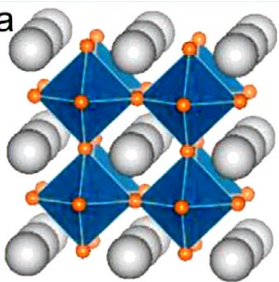
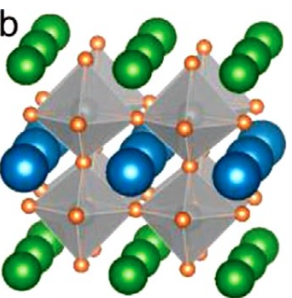
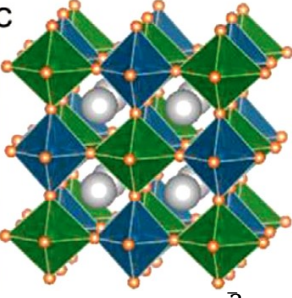
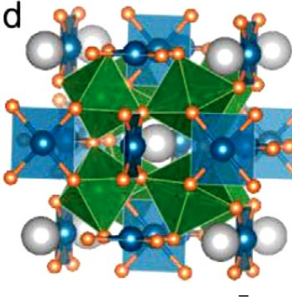


Table S1. Comparison of single perovskite oxides, double perovskite oxides, and quadruple perovskite oxides from aspects of their crystal structures and physical properties.

	Single perovskite oxides	Double perovskite oxides (DPOs)		A- and B-site-ordered quadruple perovskite oxides
		A-site ordered DPOs	B-site ordered DPOs	
General formula	ABO_3	$A'A''B_2O_6$	$A_2B'B''O_6$	$AA'_3B'_2B''_2O_{12}$
Crystal structure	 <p>Cubic, space group $Pm\bar{3}m$;</p>	 <p>Cubic, space group $R32$ or $Imm2$;</p>	 <p>Cubic, space group $Fm\bar{3}m$ or Monoclinic, space group $P2_1/n$</p>	 <p>Cubic, space group $Pn\bar{3}$</p>
Magnetic interactions	B-B interaction (or B-O-B interaction <i>via</i> oxygen ions)	$A''-B$, $A''-A''$, B-B interactions	$B'-B'$, $B''-B''$, $B'-B''$ interactions	$A'-A'$, $A'-B'$, $A'-B''$, $B'-B''$, $B'-B'$ and $B''-B''$ interactions
Structural flexibility	In ABO_3 simple perovskite (orthorhombic, $Pnma$) with AO_8 and BO_6 coordination environment, the B-O-B tilt angles are within the range of $140-180^\circ$. Random arrangements of the cation distribute along 3D directions.	$A'A''B_2O_6$ double perovskite oxides have a lamella structure with a stacking sequence of $-A'O-BO_2-A''O-BO_2-$, and A' and A'' cations are arranged alternatively along the $[001]$ crystallographic axis.	Distorted $A_2B'B''O_6$ double perovskite (monoclinic, $P2_1/n$) exhibits rock-salt ordering B' and B'' and eight-coordination AO_8 . B' and B'' cations are arranged alternatively along the $[111]$ crystallographic axis.	$AA'_3B'_2B''_2O_{12}$ quadruple perovskite oxides with 1:3 ordering A-site arrangement, have icosahedral AO_{12} , square planar $A'O_4$, and $B'O_6$ and $B''O_6$ octahedra. This special perovskite family is formed in the $a^+a^+a^+$ tilt system with very large B-O-B tilt angles of $140-145^\circ$.
Compositional flexibility	There are 32/54 kinds of elements that have been found at the A/B site with diverse oxidation states ranging from 1+ to 7+ and a wide range of ionic radii of 0.76 \AA (Li^+)– 1.52 \AA	Layered ordering of an $A'A''B_2O_6$ perovskite results in $P4/mmm$ space group symmetry. This arrangement leads to three chemically distinct environments	The structure has extremely large tolerance to different elemental combinations of (B' and B''). To maintain the charge balance, $A_2B'B''O_6$ must satisfy	$AA'_3B'_2B''_2O_{12}$ quadruple perovskite oxides combine the advantages of A- and B-site-ordered quadruple perovskite oxides. Unlike the A-site in the basic ABO_3

