

## Supplementary Information

### Observation of planar Hall effect in topological insulator candidate

#### $\text{Ni}_3\text{Bi}_2\text{Se}_2$

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**Table S1.** The parities for each time reversal invariant momentum in  $\text{Ni}_3\text{Bi}_2\text{Se}_2$ .

$\delta(0\ 0\ 0)$	$\delta(0.5\ 0\ 0)$	$\delta(0\ 0.5\ 0)$	$\delta(0.5\ 0.5\ 0)$
-	+	+	-
$\delta(0\ 0\ 0.5)$	$\delta(0.5\ 0\ 0.5)$	$\delta(0\ 0.5\ 0.5)$	$\delta(0.5\ 0.5\ 0.5)$
+	+	+	-

By using the method in [1], we get the  $Z_2$  invariant of  $\text{Ni}_3\text{Bi}_2\text{Se}_2$  is (1;111), which indicates  $\text{Ni}_3\text{Bi}_2\text{Se}_2$  is a strong topological insulator. The parities for each time reversal invariant momentum are listed in Table S1.

**Table S2.** Crystallographic data and structure refinement parameters for Ni<sub>3</sub>Bi<sub>2</sub>Se<sub>2</sub>.

Formula	Ni <sub>3</sub> Bi <sub>2</sub> Se <sub>2</sub>
Formula weight	752.01
<i>T</i> (K)	223
Space group	<i>C2/m</i>
Unit cell dimensions	<i>a</i> = 11.1858(5) Å <i>b</i> = 8.1601(5) Å <i>c</i> = 8.0756(5) Å
Volume	537.07(6) Å <sup>3</sup>
<i>Z</i>	4
Density (calculated)	9.3 g/cm <sup>3</sup>
Goodness-of-fit on F <sup>2</sup>	1.081
Final R indices [ <i>I</i> > 2σ( <i>I</i> )]	R1 = 0.0319, wR2 = 0.0928
R indices (all data)	R1 = 0.0327, wR2 = 0.0934

**Table S3.** Atomic coordinates and equivalent isotropic displacement parameters for Ni<sub>3</sub>Bi<sub>2</sub>Se<sub>2</sub>.

U<sub>eq</sub> is defined as one third of the trace of the orthogonalized U<sub>ij</sub> tensor.

atom	x	y	z	U <sub>eq</sub> (Å <sup>2</sup> )
Bi1	0.24931(7)	0.50000	0.24327(10)	0.0179(2)
Bi2	0.28285(7)	0.50000	0.79880(11)	0.0192(2)
Se1	0.47286(2)	0.21827(5)	0.69044(9)	0.0183(3)
Ni3	0.50000	0.22650(2)	1.00000	0.0202(4)
Ni1	0.48120(2)	0.50000	0.70950(4)	0.0224(5)
Ni2	0.75000	0.25000	1.00000	0.0202(5)

**Table S4.** Selected interatomic distances [ $\text{\AA}$ ] in  $\text{Ni}_3\text{Bi}_2\text{Se}_2$ .

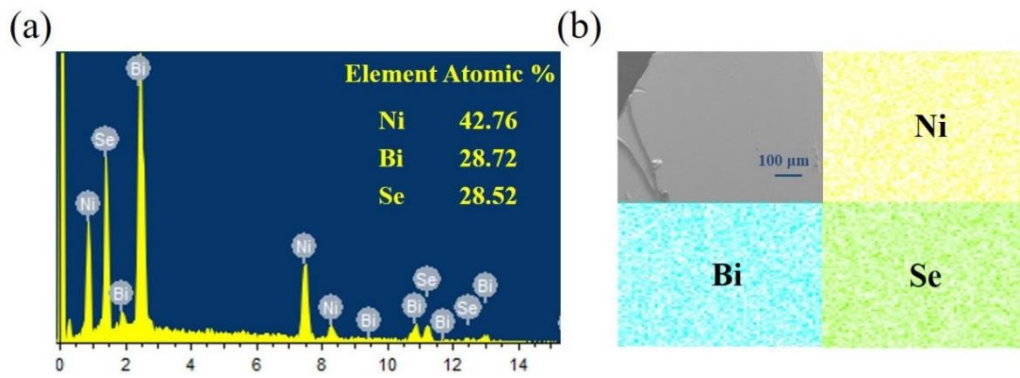
Bi1-Ni3	2.7475 (13) $\times 2$	Bi2-Ni1	2.8940(2)
Bi1-Ni1	2.7430(2)	Bi2-Ni2	2.7847(4) $\times 2$
Bi1-Ni1	2.7361(17)	Se1-Ni3	2.3036(11)
Bi1-Ni2	2.8359(4) $\times 2$	Se1-Ni1	2.3017(12)
Bi2-Bi2	3.5404(12)	Se1-Ni2	2.3045(11)
Bi2-Ni3	2.8483(15) $\times 2$	Ni3-Ni2	2.8029(17) $\times 2$
Bi2-Ni1	2.7671(17)		

