T-MoSiCS ₄	-1.76098
T-MoSiGeSe ₄	-1.46604	T-MoCGeSe ₄	-0.98835	T-MoSiCSe ₄	-0.96936
T-MoSiGeTe ₄	-0.89296	T-MoCGeTe ₄	-0.69851	T-MoSiCTe ₄	-0.69578
T-NbSiGeAs ₄	-1.57146	T-ScCGeAs ₄	-1.47432	T-ScSiCAs ₄	-1.57574
T-NbSiGeN ₄	-4.16629	T-ScCGeN ₄	-3.35448	T-ScSiCN ₄	-3.72055
T-NbSiGeP ₄	-1.91651	T-ScCGeP ₄	-1.41799	T-ScSiCP ₄	-1.61195
T-NbSiGeS ₄	-2.20838	T-ScCGeS ₄	-2.00956	T-ScSiCS ₄	-1.93393
T-NbSiGeSe ₄	-1.50284	T-ScCGeSe ₄	-1.22012	T-ScSiCSe ₄	-1.10121
T-NbSiGeTe ₄	-0.93978	T-ScCGeTe ₄	-0.72507	T-ScSiCTe ₄	-0.66915
T-ScSiGeAs ₄	-1.48293	T-TaCGeAs ₄	-1.78487	T-TaSiCAs ₄	-1.84647
T-ScSiGeN ₄	-4.01767	T-TaCGeN ₄	-3.6311	T-TaSiCN ₄	-4.06422
T-ScSiGeP ₄	-1.89887	T-TaCGeP ₄	-1.88281	T-TaSiCP ₄	-1.99984
T-ScSiGeS ₄	-2.27891	T-TaCGeS ₄	-2.094	T-TaSiCS ₄	-2.07424
T-ScSiGeSe ₄	-1.63514	T-TaCGeSe ₄	-1.30283	T-TaSiCSe ₄	-1.2607
T-ScSiGeTe ₄	-0.95849	T-TaCGeTe ₄	-0.87775	T-TaSiCTe ₄	-0.82831
T-TaSiGeAs ₄	-1.8369	T-TiCGeAs ₄	-1.66481	T-TiSiCAs ₄	-1.73691
T-TaSiGeN ₄	-4.49585	T-TiCGeN ₄	-3.53526	T-TiSiCN ₄	-3.97939
T-TaSiGeP ₄	-1.69691	T-TiCGeP ₄	-1.67474	T-TiSiCP ₄	-1.84688
T-TaSiGeS ₄	-2.49377	T-TiCGeS ₄	-2.02092	T-TiSiCS ₄	-1.982
T-TaSiGeSe ₄	-1.76544	T-TiCGeSe ₄	-1.2406	T-TiSiCSe ₄	-1.22313

T-TaSiGeTe ₄	-0.93815	T-TiCGeTe ₄	-0.81788	T-TiSiCTe ₄	-0.80941
T-TiSiGeAs ₄	-1.75798	T-VCGeAs ₄	-1.82913	T-VSiCAs ₄	-1.87554
T-TiSiGeN ₄	-4.37416	T-VCGeN ₄	-3.64982	T-VSiCN ₄	-4.14359
T-TiSiGeP ₄	-1.51387	T-VCGeP ₄	-1.89329	T-VSiCP ₄	-2.02708
T-TiSiGeS ₄	-1.93326	T-VCGeS ₄	-2.0634	T-VSiCS ₄	-2.05173
T-TiSiGeSe ₄	-1.71227	T-VCGeSe ₄	-1.26178	T-VSiCSe ₄	-1.23422
T-TiSiGeTe ₄	-1.10734	T-VCGeTe ₄	-0.93025	T-VSiCTe ₄	-0.8792
T-VSiGeAs ₄	-1.8489	T-WCGeAs ₄	-1.8274	T-WSiCAs ₄	-1.88769
T-VSiGeN ₄	-4.42421	T-WCGeN ₄	-3.62841	T-WSiCN ₄	-4.10095
T-VSiGeP ₄	-1.74859	T-WCGeP ₄	-1.95672	T-WSiCP ₄	-2.07714
T-VSiGeS ₄	-2.40557	T-WCGeS ₄	-2.01637	T-WSiCS ₄	-0.16581
T-VSiGeSe ₄	-1.74368	T-WCGeSe ₄	-1.2414	T-WSiCSe ₄	-1.22912
T-VSiGeTe ₄	-1.21655	T-WCGeTe ₄	-0.96134	T-WSiCTe ₄	-0.80058
T-WSiGeAs ₄	-1.86184	T-NbCGeAs ₄	-1.53052	T-NbSiCAs ₄	-1.59116
