

**Supporting Information**  
**Prospect of high-temperature superconductivity in layered metal borocarbides**

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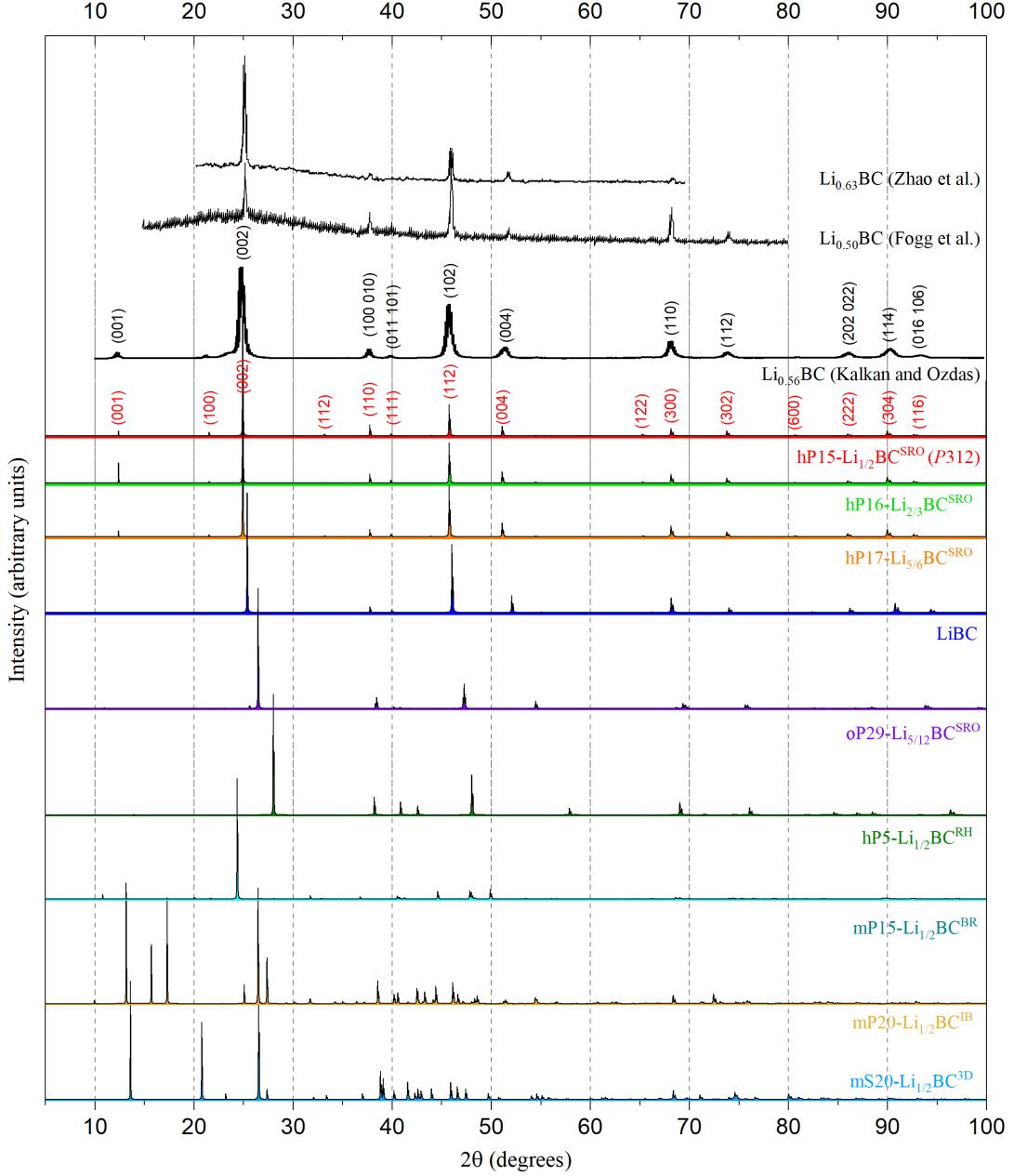


FIG. S1. Comparison of powder x-ray diffraction patterns obtained for synthesized  $\text{Li}_x\text{BC}$  samples (the top three data sets adopted from Refs. [1–3]) and simulated with  $\lambda_{\text{Cu K}-\alpha} = 1.54059 \text{ \AA}$  for  $\text{Li}_x\text{BC}$  models considered in this study (the bottom nine data sets).

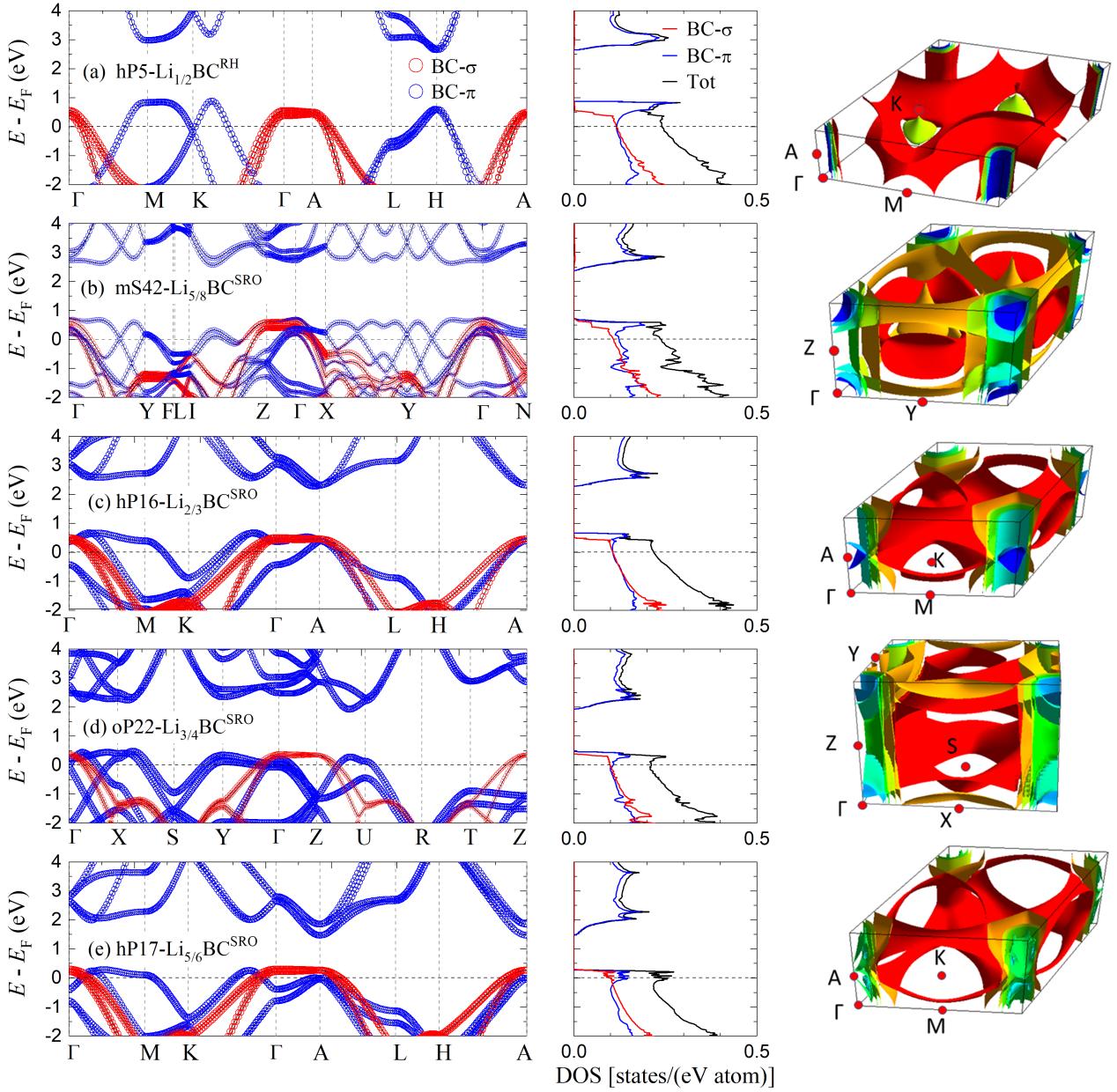


FIG. S2. Electronic properties of the five short-range ordering (SRO) or stage-2 configurations identified across the  $\text{Li}_x\text{BC}$  ( $5/6 \geq x \geq 1/2$ ) compositions: (a)  $\text{hP5-Li}_{1/2}\text{BC}^{\text{RH}}$ , (b)  $\text{mS42-Li}_{5/8}\text{BC}^{\text{SRO}}$ , (c)  $\text{hP16-Li}_{2/3}\text{BC}^{\text{SRO}}$ , (d)  $\text{oP22-Li}_{3/4}\text{BC}^{\text{SRO}}$ , and (e)  $\text{hP17-Li}_{5/6}\text{BC}^{\text{SRO}}$ . Each row contains the electronic band structure with orbital characters (left panel), the total and projected DOS (middle panel), and the Fermi surfaces (right panel).

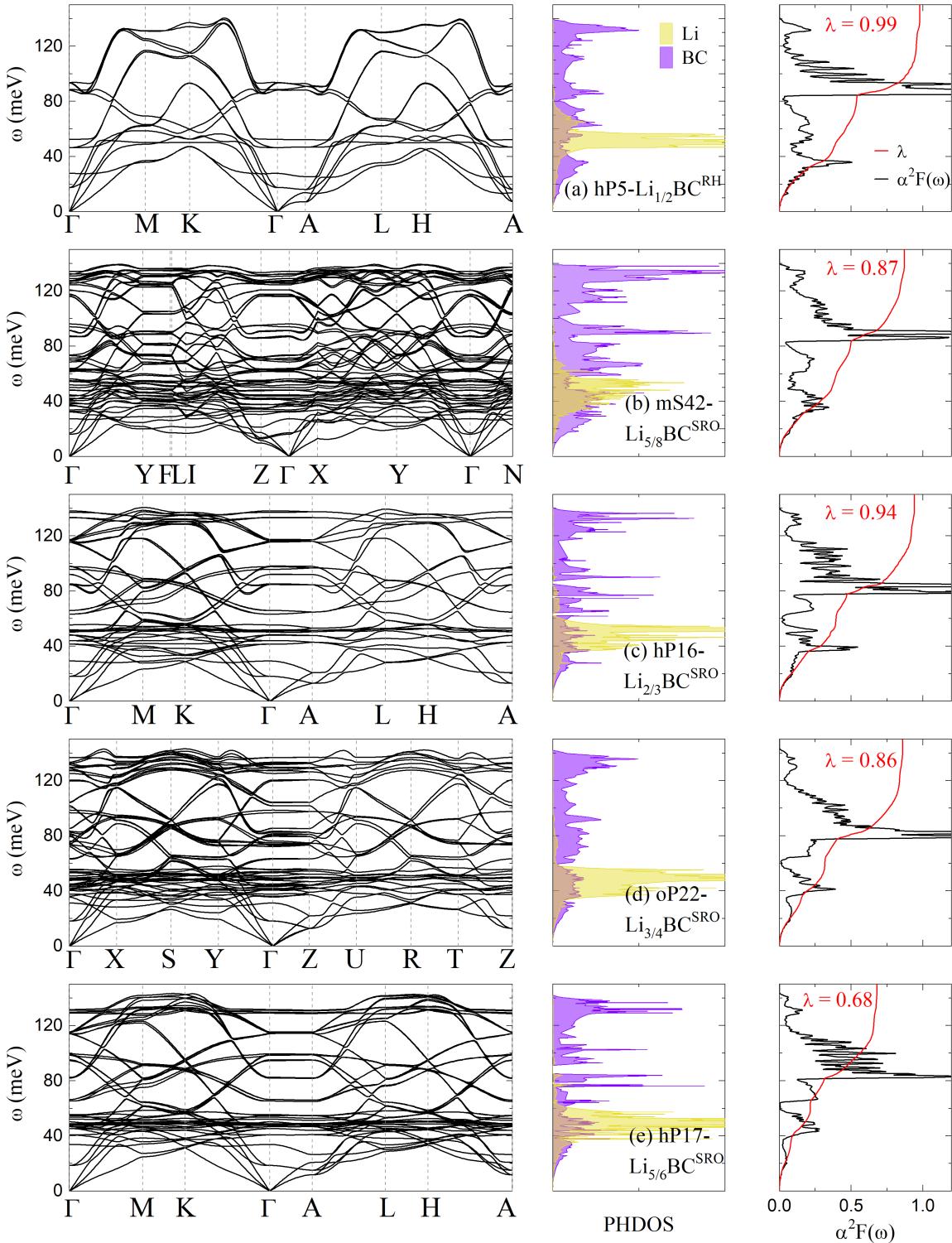


FIG. S3. Vibrational and e-ph coupling properties of the five short-range ordering (SRO) or stage-2 configurations identified across the  $\text{Li}_x\text{BC}$  ( $5/6 \geq x \geq 1/2$ ) compositions: (a) **hP5**- $\text{Li}_{1/2}\text{BC}^{\text{RH}}$ , (b) **mS42**- $\text{Li}_{5/8}\text{BC}^{\text{SRO}}$ , (c) **hP16**- $\text{Li}_{2/3}\text{BC}^{\text{SRO}}$ , (d) **oP22**- $\text{Li}_{3/4}\text{BC}^{\text{SRO}}$ , and (e) **hP17**- $\text{Li}_{5/6}\text{BC}^{\text{SRO}}$ . Each row contains the phononic dispersion (left panel), the phononic DOS decomposed into Li and BC contributions (middle panel), and the Eliashberg spectral function  $\alpha^2 F(\omega)$  with integrated e-ph coupling strength  $\lambda$  (right panel).