**Table S5.** Anisotropic displacement parameters [ $\text{\AA}^2$ ] for  $\text{Ni}_3\text{Bi}_2\text{Se}_2$ . The anisotropic displacement factor exponent takes the form:  $-2 \pi^2 [h^2 a^{*2} U^{11} + \dots + 2 h k a^* b^* U^{12}]$ .

	$U^{11}$	$U^{22}$	$U^{33}$	$U^{23}$	$U^{13}$	$U^{12}$
Bi1	0.0178(3)	0.0180(1)	0.0182(4)	0	0.0124(3)	0
Bi2	0.0191(4)	0.0191(3)	0.0195(4)	0	0.0133(3)	0
Se1	0.0182(6)	0.0183(5)	0.0172(6)	0.0002(4)	0.0116(5)	-0.0008(4)
Ni3	0.0197(10)	0.0204(10)	0.0258(13)	0	0.0138(9)	0
Ni1	0.0222(11)	0.0204(10)	0.0258(13)	0	0.0168(1)	0
Ni2	0.0180(10)	0.0227(10)	0.0190(11)	-0.0016(7)	0.0123(9)	-0.0021(7)

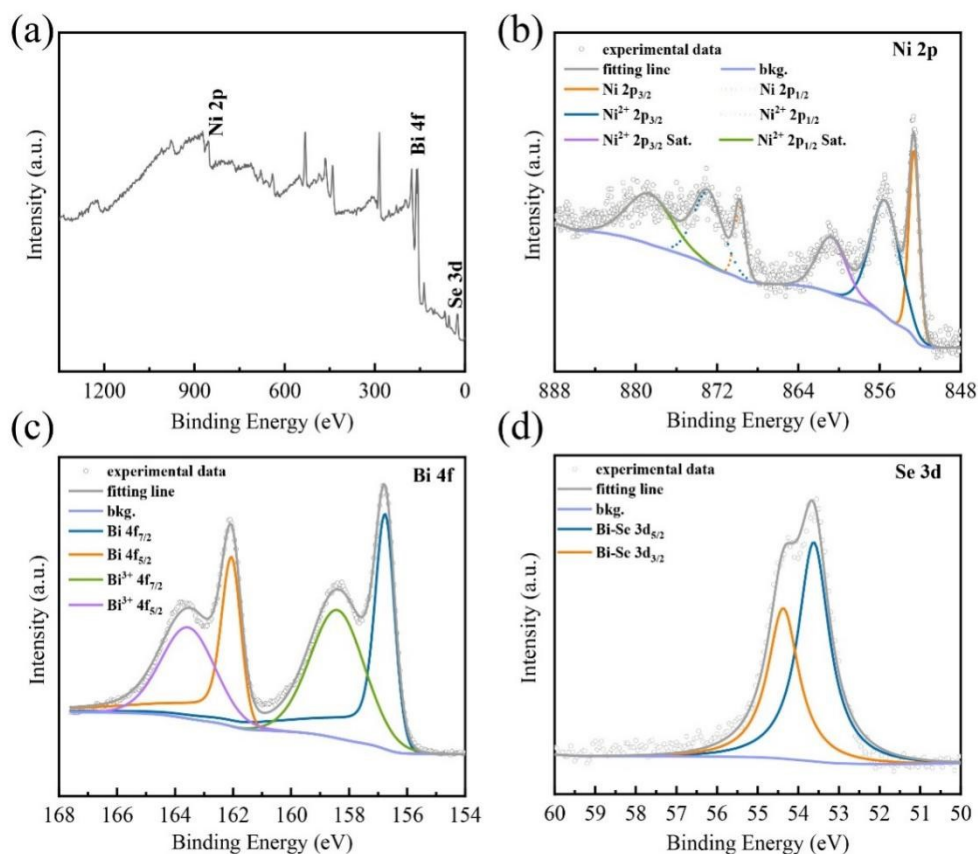
**Table S6.** The energy-dispersive X-ray spectroscopy (EDX) analyses for Ni<sub>3</sub>Bi<sub>2</sub>Se<sub>2</sub> single crystals.