T-WSiGeN ₄	-4.4146	T-NbCGeN ₄	-3.31368	T-NbSiCN ₄	-3.74878
T-WSiGeP ₄	-2.22493	T-NbCGeP ₄	-1.60749	T-NbSiCP ₄	-1.72652
T-WSiGeS ₄	-2.4189	T-NbCGeS ₄	-1.84878	T-NbSiCS ₄	-1.80371
T-WSiGeSe ₄	-1.64655	T-NbCGeSe ₄	-1.0368	T-NbSiCSe ₄	-1.00669
T-WSiGeTe ₄	-0.95374	T-NbCGeTe ₄	-0.64273	T-NbSiCTe ₄	-0.59199
T-ZrSiGeAs ₄	-1.83279	T-ZrCGeAs ₄	-1.70415	T-ZrSiCAs ₄	-1.76797
T-ZrSiGeN ₄	-4.37667	T-ZrCGeN ₄	-3.45851	T-ZrSiCN ₄	-3.82305
T-ZrSiGeP ₄	-2.11956	T-ZrCGeP ₄	-1.73073	T-ZrSiCP ₄	-1.84415
T-ZrSiGeS ₄	-2.45802	T-ZrCGeS ₄	-2.07956	T-ZrSiCS ₄	-2.04684
T-ZrSiGeSe ₄	-2.09302	T-ZrCGeSe ₄	-1.32428	T-ZrSiCSe ₄	-1.27479
T-ZrSiGeTe ₄	-1.09395	T-ZrCGeTe ₄	-0.84266	T-ZrSiCTe ₄	-0.79327

Table S5 The elastic constants of MA₂Z₄ structures (in Nm⁻¹)

Structure	C_{11}	C_{12}	C_{22}	C_{44}	$C_{11}C_{22}-C_{12}^2$
H-CrSi ₂ N ₄	517.55	156.89	156.89	180.33	56583.01
H-HfSi ₂ N ₄	466.43	153.54	153.54	156.44	48041.15
H-MoSi ₂ N ₄	548.07	158.42	158.42	194.82	61728.60
H-MoSi ₂ P ₄	219.20	56.79	56.79	81.21	9222.97
H-TaSi ₂ N ₄	523.57	163.91	163.91	179.83	58952.28
H-TiSi ₂ N ₄	495.98	156.72	156.72	169.63	53169.81
H-TiSi ₂ P ₄	189.62	46.40	46.40	71.61	6645.02
H-WSi ₂ N ₄	568.24	158.30	158.30	204.97	64893.70
H-WSi ₂ P ₄	223.95	54.53	54.53	84.71	9238.59
H-ZrSi ₂ N ₄	442.01	144.25	144.25	148.88	42952.16
H-HfGe ₂ N ₄	405.60	142.67	142.67	131.46	37511.60
H-MoGe ₂ N ₄	443.25	145.43	145.43	148.91	43311.54
H-WGe ₂ N ₄	460.18	144.96	144.96	157.61	45693.98
H-ZrGe ₂ N ₄	382.10	133.53	133.53	124.28	33192.34
T-HfSi ₂ N ₄	464.62	123.57	123.57	171.05	42143.94
T-ScSi ₂ N ₄	395.96	131.62	131.62	126.15	34793.40
T-ScSi ₂ P ₄	168.06	47.77	47.77	36.17	5746.08
T-TaSi ₂ N ₄	481.74	143.83	143.83	158.79	48601.61
T-ZrSi ₂ N ₄	442.34	117.44	117.44	163.29	38155.03
T-HfGe ₂ N ₄	413.47	124.29	124.29	145.82	35941.36

T-NbGe ₂ N ₄	397.98	126.40	126.40	133.07	34328.11
T-ScGe ₂ N ₄	334.35	123.01	123.01	102.81	25996.62
T-TaGe ₂ N ₄	404.93	127.26	127.26	134.66	35336.89
T-ZrGe ₂ N ₄	394.02	118.84	118.84	138.61	32702.38
H-HfSiGeN ₄	429.53	146.72	146.72	141.41	41494.03