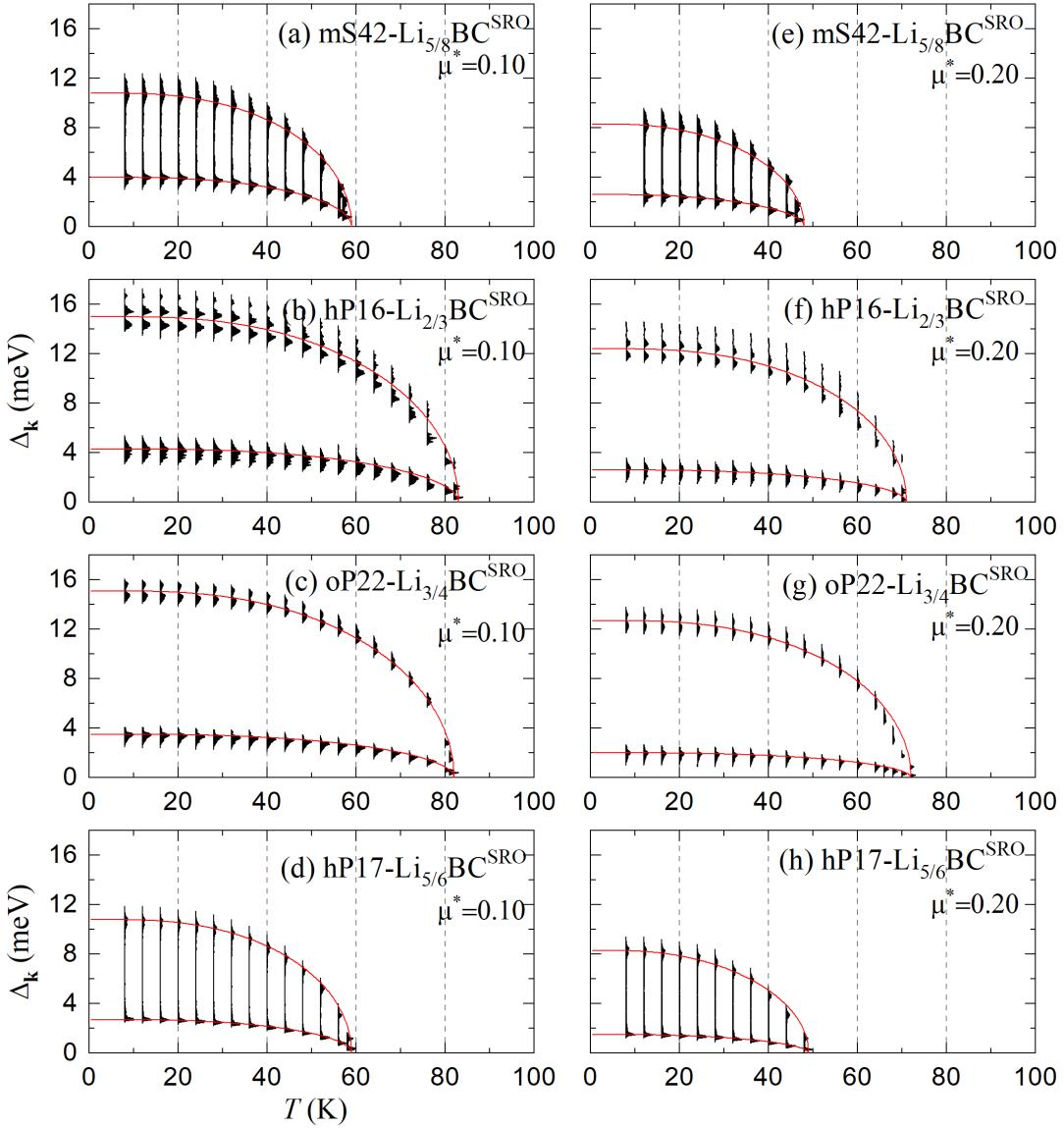


FIG. S4. Energy distribution of the superconducting gaps  $\Delta_k$  as a function of temperature with  $\mu^* = 0.10$  and  $\mu^* = 0.20$  for four short-range ordering (SRO) configurations identified across the  $\text{Li}_x\text{BC}$  ( $5/6 \geq x \geq 5/8$ ) compositions: (a,e) mS42-Li<sub>5/8</sub>BC<sup>SRO</sup>, (b,f) hP16-Li<sub>2/3</sub>BC<sup>SRO</sup>, (c,g) oP22-Li<sub>3/4</sub>BC<sup>SRO</sup>, and (d,h) hP17-Li<sub>5/6</sub>BC<sup>SRO</sup>. The red curves are a guide for the eye.

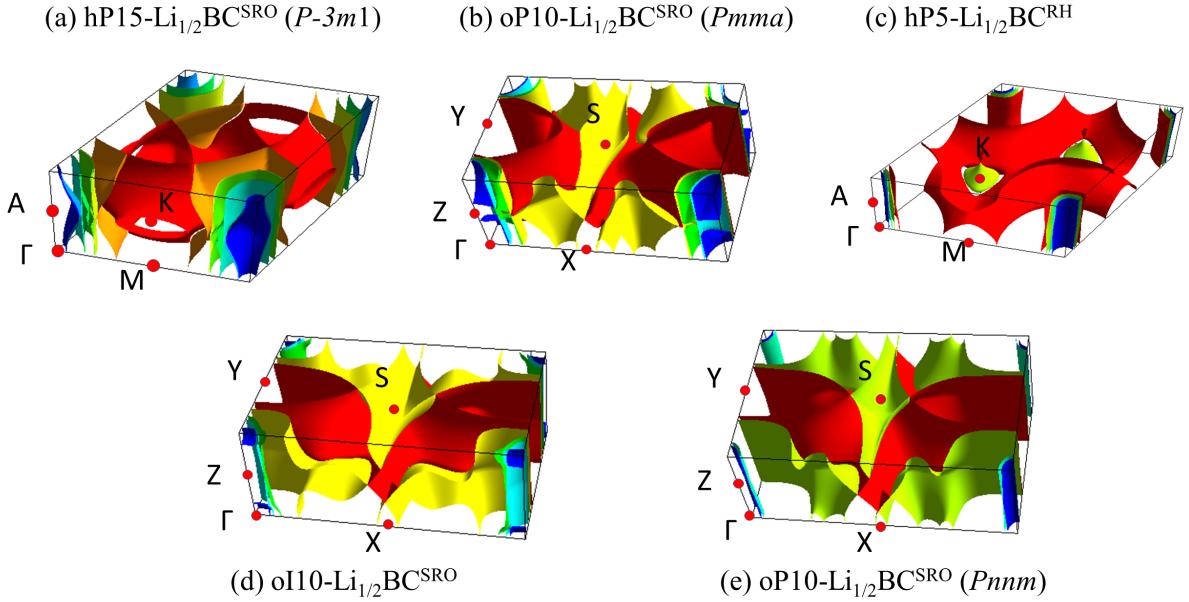


FIG. S5. Fermi surfaces for  $\text{Li}_{1/2}\text{BC}$  layered configurations (a)  $\text{hP15}^{\text{SRO}}$  ( $P\bar{3}m1$ ), (b)  $\text{oP10}^{\text{SRO}}$  ( $Pmma$ ), (c)  $\text{hP5}^{\text{RH}}$ , (d)  $\text{oI10}^{\text{SRO}}$ , and (e)  $\text{oP10}^{\text{SRO}}$  ( $Pnnm$ ), with the degree of BC layer distortion increasing from (a) to (e).

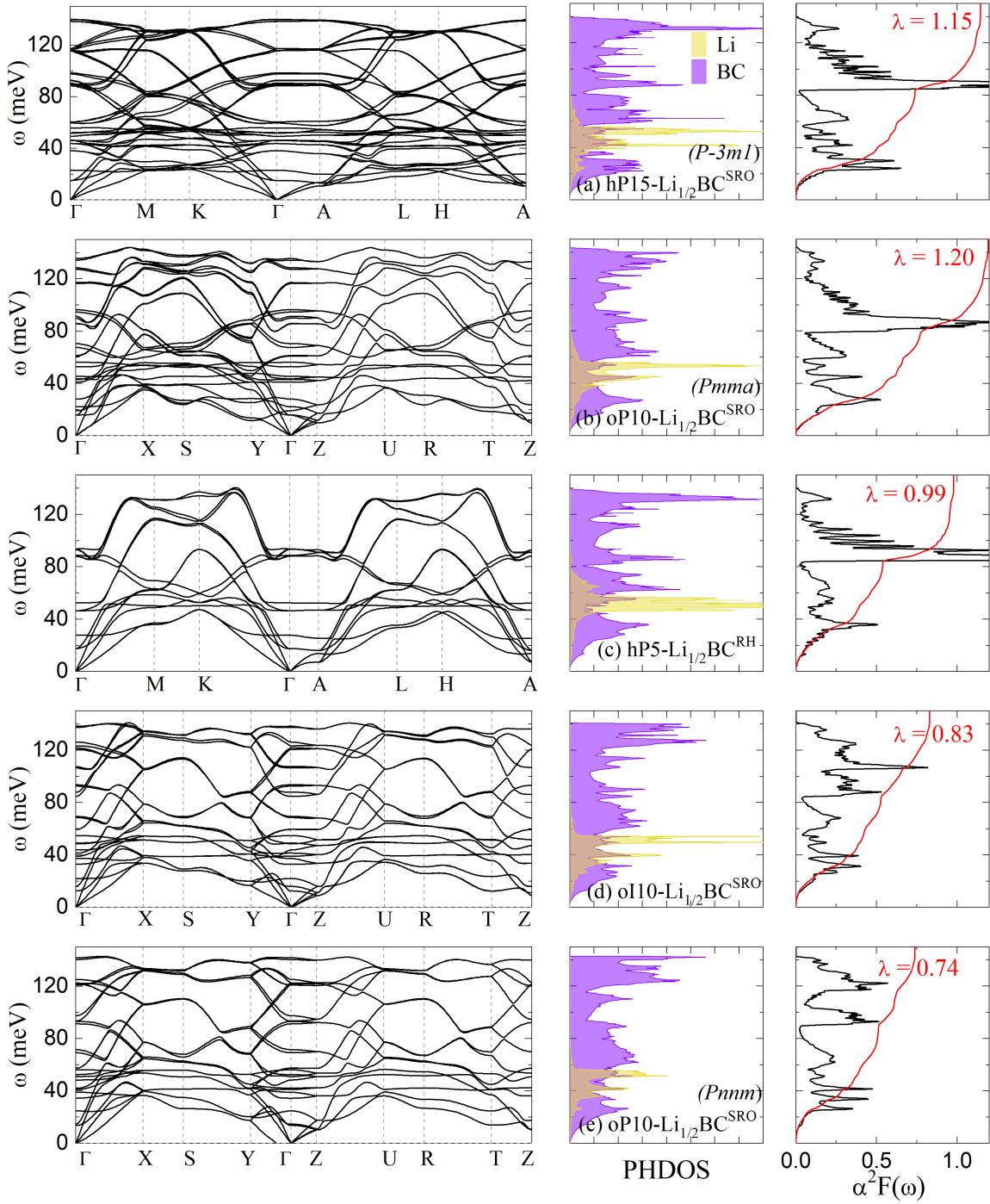


FIG. S6. Vibrational and e-ph coupling properties in  $\text{Li}_{1/2}\text{BC}$  layered configurations (a)  $\text{hP15}^{\text{SRO}}$  ( $P\bar{3}m1$ ), (b)  $\text{oP10}^{\text{SRO}}$  ( $Pmma$ ), (c)  $\text{hP5}^{\text{RH}}$ , (d)  $\text{oI10}^{\text{SRO}}$ , and (e)  $\text{oP10}^{\text{SRO}}$  ( $Pnnm$ ), with the degree of BC layer distortion increasing from (a) to (e). Each row contains the phononic dispersion (left panel), the phononic DOS decomposed into Li and BC contributions (middle panel), and the Eliashberg spectral function  $\alpha^2 F(\omega)$  with integrated e-ph coupling strength  $\lambda$  (right panel).