Sample	Point	Ni atomic ratio (%)	Bi atomic ratio (%)	Se atomic ratio (%)
1	①	42.76	28.72	28.52
	②	42.32	28.36	28.32
	③	41.98	28.94	29.08
	④	43.01	29.02	27.79
	⑤	42.29	27.95	27.76
2	①	43.24	29.01	27.75
	②	42.84	28.48	28.68
	③	43.11	28.59	28.30
	④	42.53	27.89	29.58
	⑤	43.01	29.09	27.81



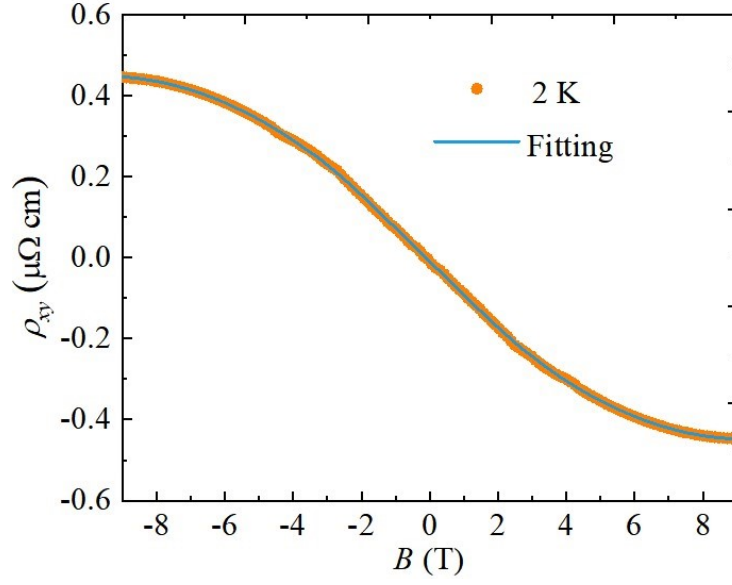
**Fig. S1** (a) The EDX spectrum of  $\text{Ni}_3\text{Bi}_2\text{Se}_2$  crystal displaying with a stoichiometric ratio. (b) The SEM and Ni, Bi, Se elemental mapping images of  $\text{Ni}_3\text{Bi}_2\text{Se}_2$  single crystal.





**Fig. S2** (a) The XPS survey spectrum of the bulk single crystal. Detailed XPS spectra of (b) Ni 2p, (c) Bi 4f, and (d) Se 3d.

Fig. S2(a) shows the X-ray photoelectron spectroscopy (XPS) survey of  $\text{Ni}_3\text{Bi}_2\text{Se}_2$ , demonstrating the presence of Ni, Bi, and Se in the single crystal, which is consistent with the results of EDX. As shown in Fig. S2(b), two peaks at binding energies of 855.43 and 872.88 eV can be assigned to Ni 2p<sub>3/2</sub> and Ni 2p<sub>1/2</sub>, respectively. The broad peaks at 860.72 and 878.65 eV correspond to the Ni 2p<sub>3/2</sub> and Ni 2p<sub>1/2</sub> satellites. For the Bi 4f spectrum, the Bi 4f<sub>7/2</sub> and Bi 4f<sub>5/2</sub> peaks with binding energies of 158.4 and 163.55 eV correspond to the Bi<sup>3+</sup> configuration in  $\text{Ni}_3\text{Bi}_2\text{Se}_2$  (Fig. S2(c)). Additionally, the two peaks at 53.62 eV and 54.37 eV observed in Figure S2(d) suggest a possible 2- valence state of Se in  $\text{Ni}_3\text{Bi}_2\text{Se}_2$ . All these results indicate the successful preparation of  $\text{Ni}_3\text{Bi}_2\text{Se}_2$ .



**Fig. S3** The magnetic-field-dependent  $\rho_{xy}$  at 2 K, and the blue solid line represents the fitting result by two-band model.

According to the two-band model, the Hall resistivity under a magnetic field can be fitted by the equation (1).

$$\rho_{xy} = \frac{1}{e} \frac{\mu_h^2 \mu_e^2 (n_h - n_e) B^3 + (\mu_h^2 n_h - \mu_e^2 n_e) B}{\mu_h^2 \mu_e^2 (n_h - n_e)^2 B^2 + (\mu_h n_h + \mu_e n_e)^2} \quad (1)$$

