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## **Supplementary**

## Near room temperature Thermoelectric performance improvement for

## Mg<sub>2</sub>Sn

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Fig. S1. The normalized inferred absorption peak of  $Mg_2Sn_{1-x}Pb_x$  ( $0 \le x \le 0.3$ ) samples at room temperature, indicating the decrease of band gap by Pb alloying.

The calculation process of Lorenze number:

$$\begin{split} L_{e} &= \left(\frac{k_{B}}{e}\right)^{2} \left[ \frac{\left(r + \frac{7}{2}\right)F_{r + \frac{5}{2}}(\xi_{e})}{\left(r + \frac{3}{2}\right)F_{r + \frac{1}{2}}(\xi_{e})} - \left(\frac{\left(r + \frac{5}{2}\right)F_{r + \frac{3}{2}}(\xi_{e})}{\left(r + \frac{3}{2}\right)F_{r + \frac{1}{2}}(\xi_{e})}\right)^{2} \right] \# (1 - 1) \\ L_{h} &= \left(\frac{k_{B}}{e}\right)^{2} \left( \frac{\left(r + \frac{7}{2}\right)F_{r + \frac{5}{2}}(\xi_{h})}{\left(r + \frac{3}{2}\right)F_{r + \frac{1}{2}}(\xi_{h})} - \left(\frac{\left(r + \frac{5}{2}\right)F_{r + \frac{3}{2}}(\xi_{h})}{\left(r + \frac{3}{2}\right)F_{r + \frac{1}{2}}(\xi_{h})}\right)^{2} \right)^{2} \# (1 - 2) \\ &\qquad S = \pm \left( \frac{\left(r + \frac{5}{2}\right)F_{r + \frac{3}{2}}(\xi_{e})}{\left(r + \frac{3}{2}\right)F_{r + \frac{1}{2}}(\xi_{e})} - \xi_{e} \right) h \# (1 - 3) \\ &\qquad \xi_{h} = -\left(\frac{E_{g}}{k_{B}T} + \xi_{e}\right) \# (1 - 4) \end{split}$$

## **Supplementary**

$$n = 2 \left( \frac{2\pi m_e^* k_B T}{h^2} \right) F_1(\xi_e) \# (1-5)$$

$$p = 2 \left( \frac{2\pi m_h^* k_B T}{h^2} \right) F_{\frac{1}{2}}(\xi_h) \# (1-6)$$
$$(n_{300 K} + \Delta) \quad (p_{300 K} + \Delta) = A T^3 \exp\left(-\frac{E_g}{k_B T}\right) \# (1-7)$$

Here, the *r* is the scattering parameter for the carrier transport based on the relaxation time approximation, where the acoustic phonon (r = -1/2) scattering dominants. The reduced Fermi energy  $\xi_e$  and  $\xi_h$  near room temperature could be estimated from the Seebeck coefficient on the basis of single band approximation formula Eq. (1-3 and 1-4). The reduced Fermi energy  $\xi(T)$  at the higher temperature is obtained by Eq. (1-4~1-7) at a given temperature.

 $m_e^*$  was obtained from the measured carrier concentration and Seebeck coefficient of Mg<sub>2.03</sub>Sn<sub>1-x</sub>Pb<sub>x</sub> in this study, while

 $m_{h=1.3}^*$  m<sub>0</sub> was used.



Fig. S2. The temperature dependent  $L_e$ ,  $L_h$  of Mg<sub>2</sub>Sn<sub>1-x</sub>Pb<sub>x</sub> ( $0 \le x \le 0.05$ ) (a) and Mg<sub>2.03</sub>Sn<sub>0.75-x</sub>Pb<sub>0.25</sub>Bi<sub>y</sub> ( $0 \le y \le 0.02$ ) (b) samples in this work.



Fig. S3. The first-principle calculated band structure of  $Mg_2Sn(a)$  and  $Mg_2Sn_{0.75}Pb_{0.25}(b)$ .