

# Supplementary Information for

## Adjustable 1D ferroelectricity and ferrielectricity in faceted GeSe nanotubes

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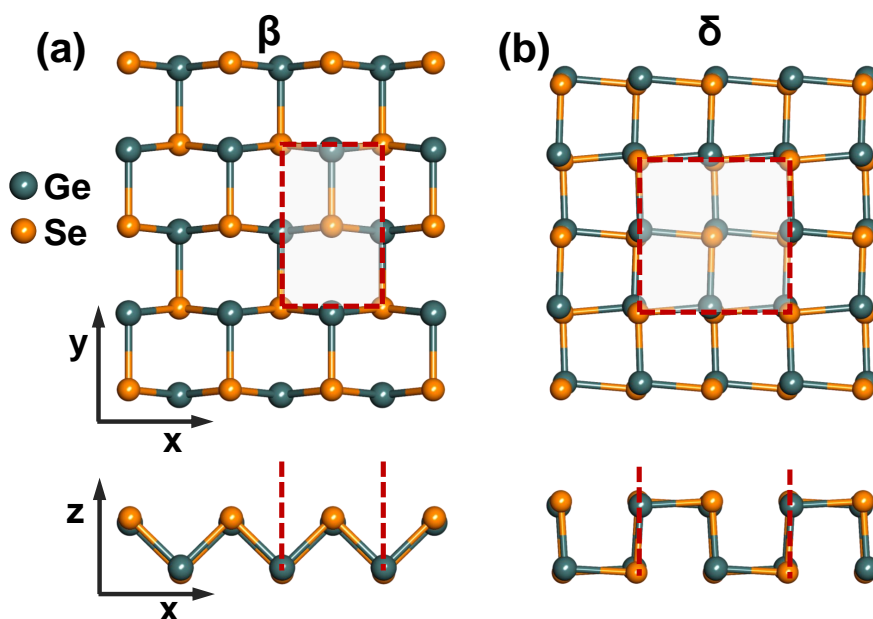


Figure S1: Equilibrium Structures of (a)  $\beta$ - and (b)  $\delta$ -GeSe monolayers in both top and side views. The unit cells are indicated by red dashed lines.

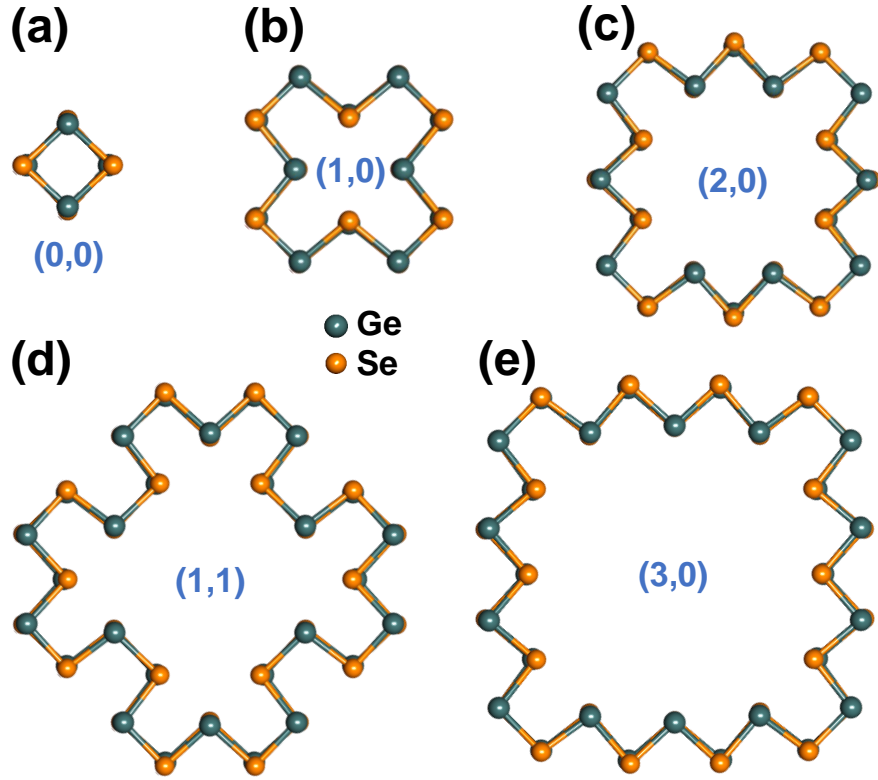


Figure S2: Equilibrium Structures of (a) (0,0)- (b) (1,0)-, (c) (2,0)-, (d) (1,1)-, and (e) (3,0)-GNTs in top view.