H-MoSiGeN ₄	489.65	148.53	148.53	170.56	50665.94
H-MoSiGeP ₄	209.34	57.97	57.97	75.68	8775.22
H-NbSiGeP ₄	35.84	230.92	230.92	-97.54	-45048.92
H-TaSiGeN ₄	480.88	154.51	154.51	163.18	50427.10
H-TiSiGeN ₄	444.87	145.44	145.44	149.71	43549.51
H-WSiGeN ₄	512.16	150.39	150.39	180.88	54407.10
H-WSiGeP ₄	214.60	56.18	56.18	79.21	8900.31
H-ZrSiGeN ₄	407.09	138.69	138.69	134.20	37224.92
H-CrSiCAs ₄	192.83	61.73	61.73	65.55	8092.93
H-CrSiCN ₄	473.42	155.51	155.51	158.96	49438.51
H-CrSiCP ₄	235.59	59.62	59.62	87.99	10490.86
H-MoSiCAs ₄	196.71	50.58	50.58	73.06	7391.02
H-MoSiCP ₄	234.37	49.75	49.75	92.31	9185.21
H-NbSiCAs ₄	149.93	72.07	72.07	38.93	5611.62
H-NbSiCP ₄	206.44	72.98	72.98	66.73	9740.14
H-TaSiCAs ₄	123.55	80.20	80.20	21.68	3477.04
H-TaSiCP ₄	189.35	85.54	85.54	51.91	8880.02
H-TiSiCP ₄	89.07	-1.24	-1.24	45.15	-111.54
H-VSiCAs ₄	140.90	63.73	63.73	38.58	4917.91
H-VSiCN ₄	432.40	166.79	166.79	132.80	44300.91
H-VSiCP ₄	184.79	66.83	66.83	58.98	7883.03
H-WSiCAs ₄	199.42	45.30	45.30	77.06	6981.25
H-WSiCP ₄	235.01	46.33	46.33	94.34	8742.20
H-MoCGeAs ₄	170.58	55.07	55.07	57.76	6361.23
H-NbCGeP ₄	203.62	55.33	55.33	74.14	8205.10
H-TaCGeAs ₄	156.05	49.48	49.48	53.29	5273.52
H-WCGeAs ₄	171.23	52.11	52.11	59.56	6207.23
T-HfSiGeN ₄	428.46	117.91	117.91	154.74	36616.82
T-ScSiGeN ₄	352.19	117.86	117.86	116.57	27618.56
T-ScSiGeP ₄	149.64	54.51	54.51	25.18	5185.22
T-TaSiGeN ₄	437.27	126.54	126.54	154.67	39319.86
T-ZrSiGeN ₄	408.71	112.71	112.71	147.55	33361.87
T-HfSiCAs ₄	109.41	31.28	31.28	38.50	2443.92
T-HfSiCP ₄	104.38	34.99	34.99	-185.26	2427.81
T-ScSiCP ₄	132.56	36.63	36.63	54.54	3514.13
T-TiSiCAs ₄	71.27	88.40	88.40	-14.97	-1513.51
T-TiSiCP ₄	138.81	50.56	50.56	-30.98	4461.68
T-ZrSiCP ₄	111.52	67.29	67.29	-580.09	2975.96

Table S6 Effective mass (m^*), elastic modulus (C_{2D}), variable situation constant E_i and carrier mobility (μ_{2D}) in the xy direction for electrons and holes

Structure name		m^*_x/m_0	m^*_y/m_0	E_{ix} (eV)	E_{iy} (eV)	C_{2Dx} (eV)	C_{2Dy} (eV)	μ_x (cm ² /(Vs))	μ_y (cm ² /(Vs))