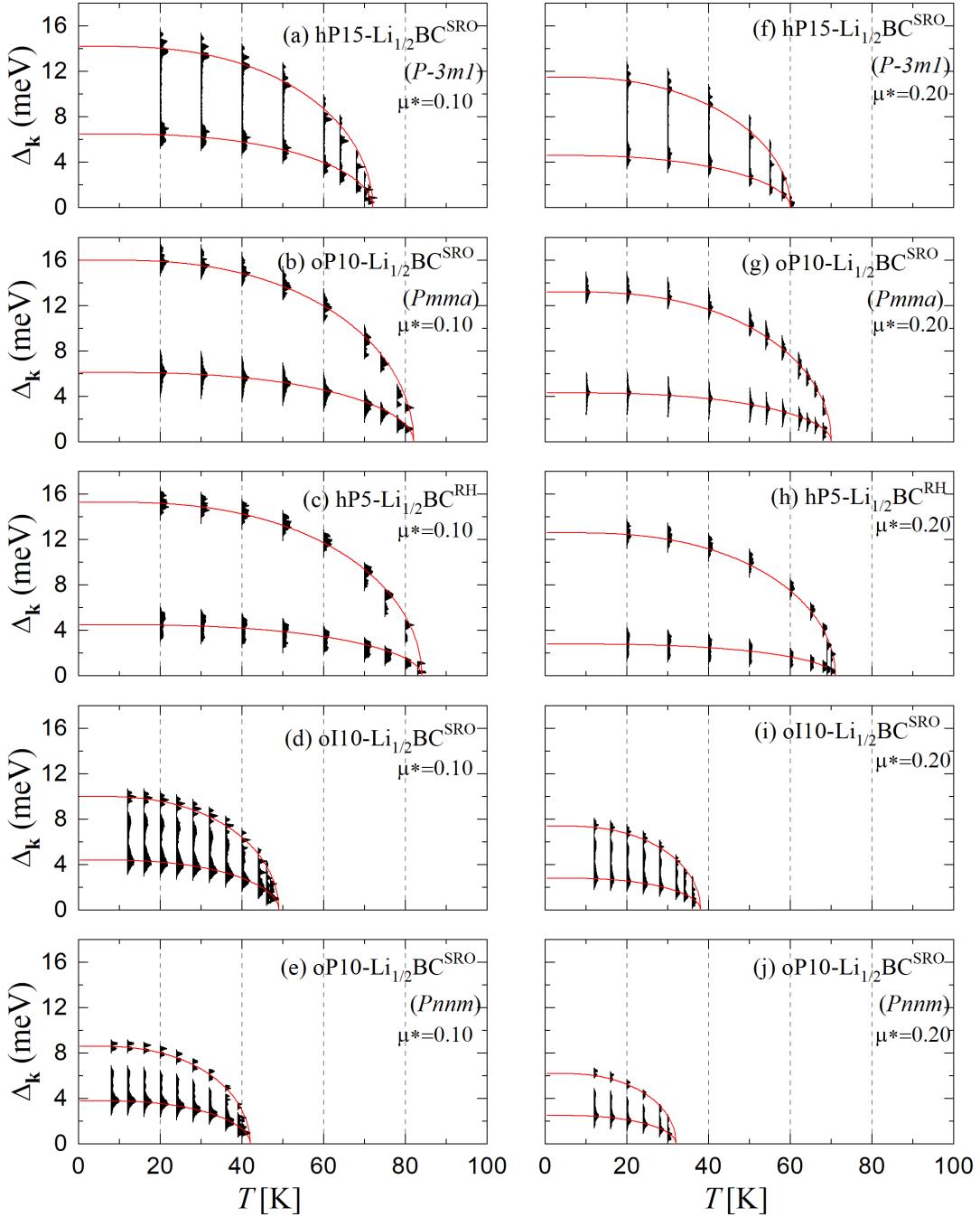


FIG. S7. Energy distribution of the superconducting gaps  $\Delta_k$  as a function of temperature with  $\mu^* = 0.10$  (left panels) and  $\mu^* = 0.20$  (right panels) for  $\text{Li}_{1/2}\text{BC}$  layered configurations (a, f)  $\text{hP15}^{\text{SRO}}$  ( $P\bar{3}m1$ ), (b, g)  $\text{oP10}^{\text{SRO}}$  ( $Pmma$ ), (c, h)  $\text{hP5}^{\text{RH}}$ , (d, i)  $\text{oI10}^{\text{SRO}}$ , and (e, j)  $\text{oP10}^{\text{SRO}}$  ( $Pnnm$ ), arranged in increasing order of BC layer distortion. The red curves are a guide for the eye.

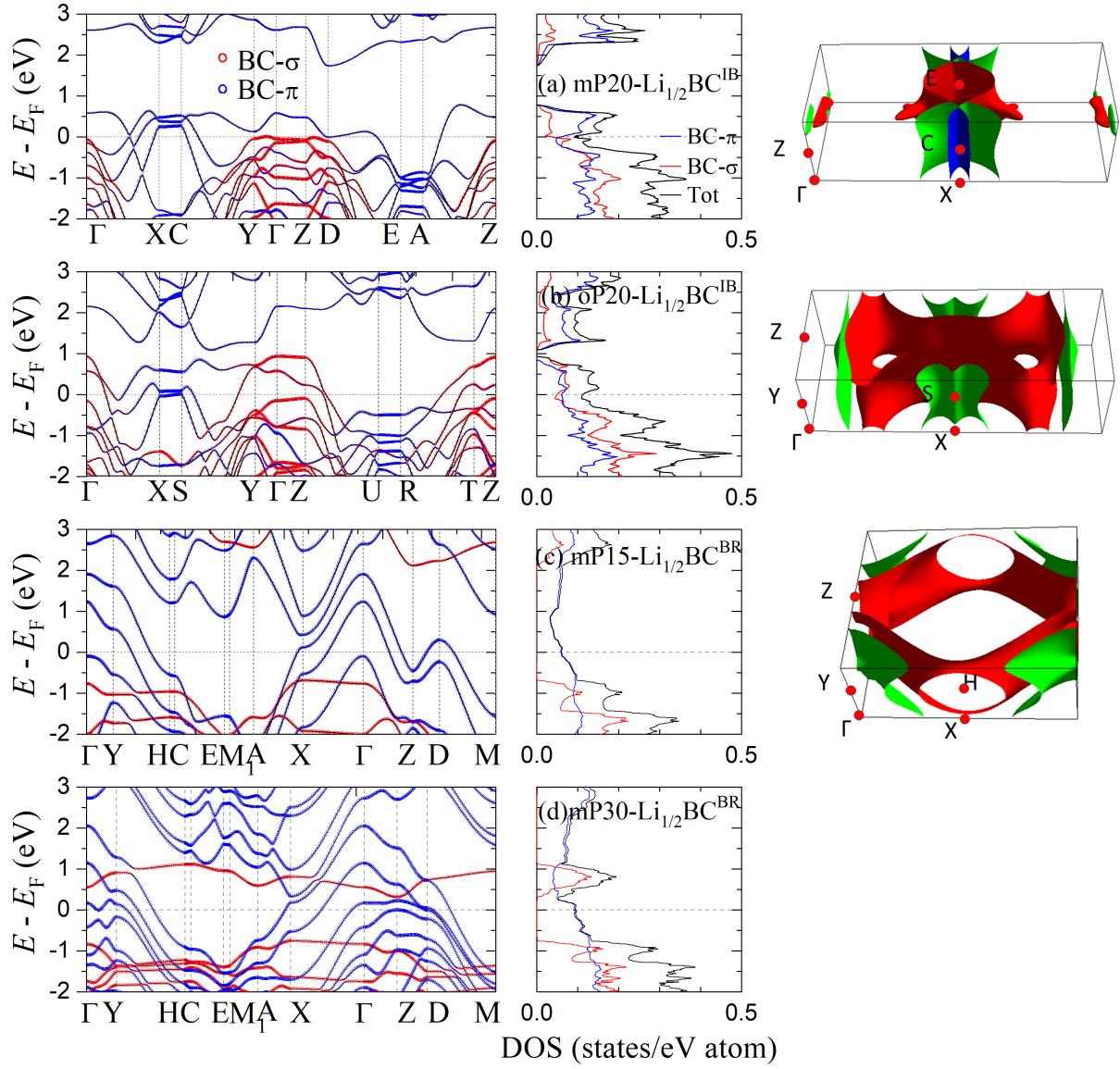


FIG. S8. Electronic properties for  $\text{Li}_{1/2}\text{BC}$  layered configurations with interlayer bridging (IB) and bond rotation (BR) defects: (a)  $\text{mP20}-\text{Li}_{1/2}\text{BC}^{\text{IB}}$ , (b)  $\text{oP20}-\text{Li}_{1/2}\text{BC}^{\text{IB}}$ , (c)  $\text{mP15}-\text{Li}_{1/2}\text{BC}^{\text{BR}}$ , and (d)  $\text{mP30}-\text{Li}_{1/2}\text{BC}^{\text{BR}}$ . Each row contains the electronic band structure with orbital characters (left panel), the total and projected DOS (middle panel), and the Fermi surfaces (right panel).

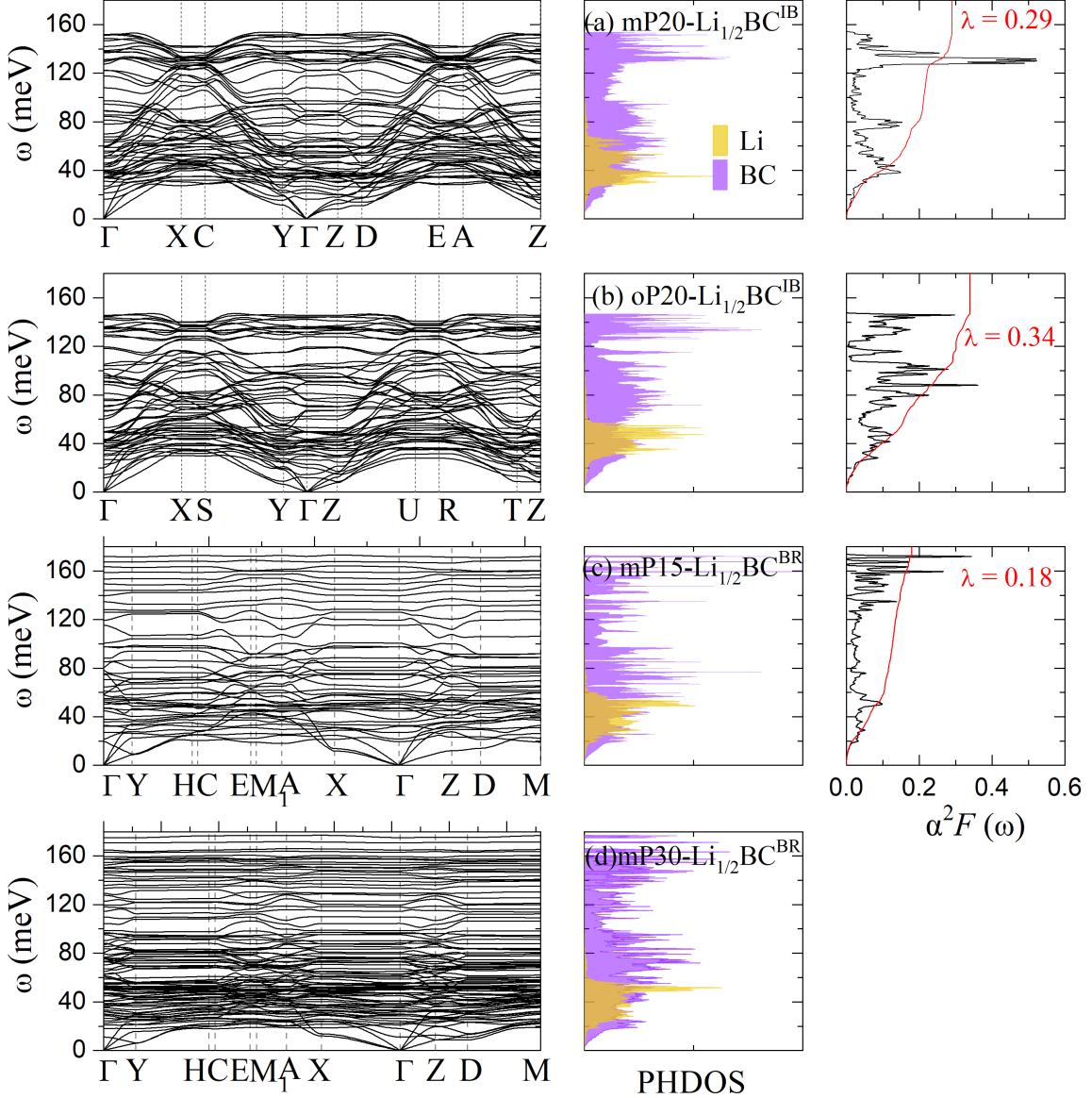


FIG. S9. Vibrational and e-ph coupling properties in  $\text{Li}_{1/2}\text{BC}$  layered configurations with interlayer bridging (IB) and bond rotation (BR) defects: (a)  $\text{mP20-}\text{Li}_{1/2}\text{BC}^{\text{IB}}$ , (b)  $\text{oP20-}\text{Li}_{1/2}\text{BC}^{\text{IB}}$ , (c)  $\text{mP15-}\text{Li}_{1/2}\text{BC}^{\text{BR}}$ , and (d)  $\text{mP30-}\text{Li}_{1/2}\text{BC}^{\text{BR}}$ . Each row contains the phononic dispersion (left panel), the phononic DOS decomposed into Li and BC contributions (middle panel), and the Eliashberg spectral function  $\alpha^2 F(\omega)$  with integrated e-ph coupling strength  $\lambda$  (right panel).