	(K ⁺) for A and 0.45 Å (Be ²⁺)–1.52 Å (K ⁺) for B, exhibiting large flexibility of compositions that can form the crystal structure of perovskites. In theory, there are 2346 kinds of ABO ₃ and at least 265 of them have been experimentally synthesized [1].	for the anions a structural instability when the sizes and/or bonding strengths of the A' and A'' cations are significantly different. Thus, layered ordering of A-site cations only partially alleviates the lattice strains associated with an A'/A'' size mismatch. From an electrostatic point of view rock salt ordering must also be preferable for A-site cations, yet long-range rock salt ordering of A-site cations is very rare [2].	the following equation of $2Q_A + Q_{B'} + Q_{B''} = 12$ [1]. There are thousands of the A ₂ B'B''O ₆ DPOs reported in the literature which were synthesized under ambient pressure [3]. Many new DPs were also synthesized at high-pressure.	perovskites, which is usually occupied by alkali-metal, alkaline-earth or rare-earth cations, the A'-site in AA' ₃ B' ₂ B'' ₂ O ₁₂ can accommodate transition metal ions. The introduction of A'-A', A'-B' and A'-B'' magnetic interactions in addition to B'-B'', B'-B' and B''-B'' couplings results in a variety of intriguing properties [4]. A large number of consistent elements can be introduced into A, A', B' and B''-sites by high pressure synthesis method.
Modulation of physical properties	Physical properties of the ABO ₃ simple perovskite are controlled by partial or complete substitution of the A-/B-site cations. The B-B interaction is dominantly responsible for the physical properties.	Physical properties of the A'A''B ₂ O ₆ double perovskites are not only controlled by the B-B interaction (mainly responsible for the properties of simple perovskites) but also the A''-A' and A''-B interactions.	Instead of the B-B interaction in a simple ABO ₃ perovskite, B'-B'' interaction mainly contributes to the physical properties of A ₂ B'B''O ₆ with a rock-salt ordered structure at B-site.	Physical properties of the AA' ₃ B' ₂ B'' ₂ O ₁₂ quadruple perovskite oxides are controlled by the multiple interactions between transition metal ions, i.e., A'-A', A'-B', A'-B'', B'-B'', B'-B' and B''-B'' interactions, which are complete each other.
Magnetic transition temperature (<i>T_C</i>)	Simple ABO ₃ perovskite compounds, La _{0.67} Ba _{0.33} Mn _{1-x} Cr _x O ₃ (0 ≤ x ≤ 0.15), are reported to have <i>T_C</i> values ranging from 275 K to 345 K [5]. The decrease of <i>T_C</i> is mainly interpreted by the decrease of the B-O-B bond angle and the increase of the B-O bond length as the Cr	A ₂ B'B''O ₆ DPOs with a 3 <i>d</i> transition metal ion at the B'-site and a 4 <i>d</i> or 5 <i>d</i> transition metal ion at the B''-site, are reported to exhibit magnetic transition temperatures ranging from ~ 200 K to ~ 800 K [6]. For example, Sr-based Sr ₂ B'B''O ₆ DPOs such as Sr ₂ FeReO ₆ (<i>T_C</i> = 432 K) [7], Sr ₂ FeWO ₆ (<i>T_C</i> ≈ 450 K) [8], Sr ₂ FeMoO ₆ (<i>T_C</i> ≈ 420 K) [9], Sr ₂ CrMoO ₆ (<i>T_C</i> = 450 K) [10], Sr ₂ CrReO ₆ (<i>T_C</i> = 635 K) [1q], Sr ₂ CrWO ₆ (<i>T_C</i> = 390 K) [12], and Sr ₂ CrOsO ₆ (<i>T_C</i> = 725 K) [13] are reported.	In the AA' ₃ B' ₂ B'' ₂ O ₁₂ quadruple perovskite oxides with the <i>Pn</i> $\bar{3}$ space group, the A'-A', A'-B/B', B/B'-B/B' interactions can further enhance and/or tune the physical properties. For example, the <i>T_C</i> value of quadruple perovskite oxide LaCu ₃ Fe ₂ Re ₂ O ₁₂ was	