H-HfSi ₂ N ₄	electron	0.80	0.86	452.55	452.41	2.94	2.93	1.17E+03	1.01E+03
	hole	2.35	2.48	452.55	452.41	2.47	2.67	1.90E+02	1.47E+02
H-MoSi ₂ N ₄	electron	0.43	0.44	540.10	539.35	2.86	2.51	5.17E+03	6.42E+03
	hole	1.63	1.63	540.10	539.35	5.41	5.40	9.86E+01	9.92E+01

H-MoSi ₂ P ₄	electron	0.32	0.33	221.09	220.41	4.51	4.31	1.48E+03	1.53E+03
	hole	0.34	0.38	221.09	220.41	2.16	2.43	5.90E+03	3.75E+03
H-TaSi ₂ N ₄	electron	0.83	0.83	492.28	495.83	8.59	8.76	1.38E+02	1.33E+02
	hole	1.06	5.15	492.28	495.83	6.73	5.93	1.38E+02	7.56E+00
H-TiSi ₂ N ₄	electron	1.44	3.26	471.90	471.89	3	4.08	3.61E+02	3.80E+01
	hole	3.84	1.13	471.90	471.89	3.47	3.05	3.78E+01	5.66E+02
H-TiSi ₂ P ₄	electron	0.62	0.24	193.76	191.52	0.89	0.80	9.08E+03	7.27E+04
	hole	1.09	0.94	193.76	191.52	4.63	4.54	1.08E+02	1.51E+02
H-WSi ₂ N ₄	electron	0.34	0.34	565.23	564.82	3.72	3.91	4.98E+03	4.66E+03
	hole	1.53	1.52	565.23	564.82	5.64	5.05	1.08E+02	1.37E+02
H-WSi ₂ P ₄	electron	0.18	0.19	228.38	227.89	3.72	4.14	7.10E+03	5.42E+03
	hole	0.24	0.24	228.38	227.89	2.43	2.40	9.53E+03	9.61E+03
H-ZrSi ₂ N ₄	electron	2.30	1.37	431.38	430.36	2.26	2.59	2.27E+02	4.88E+02
	hole	3.61	2.26	431.38	430.36	3.95	3.97	3.02E+01	7.60E+01
T-HfSi ₂ N ₄	electron	0.52	0.24	492.89	491.44	5.1	5.79	1.00E+03	3.50E+03
	hole	-1.09	1.08	492.89	491.44	3.52	3.04	4.74E+02	6.43E+02
T-ZrSi ₂ N ₄	electron	0.54	0.25	471.67	470.46	3.95	4.77	1.46E+03	4.74E+03
	hole	-1.10	-1.4	471.67	470.46	3.51	3.23	4.48E+02	3.30E+02
H-HfGe ₂ N ₄	electron	0.72	2.2	383.63	381.39	2.17	2.00	2.26E+03	2.78E+02
	hole	1.86	1.8	383.63	381.39	3.09	3.13	1.66E+02	1.71E+02
H-MoGe ₂ N ₄	electron	0.38	0.39	434.55	433.35	2.02	2.81	1.03E+04	5.11E+03
	hole	1.10	1.1	434.55	433.35	3.5	3.43	4.21E+02	4.38E+02
H-WGe ₂ N ₄	electron	0.30	0.31	457.89	457.19	2.86	2.50	8.61E+03	1.09E+04
	hole	0.80	0.8	457.89	457.19	3.4	3.32	8.77E+02	9.22E+02
H-ZrGe ₂ N ₄	electron	1.50	1.7	364.79	362.43	3.35	3.50	2.04E+02	1.45E+02
	hole	1.77	1.52	364.79	362.43	2.78	2.81	2.15E+02	2.81E+02
T-HfGe ₂ N ₄	electron	0.21	0.21	416.89	415.66	8.47	8.62	1.86E+03	1.79E+03