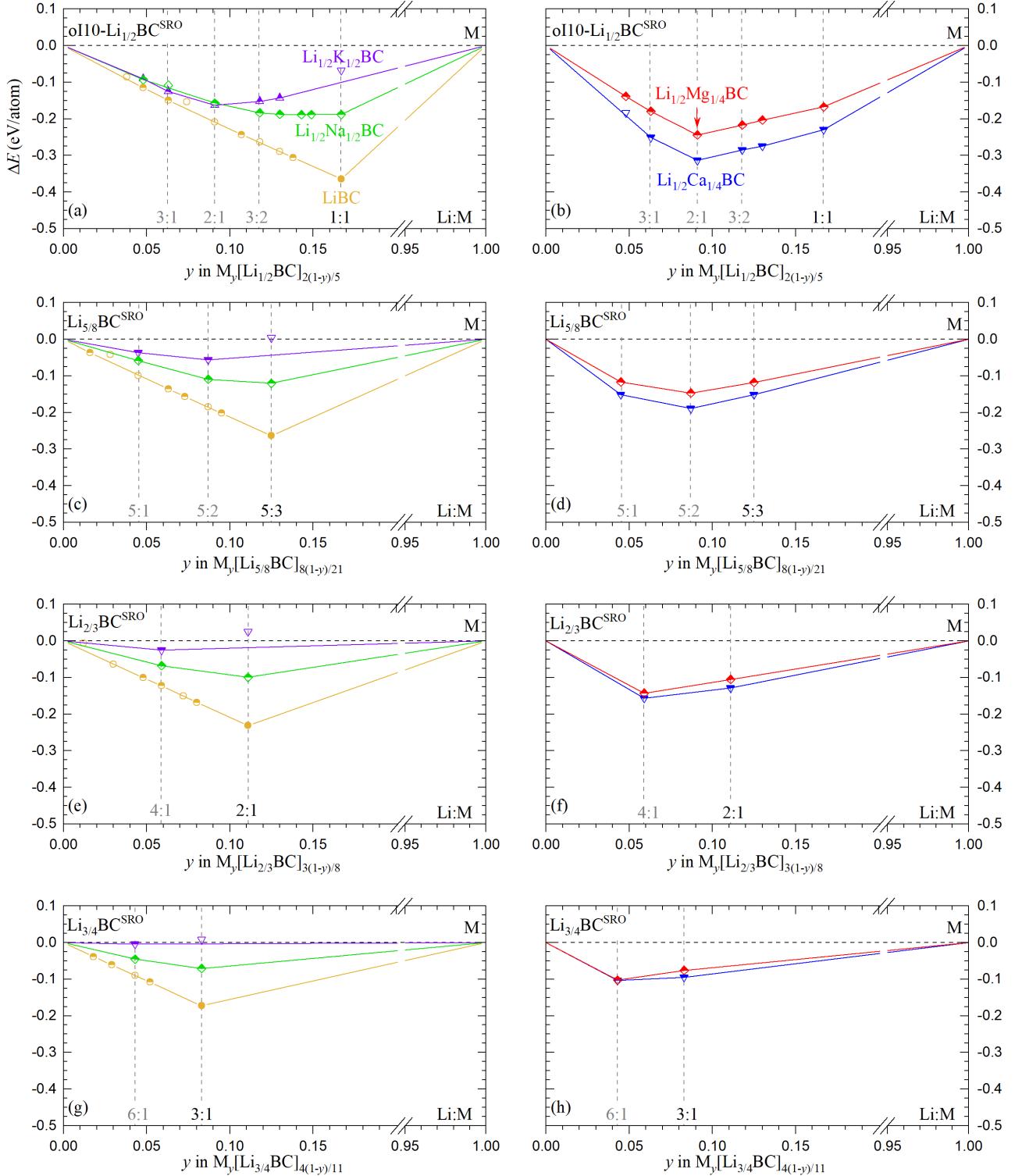


FIG. S10. Relative energies of  $\text{Li}_x\text{M}_{[(x+2)y/(1-y)]}\text{BC}$  phases referenced to the lowest energy honeycomb layered phases  $\text{Li}_x\text{BC}$  ( $3/4 \geq x \geq 1/2$ ) and pure M. The stable LiBC is marked with a solid circle. Metastable phases defining the local convex hull in the kinetically-protected subspace of layered borocarbides are shown as half-filled points connected with solid lines. The results indicate that it is thermodynamically favorable for the Na, K, Mg, and Ca metals to intercalate into the starting  $\text{Li}_x\text{BC}$  material for all considered *fixed* values of  $x$ . Information on the *global* stability of the  $\text{Li}_x\text{M}_y\text{BC}$  phases can be found in Figs. 8 and S12.

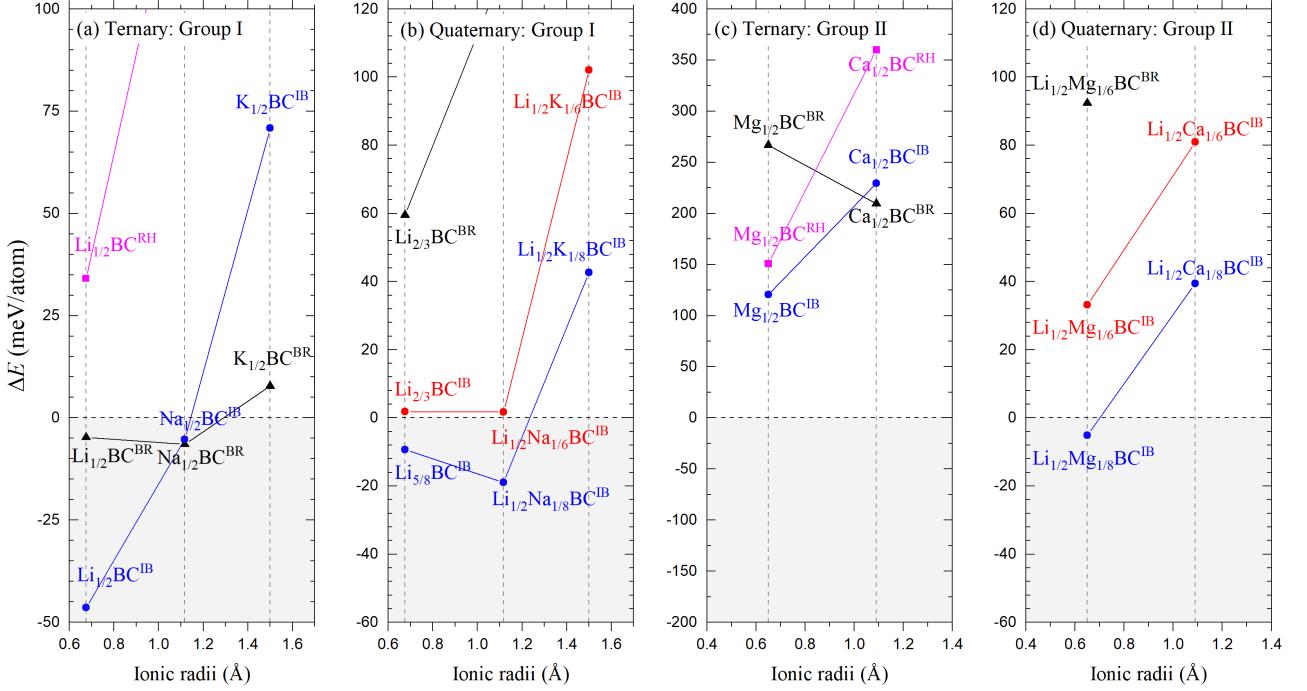


FIG. S11. Relative energies of (a,c)  $M_{1/2}\text{BC}$  ternaries and (b,d) a selection of  $\text{Li}_{1/2}\text{M}_y\text{BC}$  quaternaries with structural transformations referenced to their lowest energy ordered phase with a hexagonal BC network at that composition, plotted versus the ionic radius of the M intercalant [4]. The “BR” transformation refers to in-plane bond rotations resulting in a swap of B and C atoms. The “IB” transformation refers to interlayer bridging leading to the formation of C-C interlayer bonds. The “RH” refers to Rüdorff-Hofmann stage-2 configuration.

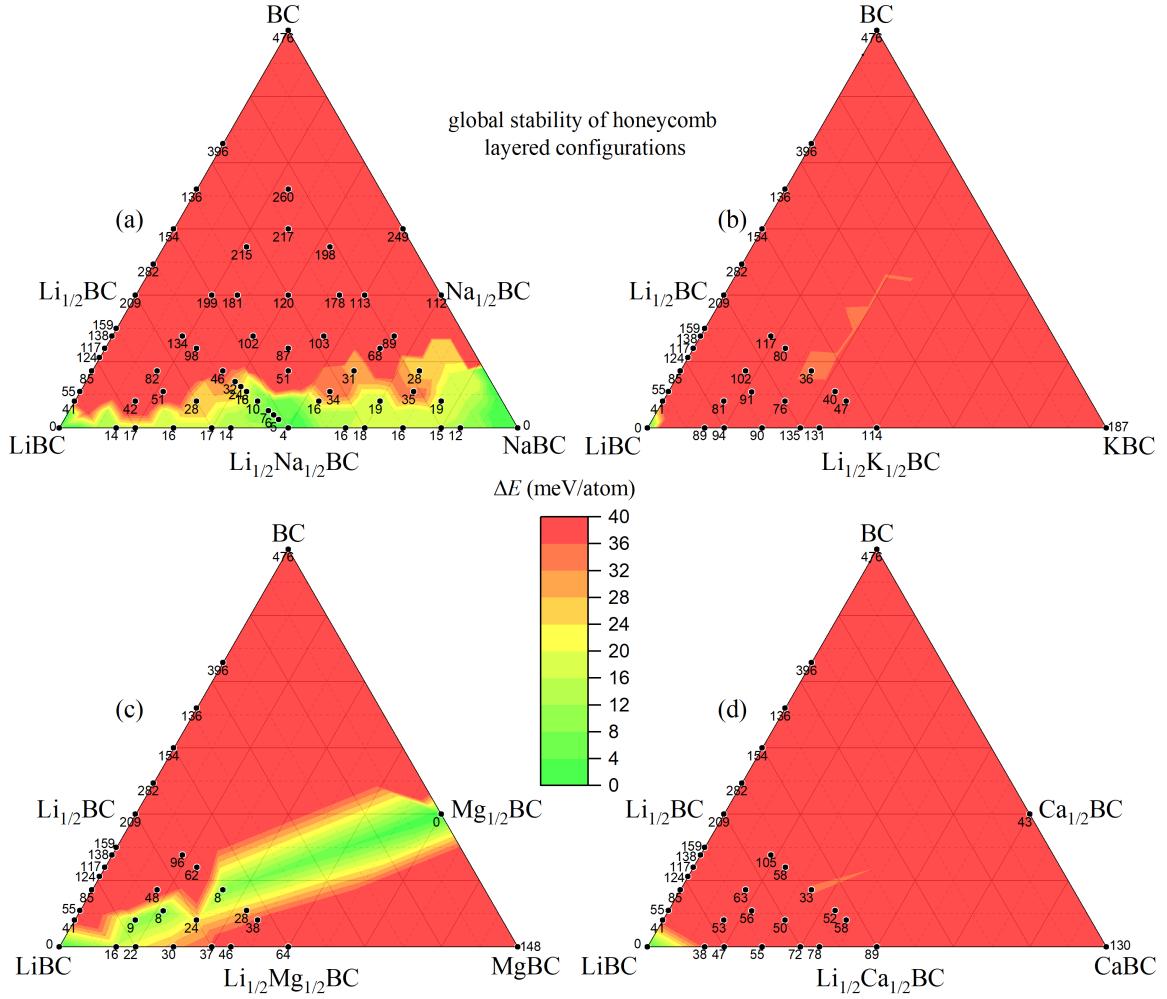


FIG. S12. Distance to the global convex hull for  $\text{Li}_x\text{M}_y\text{BC}$  phases with honeycomb morphology at  $T = 0$  K. For the elemental metals, we considered cI2, cF4 and hP2 configurations and used the most stable representation with the **optB86b** functional. The convex hull for each quaternary was constructed using the full set of synthesized materials reported in the literature or proposed compounds discussed in our study: cF4-Li, hR36-B, hP4-C, cF4-Na, hP2-Mg, cF4-K, cF4-Ca, tP16-LiB<sub>3</sub>, hP15-Li<sub>8</sub>B<sub>7</sub>, tP136-Li<sub>24</sub>B<sub>112</sub>, hP34-Li<sub>18</sub>B<sub>16</sub>, hP13-LiC<sub>12</sub>, hP7-LiC<sub>6</sub>, mS14-Li<sub>8</sub>C<sub>6</sub>, mS30-B<sub>4</sub>C, oF46-Na<sub>6</sub>B<sub>40</sub>, oI64-Na<sub>4</sub>B<sub>60</sub>, hP6-NaBC, aP189-NaB<sub>5</sub>C, oP14-NaB<sub>5</sub>C, hP6-LiBC, oI64-LiB<sub>13</sub>C<sub>2</sub>, oF32-LiB<sub>6</sub>C, oS80-MgB<sub>2</sub>C<sub>2</sub>, oI60-MgB<sub>12</sub>C<sub>2</sub>, tP54-Mg<sub>2</sub>B<sub>24</sub>C, hP3-MgB<sub>2</sub>, oP20-MgB<sub>4</sub>, cP7-KB<sub>6</sub>, oF72-KC<sub>8</sub>, tI20-CaB<sub>2</sub>C<sub>2</sub>, mS12-CaC<sub>2</sub>, hR21-CaC<sub>6</sub>, tP20-CaB<sub>4</sub>, and cP7-CaB<sub>6</sub>. The phases are described in Refs. [5–9] and specified in the provided CIF files.