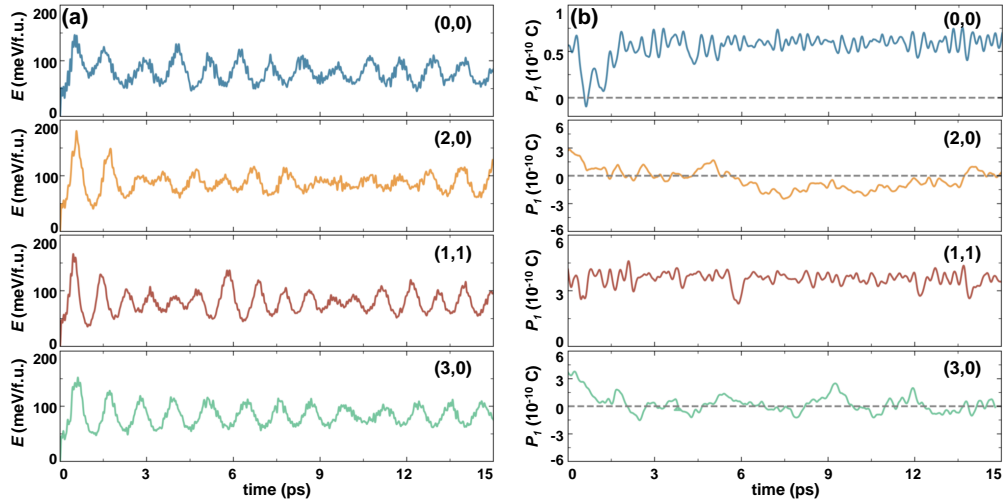


Figure S3: Fluctuations of the (a) total potential energy and (b) linear polarization ( $P_1$ ) at 300 K for (0,0)-, (2,0)-, (1,1)-, and (3,0)-GNTs.

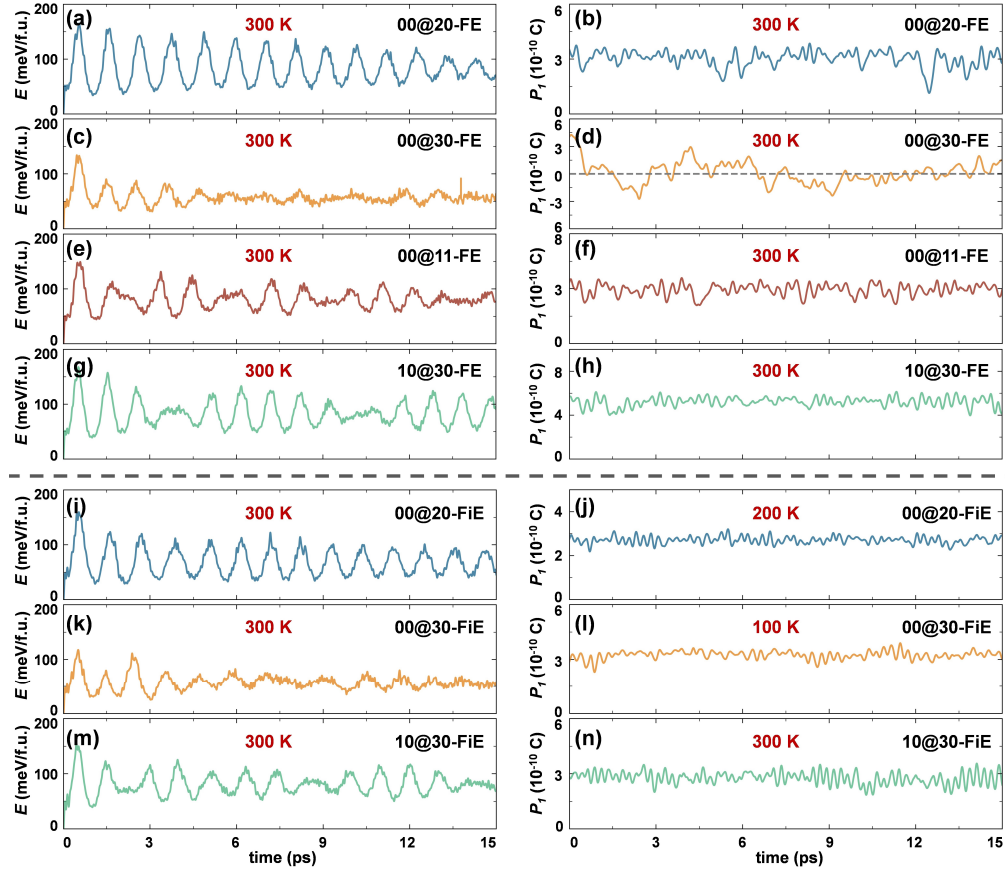


Figure S4: Fluctuations of the (a) total potential energy and (b) linear polarization ( $P_1$ ) for the FE- and FiE-stacking (0,0)@(2,0)-, (0,0)@(3,0)-, (0,0)@(1,1)-, and (1,0)@(3,0)-GNTs at selected temperatures.