	hole	1.29	0.97	416.89	415.66	2.28	2.05	6.84E+02	1.50E+03
T-ScGe ₂ N ₄	electron	0.45	-0.99	413.62	413.16	3.98	3.56	1.80E+03	4.79E+02
	hole	0.65	0.66	413.62	413.16	4.64	4.29	6.46E+02	7.42E+02
T-ZrGe ₂ N ₄	electron	0.31	0.65	401.27	400.01	3.84	3.72	4.08E+03	9.67E+02
	hole	-0.97	-1.03	401.27	400.01	4.54	4.54	2.94E+02	2.58E+02
H-HfSiGeN ₄	electron	0.78	0.86	414.51	414.32	3.08	2.98	1.04E+03	8.93E+02
	hole	2.91	2.97	414.51	414.32	3.23	3.49	6.66E+01	5.50E+01
H-MoSiGeN ₄	electron	0.40	0.41	484.97	484.22	1.94	1.63	1.16E+04	1.56E+04
	hole	-6.20	-6.2	484.97	484.22	4.79	4.74	7.83E+00	7.96E+00
H-MoSiGeP ₄	electron	0.33	0.33	209.52	209.20	4.04	4.06	1.73E+03	1.62E+03
	hole	0.34	0.37	209.52	209.20	2.31	2.56	4.99E+03	3.25E+03
H-TaSiGeN ₄	electron	1.57	1.8	468.55	476.69	3.27	2.51	2.52E+02	3.30E+02
	hole	1.52	1.27	468.55	476.69	4.27	3.79	1.58E+02	2.93E+02
H-TiSiGeN ₄	electron	2.11	3	427.59	426.66	4.11	3.34	8.08E+01	6.04E+01
	hole	2.44	1.33	427.59	426.66	4.32	4.75	5.50E+01	1.51E+02
H-WSiGeN ₄	electron	0.32	0.32	511.54	509.90	2.89	2.55	8.44E+03	1.09E+04
	hole	16.50	16.84	511.54	509.90	4.81	4.70	1.15E+00	1.16E+00
H-WSiGeP ₄	electron	0.21	0.2	216.98	215.76	3.98	3.64	4.34E+03	5.79E+03
	hole	0.24	0.24	216.98	215.76	2.37	2.78	9.30E+03	6.69E+03
H-ZrSiGeN ₄	electron	1.64	1.92	394.27	393.35	3.77	3.97	1.47E+02	9.60E+01
	hole	2.19	2.33	394.27	393.35	3.17	3.37	1.16E+02	9.10E+01
T-HfSiGeN ₄	electron	0.56	0.27	449.62	449.21	2.32	5.72	3.75E+03	2.70E+03
	hole	1.08	1.11	449.62	449.21	8.61	8.75	7.41E+01	6.82E+01
T-ZrSiGeN ₄	electron	0.22	0.61	431.75	431.04	3.48	2.68	1.01E+04	2.31E+03
	hole	1.01	1.28	431.75	431.04	5.34	5.48	2.11E+02	1.25E+02
H-CrSiCN ₄	electron	0.95	1.03	490.90	478.38	6.93	6.62	1.62E+02	1.48E+02
	hole	0.95	1.05	490.90	478.38	3.45	3.68	6.56E+02	4.55E+02
H-CrSiCP ₄	electron	0.25	0.76	224.25	228.76	1.25	2.12	3.33E+04	1.27E+03
	hole	0.51	0.6	224.25	228.76	2.05	2.53	2.98E+03	1.40E+03
H-VSiCN ₄	electron	0.72	0.82	372.21	371.14	3	3.13	1.13E+03	8.01E+02
	hole	5.55	0.99	372.21	371.14	2.9	2.47	2.04E+01	8.83E+02

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