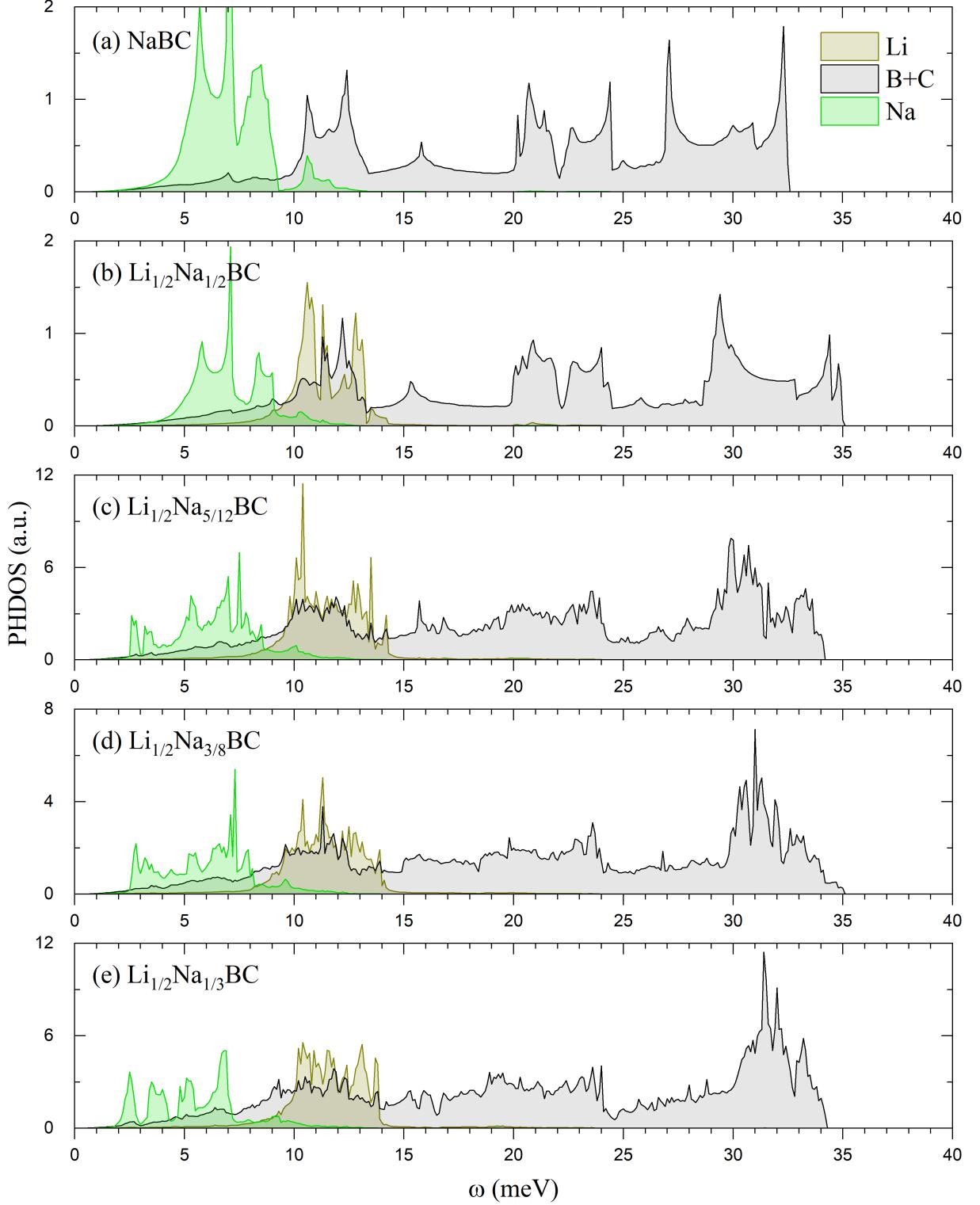


FIG. S13. Projected phononic DOS for NaBC and  $\text{Li}_{1/2}\text{Na}_y\text{BC}$  calculated with the finite displacement method using PHONOPY and VASP. Details on the hP6- $\text{Li}_{1/2}\text{Na}_{1/2}\text{BC}$ , mP35- $\text{Li}_{1/2}\text{Na}_{5/12}\text{BC}$ , mP23- $\text{Li}_{1/2}\text{Na}_{3/8}\text{BC}$ , and mP34- $\text{Li}_{1/2}\text{Na}_{1/3}\text{BC}$  phases can be found in main text Table 1. The removal of Na in the double-metal borocarbides, from  $y = 1/2$  in (b) to  $y = 1/3$  in (e), results in the softening of the Na modes.

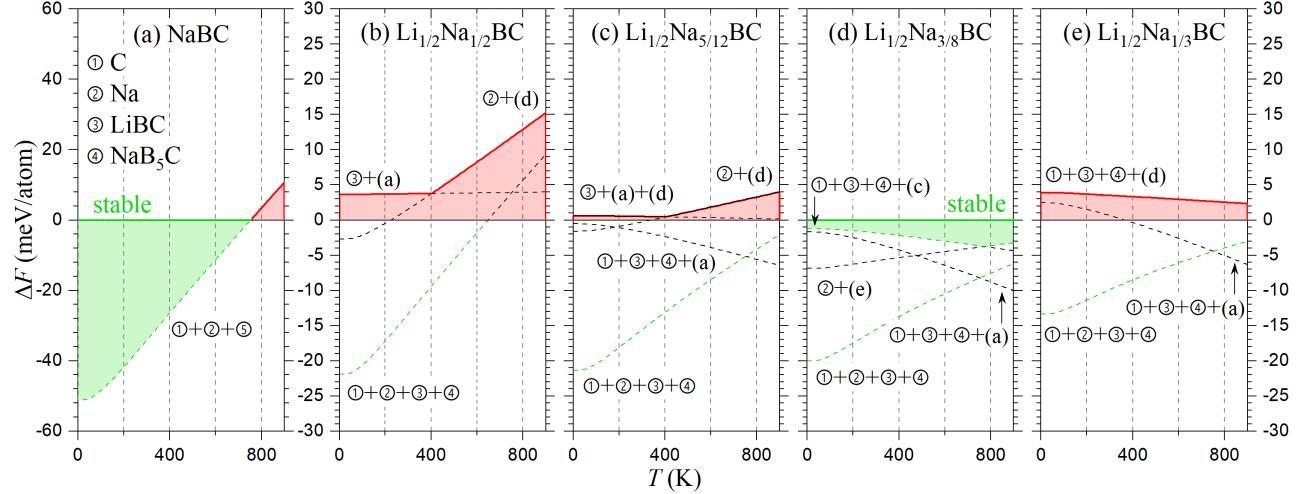


FIG. S14. Distance to the convex hull as a function of temperature for proposed Na and Li-Na borocarbides calculated with the optB88 functional [10]. Different lines correspond to the lowest-free energy combinations among all observed ground states (circled numbers) and proposed phases (bracketed letters). NaBC and  $\text{Li}_{1/2}\text{Na}_y\text{BC}$  ( $y = 1/2, 5/12$ , and  $3/8$ ) appear thermodynamically stable at low temperatures with respect to any mixture of the synthesized Li-Na-B-C phases listed in Fig. S12. The displayed set of phases equals that in Figs. 8 and S13.

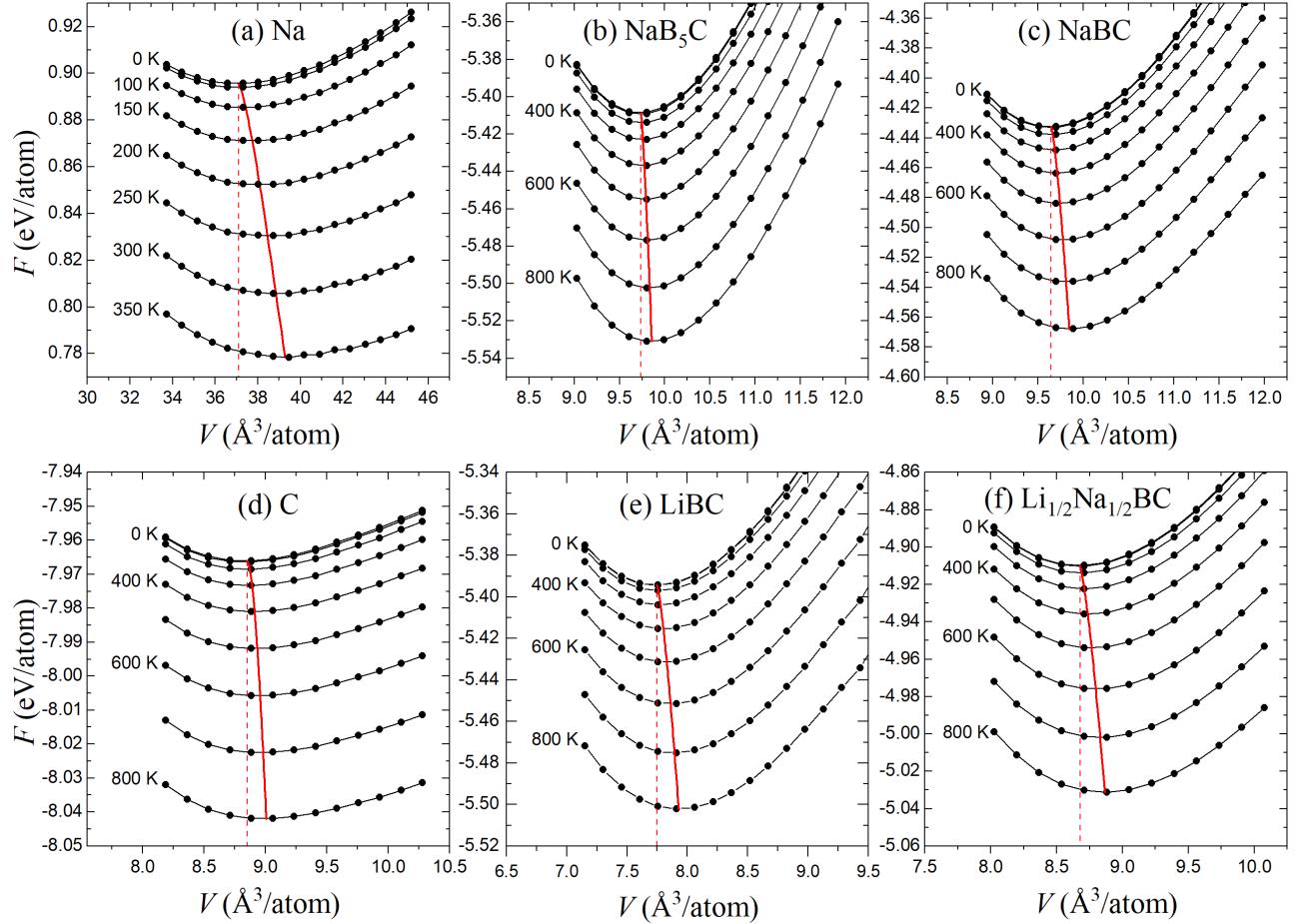


FIG. S15. Quasi-harmonic approximation (QHA) results for fcc-Na, oP14-NaB<sub>5</sub>C, hP6-NaBC, hP4-C, hP6-LiBC and hP6-Li<sub>½</sub>Na<sub>½</sub>BC. In these simulations, we (i) generated a uniform grid of volumes around equilibrium by rescaling the lattice constants; (ii) optimized the unit cell shape and atomic positions at each fixed volume with VASP; (iii) used Phonopy and VASP to perform phonon calculations in the harmonic approximation at each volume; (iv) fitted the resulting free energy points at each temperature with a third-order polynomial; and (v) showed the free energy values for every (a) 50 K or (b-f) 100 K (black circles), the polynomial fits (black solid lines), the minimum free energy values at the corresponding volumes for every 10 K (red solid line), and the starting volume (red dashed line). At 800 K, the free energy difference between the standard harmonic formalism and the QHA values was found to be (b) -2.6 (c) -4.2 (d) -1.0 (e) -4.5 and (f) -4.4 meV/atom. At 350 K, the free energy difference for fcc-Na is -6.1 meV/atom.