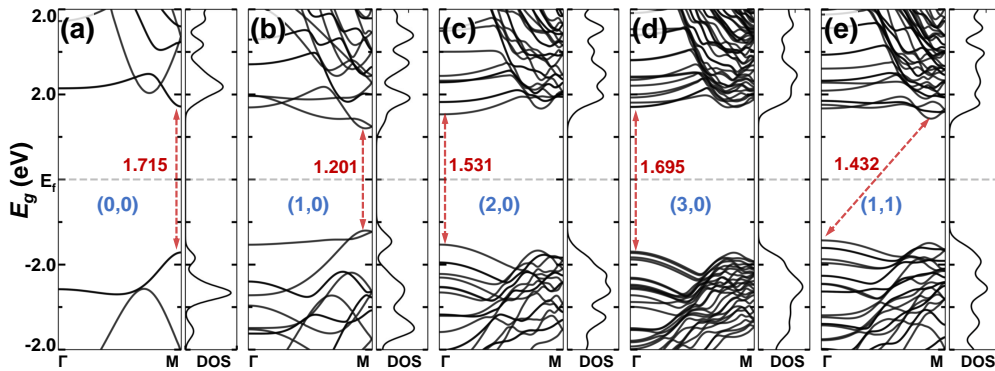


Figure S5: Electronic band structure and density of states (DOS) based on DFT-PBE for (a) (0,0)-, (b) (1,0)-, (c) (2,0)-, (d) (3,0)-, and (e) (1,1)-GNTs. The band gaps are indicated by dashed arrows and the corresponding values are given in the unit of eV.

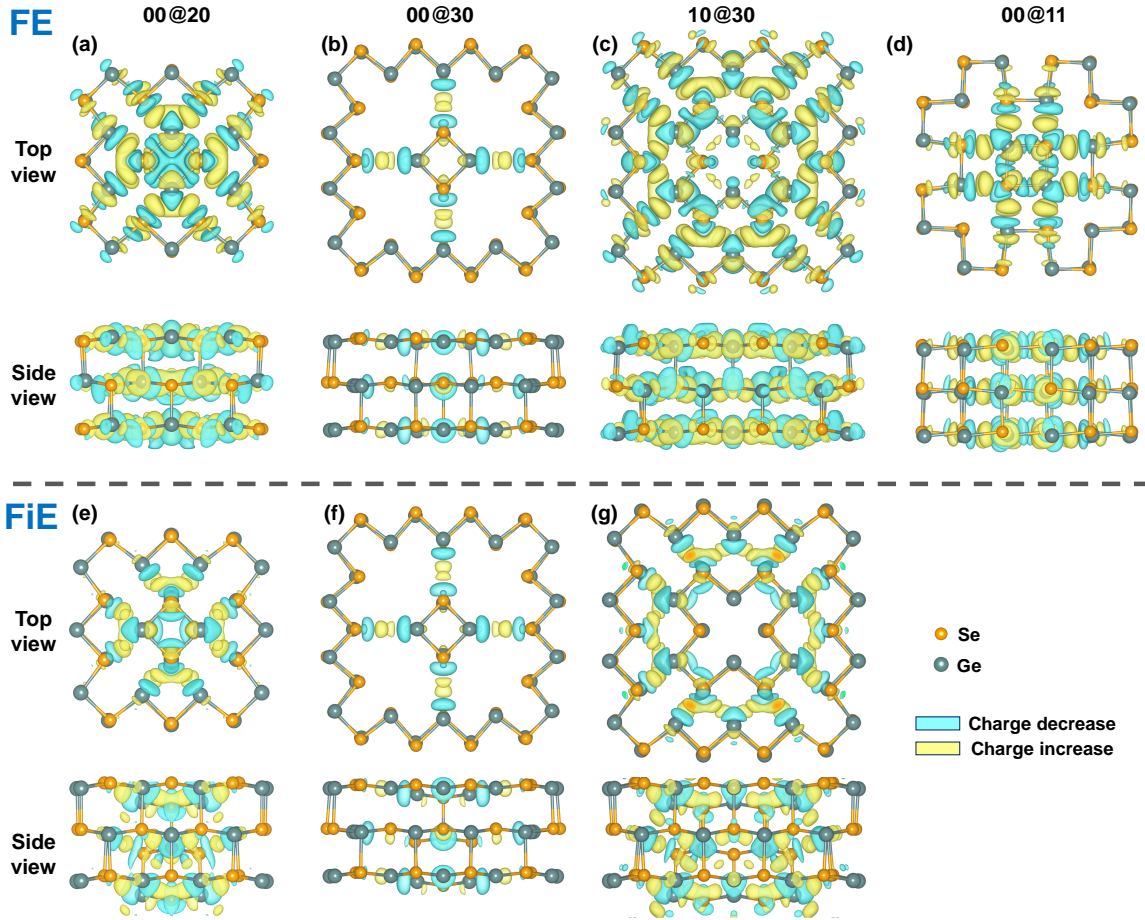


Figure S6: Differential charge density distribution for combining the DW FE-stacking (a)  $(0,0)@(2,0)-$ , (b)  $(0,0)@(3,0)-$ , (c)  $(1,0)@(3,0)-$ , (d)  $(0,0)@(1,1)-$ GNTs and FiE-stacking (e)  $(0,0)@(2,0)-$ , (f)  $(0,0)@(3,0)-$ , (g)  $(1,0)@(3,0)-$ GNTs. The yellow and blue isosurfaces represent the electron excess and deficit. The isosurface value for  $(0,0)@(3,0)-$ GNT is  $0.0002 e/\text{Bohr}^3$  and that for the others is  $0.001 e/\text{Bohr}^3$ .