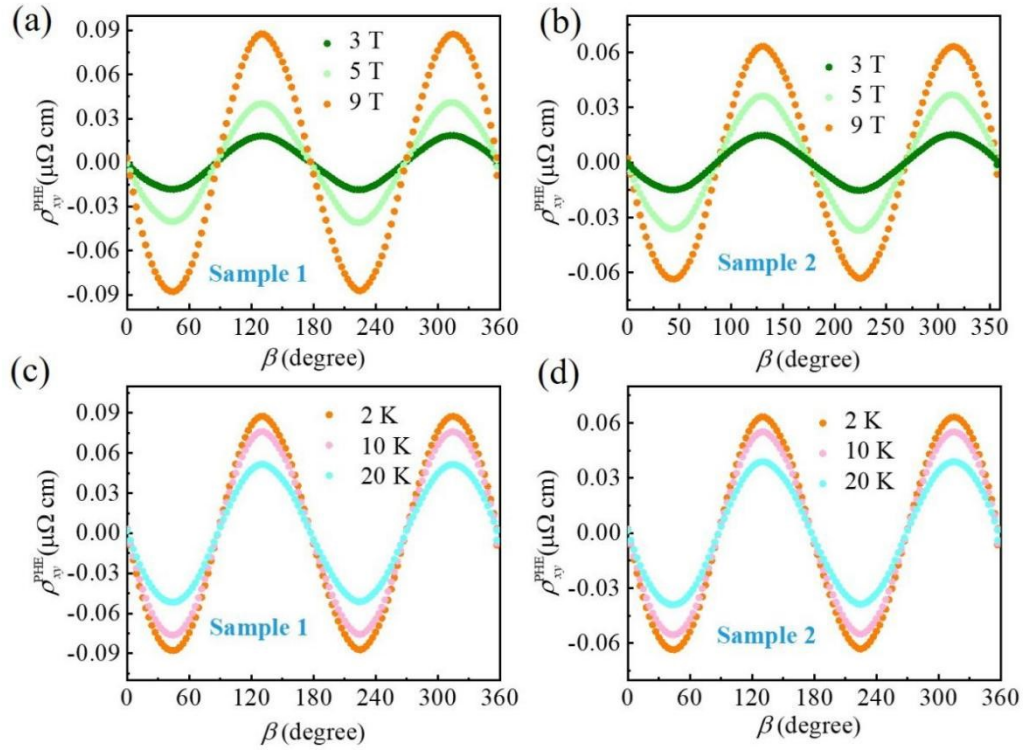
Where  $n_e$  and  $n_h$  are the concentration of electron and hole,  $u_e$  and  $u_h$  the mobility of electron and hole. Subsequently, the equation can be written as follows.

$$\rho_{xy} = \frac{aB^3 + bB}{cB^2 + 1} \quad (2)$$

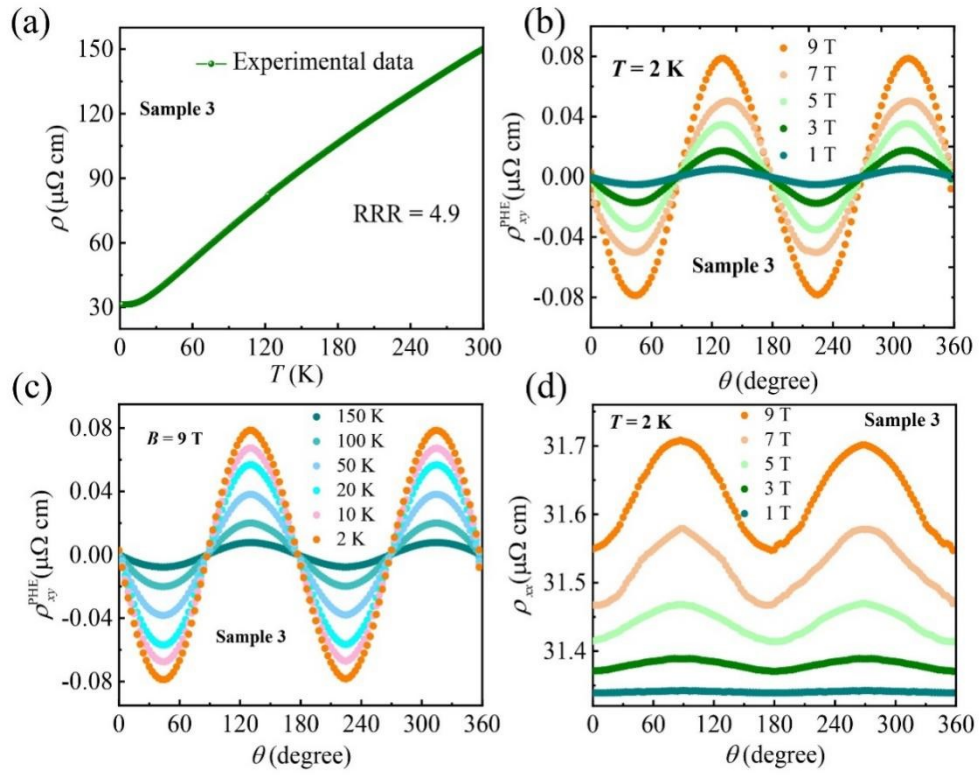
where  $a$ ,  $b$ , and  $c$  can be expressed as follows.