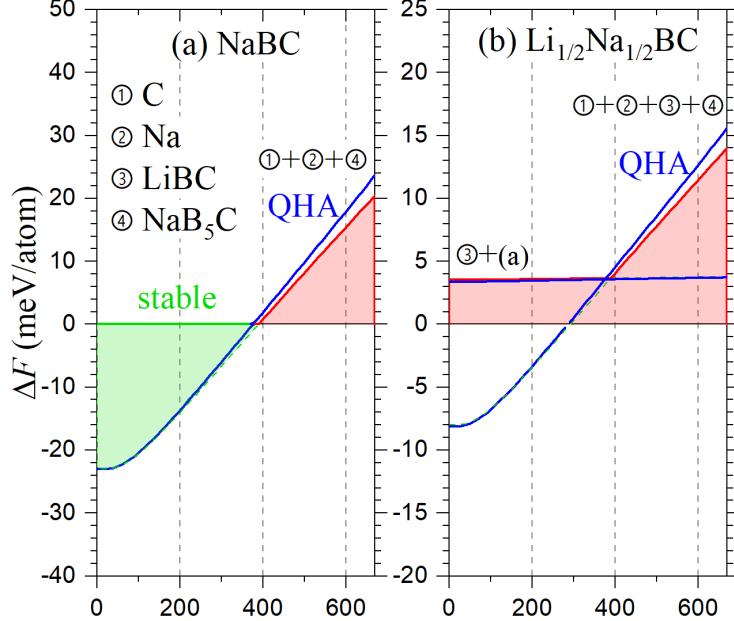


FIG. S16. Effect of the quasi-harmonic approximation (QHA) on the distance to the convex hull as a function of temperature for proposed NaBC and Li<sub>1/2</sub>Na<sub>1/2</sub>BC calculated with the optB86b functional [11]. The distance to the convex hull using the QHA is shown as blue lines.

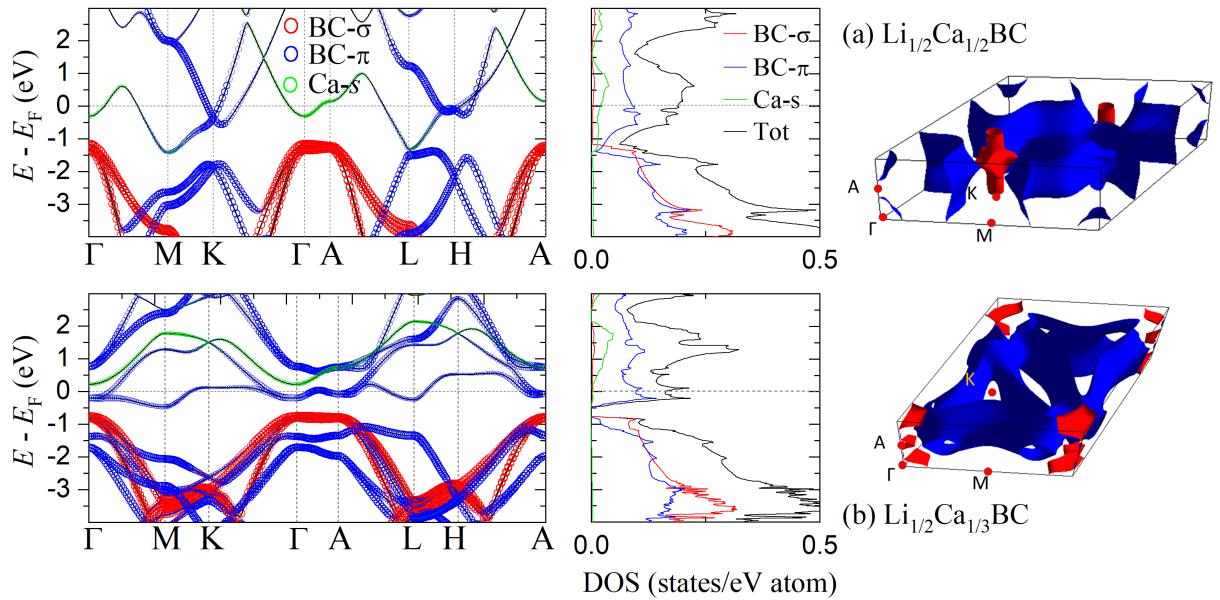


FIG. S17. Electronic properties for (a) Li<sub>1/2</sub>Ca<sub>1/2</sub>BC and (b) Li<sub>1/2</sub>Ca<sub>1/3</sub>BC. Each row contains the electronic band structure with orbital characters (left panel), the total and projected DOS (middle panel), and the Fermi surfaces (right panel).

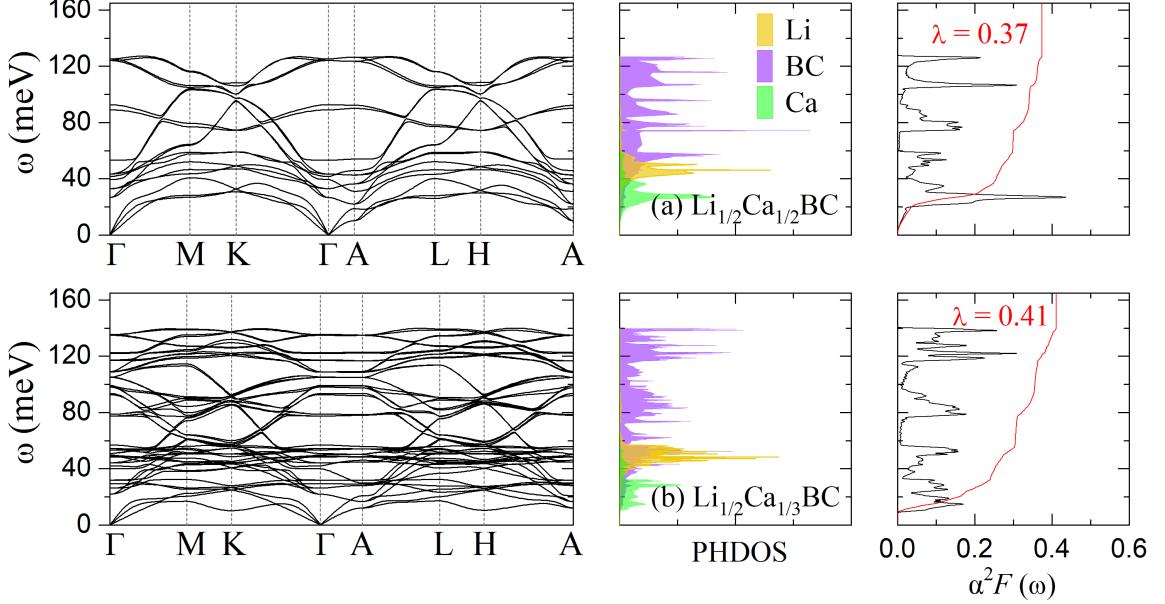


FIG. S18. Vibrational and e-ph coupling properties in (a)  $\text{Li}_{1/2}\text{Ca}_{1/2}\text{BC}$  and (b)  $\text{Li}_{1/2}\text{Ca}_{1/3}\text{BC}$ . Each row contains the phononic dispersion (left panel), the phononic DOS decomposed into Li, Ca and BC contributions (middle panel), and the Eliashberg spectral function  $\alpha^2 F(\omega)$  with integrated e-ph coupling strength  $\lambda$  (right panel).

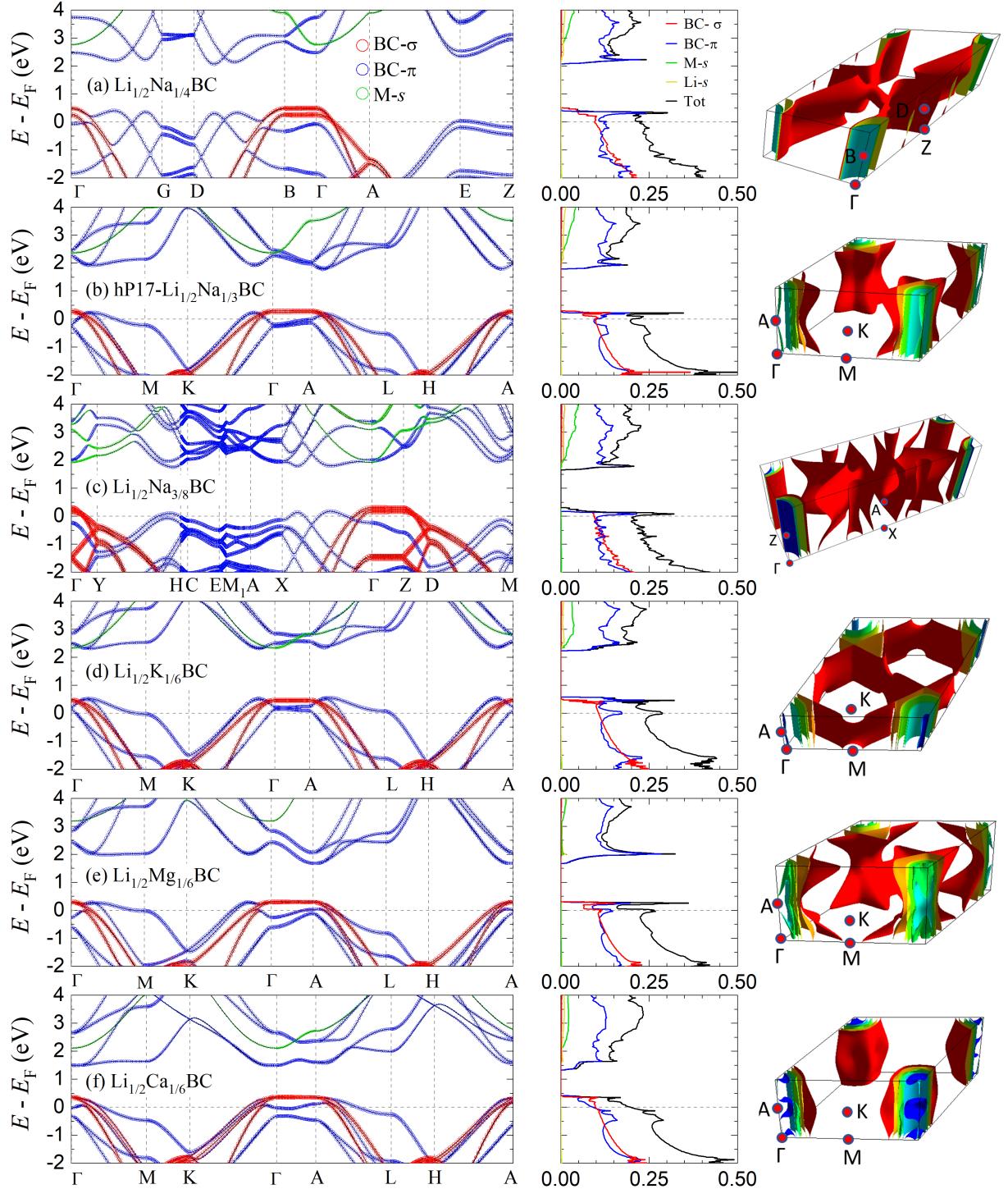


FIG. S19. Electronic properties for (a)  $\text{Li}_{1/2}\text{Na}_{1/4}\text{BC}$ , (b) hP17- $\text{Li}_{1/2}\text{Na}_{1/3}\text{BC}$ , (c)  $\text{Li}_{1/2}\text{K}_{1/6}\text{BC}$ , (d)  $\text{Li}_{1/2}\text{Mg}_{1/6}\text{BC}$ , and (e)  $\text{Li}_{1/2}\text{Ca}_{1/6}\text{BC}$ . Each row contains the electronic band structure with orbital characters (left panel), the total and projected DOS (middle panel), and the Fermi surfaces (right panel).