	content increases.		reported to be 710 K due to the strong $\text{Cu}^{2+}(\uparrow)\text{Fe}^{3+}(\uparrow)\text{Re}^{4.5+}(\downarrow)$ spin interactions [14].
Magnetization ($\mu_{\text{B}}/\text{f.u.}$)	Simple ABO_3 perovskite compounds, $\text{La}_{0.67}\text{Ba}_{0.33}\text{Mn}_{1-x}\text{Cr}_x\text{O}_3$ ($0 \leq x \leq 0.15$), are reported to have magnetization values ranging from 2.73 to 3.49 $\mu_{\text{B}}/\text{f.u.}$ [5].	For $\text{A}_2\text{B}'\text{B}''\text{O}_6$ DPOs, a fully ordered state in an ideal state will result in a maximum saturation magnetization (M_{S}). For example, in theory, M_{S} is 2.0 $\mu_{\text{B}}/\text{f.u.}$ in fully ordered $\text{Bi}_2\text{FeCrO}_6$ and $\text{Bi}_2\text{NiMnO}_6$ thin films [15,16], and even higher in fully ordered $\text{La}_2\text{CoMnO}_6$ thin films, $M_{\text{S}} = 6.0 \mu_{\text{B}}/\text{f.u.}$ [17,18]. This value can be used to estimate the degree of “magnetic” ordering.	Quadruple perovskite oxide $\text{LaCu}_3\text{Fe}_2\text{Re}_2\text{O}_{12}$ has a large saturation magnetization (M_{S}) of 8.7 $\mu_{\text{B}}/\text{f.u.}$, which is considerably enhanced compared with those observed in A_2FeReO_6 ($\text{A} = \text{Ca}, \text{Sr}$ and Ba) DPOs [19-21].

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Table S2. Summaries of quadruple perovskite oxides synthesized by different methods and their crystal structures and physical properties