$$\begin{aligned} a &= \frac{e\mu_h^2\mu_e^2(n_h - n_e)}{\sigma_0^2} & b &= \frac{e(\mu_h^2 n_h - \mu_e^2 n_e)}{\sigma_0^2} \\ c &= \frac{e^2\mu_h^2\mu_e^2(n_h - n_e)^2}{\sigma_0^2} & \sigma_0 &= e(\mu_h n_h + \mu_e n_e) \end{aligned} \quad (3)$$

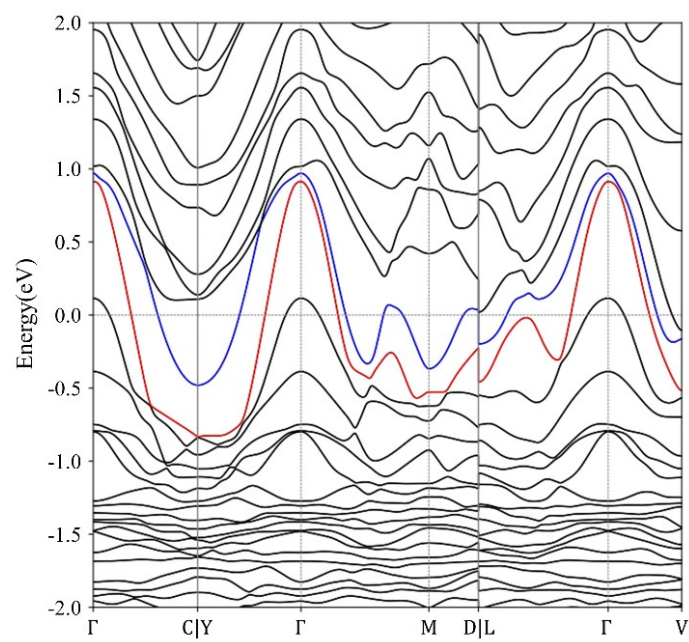
$\sigma_0$  is the conductivity at zero field ( $\sigma_0 = 1/\rho_0$ ), which can be measured independently. Then, by fitting  $\rho_{xy}(B)$  using equations (1) and (2),  $n_e$  ( $n_h$ ) and  $\mu_e$  ( $\mu_h$ ) at different temperatures were obtained.



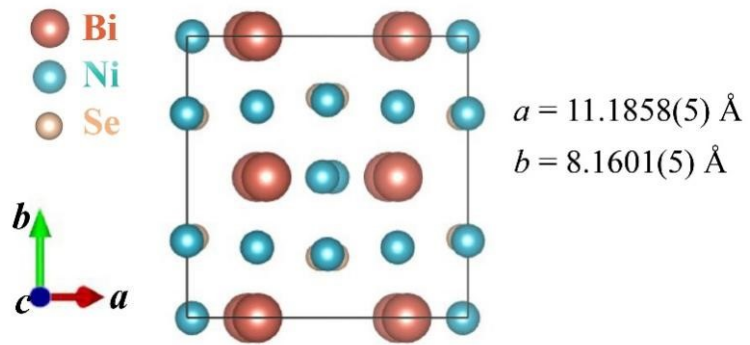
**Fig. S4** (a) (b) The planar Hall resistivity under different magnetic fields (3 T, 5 T, 7 T) at 2 K for sample 1 and sample 2. (c) (d) The angle-dependent planar Hall resistivity under different temperatures (2 K, 10 K, 20 K) at 9 T.



**Fig. S5** (a) The temperature-dependent resistivity for  $\text{Ni}_3\text{Bi}_2\text{Se}_2$  single crystal measured with  $I // ab$  plane. (b) The angle-dependent planar Hall resistivity under different magnetic fields at 2 K. (c) The PHE data under various temperatures at 9 T. (d) The angle dependence of planar resistivity at different magnetic fields for  $T = 2$  K.



**Fig. S6** The calculated electronic band structure of  $\text{Ni}_3\text{Bi}_2\text{Se}_2$  with spin-orbit coupling.



**Fig. S7** The schematic single crystal structure of  $\text{Ni}_3\text{Bi}_2\text{Se}_2$  along  $c$  axis.

## Reference

- [1] Liang Fu and C. L. Kane. *Phys. Rev. B*, 2007, **76**, 045302.