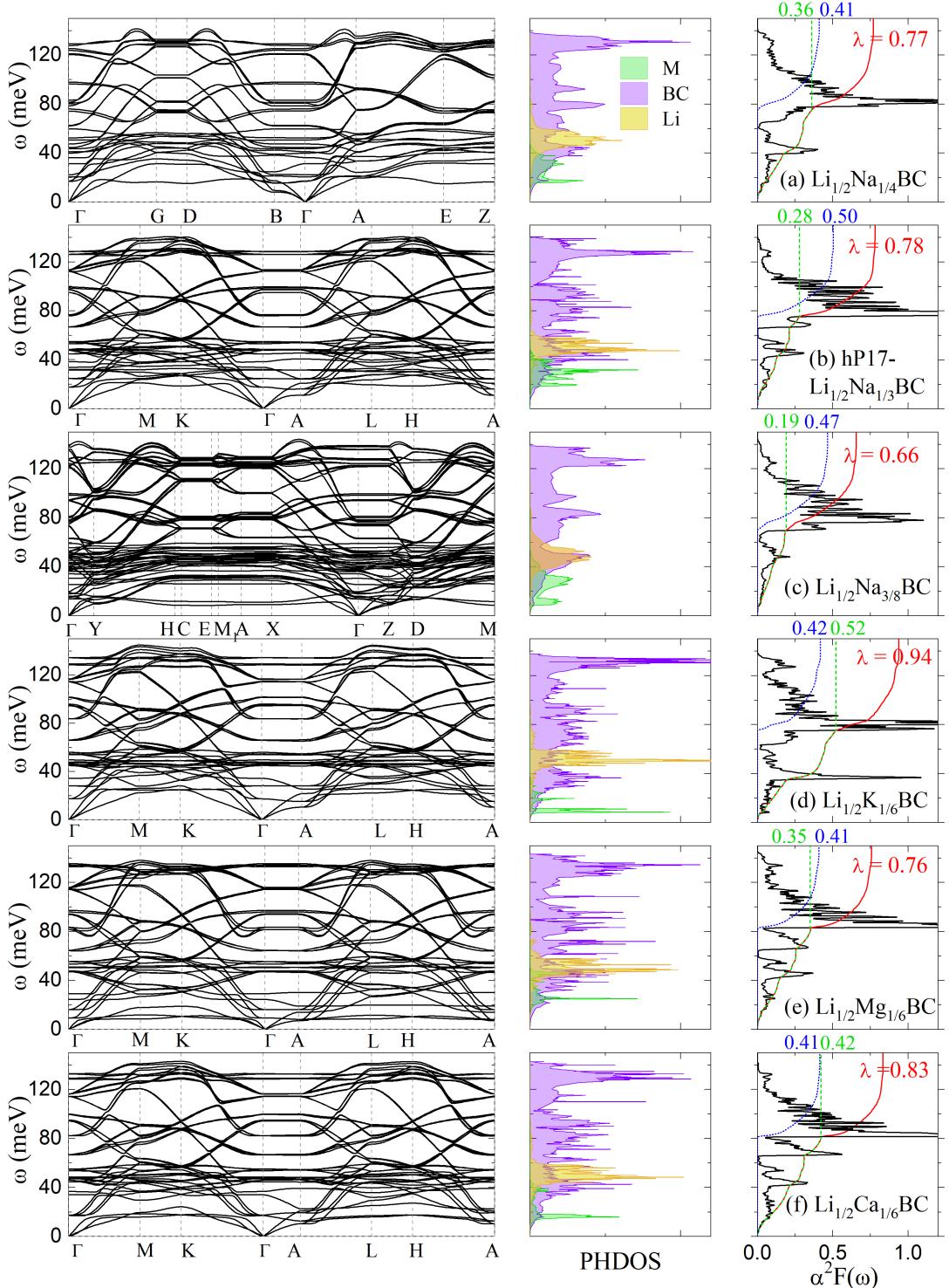


FIG. S20. Vibrational and e-ph coupling properties in (a)  $\text{Li}_{1/2}\text{Na}_{1/4}\text{BC}$ , (b) hP17- $\text{Li}_{1/2}\text{Na}_{1/3}\text{BC}$ , (c)  $\text{Li}_{1/2}\text{K}_{1/6}\text{BC}$ , (d)  $\text{Li}_{1/2}\text{Mg}_{1/6}\text{BC}$ , and (e)  $\text{Li}_{1/2}\text{Ca}_{1/6}\text{BC}$ . Each row contains the phononic dispersion (left panel), the phononic DOS decomposed into Li, M and BC contributions (middle panel), and the Eliashberg spectral function  $\alpha^2 F(\omega)$  with integrated e-ph coupling strength  $\lambda$  (right panel). The partial e-ph coupling strength from modes above and below (a-b,d) 75, (c) 70, or (e-f) 80 meV are shown as the dotted blue and dashed green lines, respectively.

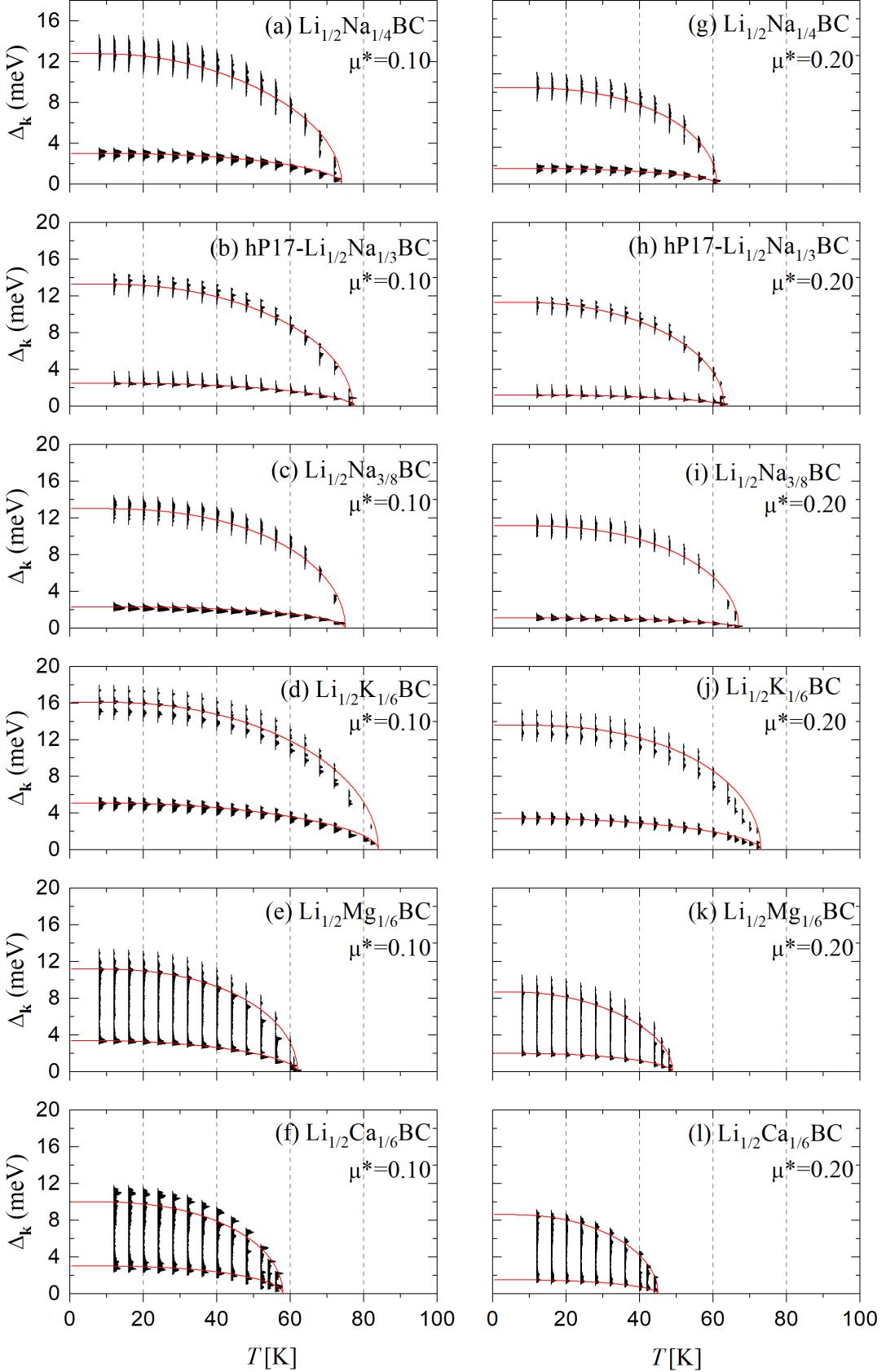


FIG. S21. Energy distribution of the superconducting gaps  $\Delta_k$  as a function of temperature with  $\mu^* = 0.10$  (left panels) and  $\mu^* = 0.20$  (right panels) for (a, g)  $\text{Li}_{1/2}\text{Na}_{1/4}\text{BC}$ , (b, h) hP17- $\text{Li}_{1/2}\text{Na}_{1/3}\text{BC}$ , (c, i)  $\text{Li}_{1/2}\text{Na}_{3/8}\text{BC}$  (d, j)  $\text{Li}_{1/2}\text{K}_{1/6}\text{BC}$ , (e, k)  $\text{Li}_{1/2}\text{Mg}_{1/6}\text{BC}$ , and (f, l)  $\text{Li}_{1/2}\text{Ca}_{1/6}\text{BC}$ . The red curves are a guide for the eye.

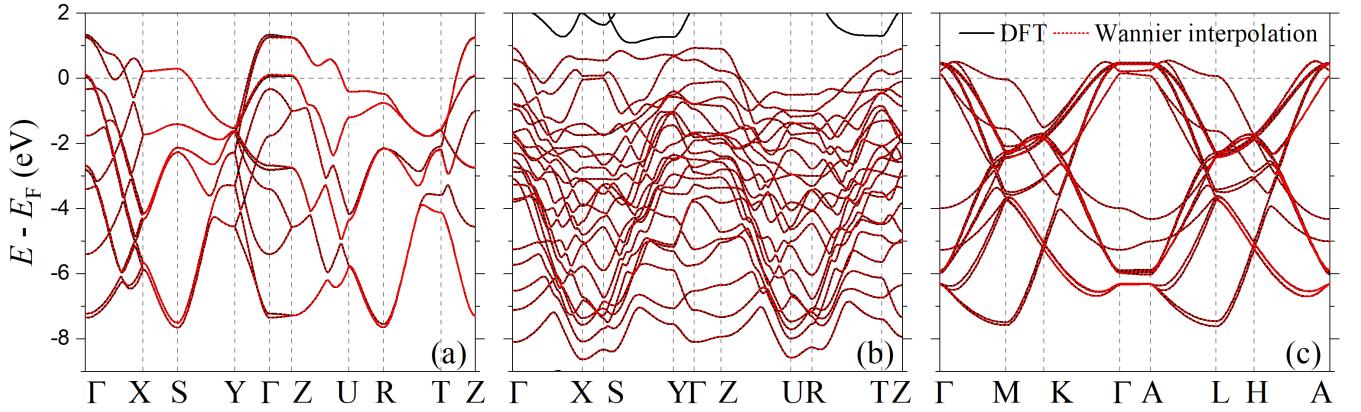


FIG. S22. Comparison of band structures obtained with DFT and Wannier interpolation for representative phases (a) oP10-Li<sub>1/2</sub>BC<sup>SRO</sup> (*Pnnm*) (b) oP20-Li<sub>1/2</sub>BC<sup>IB</sup> and (c) Li<sub>1/2</sub>K<sub>1/6</sub>BC.

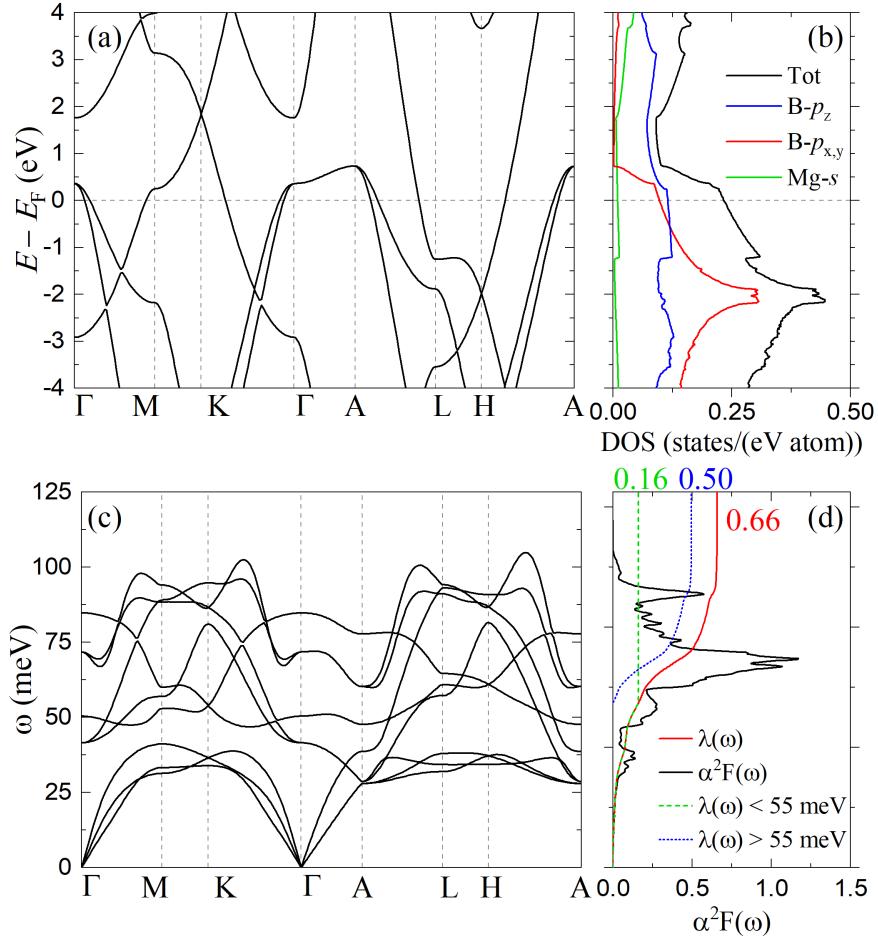


FIG. S23. Electronic and vibrational properties for MgB<sub>2</sub>. Panel (a) shows the band structure and panel (b) the total and projected density of states. Panel (c) shows the phonon dispersion and panel (d) the Eliashberg spectral function  $\alpha^2 F(\omega)$  with total integrated e-ph coupling strength  $\lambda$ . The partial e-ph coupling strength from modes above and below 55 meV are shown as the dotted blue and dashed green lines, respectively.

TABLE S1. Structural and electronic information for select  $\text{Li}_x\text{BC}$  and  $\text{Li}_x\text{M}_y\text{BC}$  phases obtained with Quantum ESPRESSO [12]. The morphology of the  $\text{Li}_x\text{BC}$  phases is specified with superscript abbreviations defined in the main text. The AA or AA'  $c$ -axis stacking notation specifies whether the placement of B and C atoms in adjacent honeycomb layers follows the same (BB and CC) or alternating (BC and CB) sequences, respectively. The total DOS at the Fermi level ( $N$ ) is listed along with partial DOS for BC- $\sigma$  ( $N_\sigma$ ) and BC- $\pi$  ( $N_\pi$ ) states. The level of hole or electron doping is given per BC formula unit. The full structural information for unit cells relaxed with VASP [13] is provided in CIF files.

Structure name	Space group	Pearson symbol	Lattice parameters (Å, °)				Stacking sequence	Buckling (Å)	DOS [states/(eV atom)]			Doping level
			<i>a</i>	<i>b</i>	<i>c</i>	$\beta$			<i>N</i>	$N_\sigma$	$N_\pi$	
$\text{Li}_{1/2}\text{BC}^{\text{SRO}}$	<i>Pnnm</i>	oP10	2.735	4.562	7.128		AA'	0.160	0.267	0.110	0.149	+1/2
$\text{Li}_{1/2}\text{BC}^{\text{SRO}}$	<i>Imm2</i>	oI10	2.728	7.083	4.601		AA	0.130	0.244	0.110	0.128	+1/2
$\text{Li}_{1/2}\text{BC}^{\text{RH}}$	<i>P\bar{3}m1</i>	hP5	2.718	—	6.420		AA'	0.032	0.240	0.116	0.117	+1/2
$\text{Li}_{1/2}\text{BC}^{\text{SRO}}$	<i>Pmma</i>	oP10	7.057	2.717	4.671		AA'	0.016	0.266	0.120	0.141	+1/2
$\text{Li}_{1/2}\text{BC}^{\text{SRO}}$	<i>P\bar{3}m1</i>	hP15	4.687	—	7.059		AA'	0.010	0.265	0.120	0.139	+1/2
$\text{Li}_{1/2}\text{BC}^{\text{IB}}$	<i>P2/m</i>	mP20	6.765	2.742	8.935	95.37	AA'		0.102	0.053	0.022	+1/2
	<i>Pmm2</i>	oP20	2.719	7.015	9.027		AA		0.113	0.047	0.061	+1/2
$\text{Li}_{1/2}\text{BC}^{\text{BR}}$	<i>P/m</i>	mP15	4.454	3.656	8.248	95.97	AA		0.083	0.083	0.000	+1/2
	<i>P/m</i>	mP30	8.241	3.650	9.004	94.89	AA		0.083	0.083	0.000	+1/2
$\text{Li}_{5/8}\text{BC}^{\text{SRO}}$	<i>C2/m</i>	mS42	5.412	5.412	7.088	91.22	AA'	0.026	0.240	0.109	0.122	+3/8
$\text{Li}_{2/3}\text{BC}^{\text{SRO}}$	<i>P6_3/mcm</i>	hP16	4.704	—	7.068		AA'	0.000	0.218	0.106	0.107	+1/3
$\text{Li}_{3/4}\text{BC}^{\text{SRO}}$	<i>Pmma</i>	oP22	5.455	4.710	7.068		AA'	0.000	0.211	0.099	0.107	+1/4
$\text{Li}_{5/6}\text{BC}^{\text{SRO}}$	<i>P\bar{3}1m</i>	hP17	4.730	—	7.054		AA'	0.009	0.235	0.097	0.130	+1/6
$\text{Li}_{7/8}\text{BC}^{\text{SRO}}$	<i>P\bar{3}m1</i>	hP23	5.470	—	7.040		AA'	0.003	0.239	0.090	0.141	+1/8
$\text{Li}_{1/2}\text{Na}_{1/4}\text{BC}$	<i>P2/m</i>	mP11	4.706	2.744	7.862	90.92	AA'	0.003	0.225	0.096	0.124	+1/4
$\text{Li}_{1/2}\text{Na}_{1/3}\text{BC}$	<i>P\bar{3}m1</i>	hP17	4.751	—	7.809		AA'	0.009	0.198	0.097	0.096	+1/6
$\text{Li}_{1/2}\text{Na}_{3/8}\text{BC}$	<i>P2/m</i>	mP23	7.846	2.759	9.489	90.43	AA'	0.023	0.214	0.093	0.114	+1/8
$\text{Li}_{1/2}\text{Mg}_{1/6}\text{BC}$	<i>P\bar{3}1m</i>	hP16	4.724	—	7.187		AA'	0.011	0.264	0.115	0.141	+1/6
$\text{Li}_{1/2}\text{Ca}_{1/6}\text{BC}$	<i>P\bar{3}m1</i>	hP16	4.722	—	7.850		AA'	0.009	0.199	0.099	0.093	+1/6
$\text{Li}_{1/2}\text{K}_{1/6}\text{BC}$	<i>P\bar{3}1m</i>	hP16	4.713	—	8.749		AA'	0.019	0.287	0.107	0.173	+1/3
$\text{Li}_{1/2}\text{Ca}_{1/3}\text{BC}$	<i>P\bar{3}m1</i>	hP17	4.818	—	7.651		AA'	0.000	0.153	0.003	0.098	-1/6
$\text{Li}_{1/2}\text{Ca}_{1/2}\text{BC}$	<i>P\bar{3}m1</i>	hP6	2.845	—	7.608		AA'	0.003	0.188	0.004	0.090	-1/2

TABLE S2. Settings used in the calculations of electronic, vibrational, and superconducting properties of  $\text{Li}_x\text{BC}$  and  $\text{Li}_x\text{M}_y\text{BC}$  phases performed with Quantum ESPRESSO (QE) [12] and EPW [14, 15].

Structure name	Space group	Pearson symbol	k-mesh (QE)	q-mesh (QE)	k-mesh (Wannier90)	# of Wannier Functions	Fine k-mesh (EPW)	Fine q-mesh (EPW)
$\text{Li}_{1/2}\text{BC}^{\text{SRO}}$	$Pnnm$	oP10	$30 \times 18 \times 8$	$6 \times 4 \times 3$	$12 \times 8 \times 6$	12	$120 \times 70 \times 30$	$60 \times 35 \times 15$
$\text{Li}_{1/2}\text{BC}^{\text{SRO}}$	$Imm2$	oI10	$30 \times 8 \times 18$	$6 \times 3 \times 4$	$12 \times 6 \times 8$	12	$120 \times 30 \times 70$	$60 \times 15 \times 35$
$\text{Li}_{1/2}\text{BC}^{\text{RH}}$	$P\bar{3}m1$	hP5	$30 \times 30 \times 8$	$6 \times 6 \times 3$	$12 \times 12 \times 6$	6	$120 \times 120 \times 30$	$60 \times 60 \times 15$
$\text{Li}_{1/2}\text{BC}^{\text{SRO}}$	$Pmma$	oP10	$8 \times 30 \times 18$	$3 \times 6 \times 4$	$6 \times 12 \times 8$	12	$30 \times 120 \times 70$	$15 \times 60 \times 35$
$\text{Li}_{1/2}\text{BC}^{\text{SRO}}$	$P\bar{3}m1$	hP15	$18 \times 18 \times 8$	$5 \times 5 \times 3$	$10 \times 10 \times 6$	18	$70 \times 70 \times 30$	$35 \times 35 \times 15$
$\text{Li}_{1/2}\text{BC}^{\text{IB}}$	$P2/m$	mP20	$12 \times 30 \times 10$	$3 \times 6 \times 2$	$6 \times 12 \times 4$	24	$50 \times 120 \times 30$	$25 \times 60 \times 15$
$\text{Li}_{1/2}\text{BC}^{\text{IB}}$	$Pmm2$	oP20	$30 \times 8 \times 8$	$6 \times 3 \times 3$	$12 \times 6 \times 6$	24	$120 \times 30 \times 30$	$60 \times 15 \times 15$
$\text{Li}_{1/2}\text{BC}^{\text{BR}}$	$P/m$	mP15	$18 \times 24 \times 8$	$4 \times 6 \times 3$	$8 \times 12 \times 6$	18	$70 \times 100 \times 30$	$35 \times 50 \times 15$
$\text{Li}_{1/2}\text{BC}^{\text{BR}}$	$P/m$	mP30	$10 \times 24 \times 8$	$3 \times 4 \times 2$				
$\text{Li}_{5/8}\text{BC}^{\text{SRO}}$	$C2/m$	mS42	$18 \times 18 \times 8$	$4 \times 4 \times 3$	$8 \times 8 \times 6$	24	$70 \times 70 \times 30$	$35 \times 35 \times 15$
$\text{Li}_{2/3}\text{BC}^{\text{SRO}}$	$P6_3/mcm$	hP16	$18 \times 18 \times 8$	$4 \times 4 \times 3$	$8 \times 8 \times 6$	18	$70 \times 70 \times 30$	$35 \times 35 \times 15$
$\text{Li}_{3/4}\text{BC}^{\text{SRO}}$	$Pmma$	oP22	$18 \times 18 \times 8$	$4 \times 4 \times 3$	$8 \times 8 \times 6$	24	$70 \times 70 \times 30$	$35 \times 35 \times 15$
$\text{Li}_{5/6}\text{BC}^{\text{SRO}}$	$P\bar{3}1m$	hP17	$18 \times 18 \times 8$	$4 \times 4 \times 3$	$8 \times 8 \times 6$	18	$70 \times 70 \times 30$	$35 \times 35 \times 15$
$\text{Li}_{1/2}\text{Na}_{1/4}\text{BC}$	$P2/m$	mP11	$18 \times 30 \times 8$	$4 \times 6 \times 3$	$8 \times 12 \times 6$	12	$70 \times 120 \times 30$	$35 \times 60 \times 15$
$\text{Li}_{1/2}\text{Na}_{1/3}\text{BC}$	$P\bar{3}m1$	hP17	$18 \times 18 \times 8$	$4 \times 4 \times 3$	$8 \times 8 \times 6$	18	$70 \times 70 \times 30$	$35 \times 35 \times 15$
$\text{Li}_{1/2}\text{Na}_{3/8}\text{BC}$	$P2/m$	mP23	$10 \times 30 \times 8$	$3 \times 4 \times 2$	$6 \times 8 \times 4$	24	$30 \times 120 \times 30$	$15 \times 60 \times 15$
$\text{Li}_{1/2}\text{K}_{1/6}\text{BC}$	$P\bar{3}1m$	hP16	$18 \times 18 \times 8$	$5 \times 5 \times 3$	$10 \times 10 \times 6$	18	$70 \times 70 \times 30$	$35 \times 35 \times 15$
$\text{Li}_{1/2}\text{Mg}_{1/6}\text{BC}$	$P\bar{3}1m$	hP16	$18 \times 18 \times 8$	$5 \times 5 \times 3$	$10 \times 10 \times 6$	18	$70 \times 70 \times 30$	$35 \times 35 \times 15$
$\text{Li}_{1/2}\text{Ca}_{1/6}\text{BC}$	$P\bar{3}m1$	hP16	$18 \times 18 \times 8$	$4 \times 4 \times 3$	$8 \times 8 \times 6$	18	$70 \times 70 \times 30$	$35 \times 35 \times 15$
$\text{Li}_{1/2}\text{Ca}_{1/3}\text{BC}$	$P\bar{3}m1$	hP17	$18 \times 18 \times 8$	$4 \times 4 \times 3$	$8 \times 8 \times 6$	18	$70 \times 70 \times 30$	$35 \times 35 \times 15$
$\text{Li}_{1/2}\text{Ca}_{1/2}\text{BC}$	$P\bar{3}m1$	hP6	$30 \times 30 \times 8$	$6 \times 6 \times 3$	$12 \times 12 \times 6$	6	$120 \times 120 \times 30$	$60 \times 60 \times 15$

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