Synthesized methods	Quadruple perovskite oxides	Crystal structures	Physical properties	Reference
Solid-state reaction (SSR) method	A-site ordered perovskite AA'B₄O₁₂			
	CaCu ₃ Ti ₄ O ₁₂	Cubic, $Im\bar{3}$	AFM, $T_N \approx 25$ K, $M_s = 0.56 \mu_B/\text{f.u.}$, $\epsilon_r \sim 10286$, $\tan \delta \sim 0.067$	1-3
	ACu ₃ Ru ₄ O ₁₂ (A = Ca, La, and Nd)			
	CaCu ₃ Ru ₄ O ₁₂ LaCu ₃ Ru ₄ O ₁₂ NdCu ₃ Ru ₄ O ₁₂	Cubic, $Im\bar{3}$	PM, $M_s = 0.32 \mu_B/\text{f.u.}$, $\rho_{0(1.5\text{K})} = 0.110 \text{ m}\Omega \cdot \text{cm}$ $\rho_{0(1.5\text{K})} = 0.313 \text{ m}\Omega \cdot \text{cm}$, $\rho_{300\text{K}} = 1.28 \text{ m}\Omega \cdot \text{cm}$, $\Theta = 390$ K $\rho_{0(1.5\text{K})} = 0.474 \text{ m}\Omega \cdot \text{cm}$, $\Theta = 390$ K	4,5 6,7 6
	A-site columnar-ordered perovskite A₂A'A''B₄O₁₂			
	CaMnTi ₂ O ₆ (HT-HP)	Tetragonal, $P4_2mc$	$T_c = 630$ K, $P = 24 \mu\text{C}/\text{cm}^2$, $P_r = 3.5 \mu\text{C}/\text{cm}^2$, $E_c = 53 \text{ kV}/\text{cm}$	8
	CaFeTi ₂ O ₆ (HT-HP)	Tetragonal, $P4_2/nmc$	-	9
	MnLaMnSbO ₆ MnPrMnSbO ₆ MnNdMnSbO ₆ MnSmMnSbO ₆ (HT-HP)	Tetragonal, $P4_2/n$	$T_c = 48$ K, $\mu_{th} = 8.37 \mu_B/\text{f.u.}$ $T_c = 89$ K, $T_{N2} = 75$ K, $\mu_{th} = 9.12 \mu_B/\text{f.u.}$ $T_c = 76$ K, $T_{N2} = 42$ K, $\mu_{th} = 9.14 \mu_B/\text{f.u.}$, $\mu_{exp} = 8.9 \mu_B/\text{f.u.}$ $T_c = 48$ K, $T_{N2} = 39$ K, $\mu_{th} = 8.5 \mu_B/\text{f.u.}$, $\mu_{exp} = 8.3 \mu_B/\text{f.u.}$	10
SmMnGaTiO ₆ GdMnGaTiO ₆ (HT-HP)	Tetragonal, $P4_2/nmc$	$\mu_{eff} = 6.21 \mu_B/\text{f.u.}$, $M_s = 2.5 \mu_B/\text{f.u.}$, $C = 4.82 \text{ emu K}$, $T_N = 3$ K $\mu_{eff} = 9.75 \mu_B/\text{f.u.}$, $M_s = 11 \mu_B/\text{f.u.}$, $C = 11.88 \text{ emu K}$, $T_N = 3$ K	11	
RMnMn ₂ O ₆ (R=Gd-Tm and Y) (HTHP) Tm _{0.88} Mn ₃ O _{5.82} Er _{0.88} Mn ₃ O _{5.82} Ho _{0.9} Mn ₃ O _{5.85} Y _{0.9} Mn ₃ O _{5.85} DyMn ₃ O ₆ GdMn _{2.833} O _{5.75}	Orthorhombic, $Pmmn$	$\mu_{eff} = 10.608 \mu_B/\text{f.u.}$, $M_s = 6.4 \mu_B/\text{f.u.}$, $T_{N1} = 75$ K, $T_{N2} = 20$ K $\mu_{eff} = 12.318 \mu_B/\text{f.u.}$, $M_s = 6.97 \mu_B/\text{f.u.}$, $T_{N1} = 68$ K, $T_{N2} = 21$ K $\mu_{eff} = 12.917 \mu_B/\text{f.u.}$, $M_s = 6.89 \mu_B/\text{f.u.}$, $T_{N1a} = 69$ K, $T_{N1b} = 65$ K $\mu_{eff} = 8.027 \mu_B/\text{f.u.}$, $M_s = 3.05 \mu_B/\text{f.u.}$, $T_{N1a} = 69$ K, $T_{N1b} = 65$ K $\mu_{eff} = 13.444 \mu_B/\text{f.u.}$, $M_s = 7.18 \mu_B/\text{f.u.}$, $T_{N1} = 58$ K, $T_{N2} = 46$ K $\mu_{eff} = 11.095 \mu_B/\text{f.u.}$, $M_s = 6.39 \mu_B/\text{f.u.}$, $T_N = 87$ K	12	
Solid-state reaction (SSR) method				

	CaMnMnReO ₆ (HT-HP) Ca(Mn _{0.5} Cu _{0.5})FeReO ₆	Tetragonal, $P4_2/n$	$T_{N1}=100$ K, $T_{N2}=120$ K, $M_s=3.4$ μ_B /f.u. $T_{N1}=160$ K, $T_{N2}=560$ K, $M_s=4.8$ μ_B /f.u.	13
	A- and B-site multiply ordered perovskite AA'B₂B'₂O₁₂			
	LaCu ₃ Fe ₂ TiSbO ₁₂	Cubic, $Im\bar{3}$	AFM, $T_{N1}=60$ K, $T_{N2}=160$ K, $M_s=1.2$ μ_B /f.u.	14
	Hexagonal quadruple perovskite oxides			
	Ba ₄ BiIr ₃ O ₁₂	Hexagonal, $C2/m$	$T_N=215$ K, $\mu_{\text{eff}}=0.22$ μ_B /Ir.	15
	Ba ₄ EuRu ₃ O ₁₂ Ba ₄ EuIr ₃ O ₁₂	Hexagonal, $C2/m$	AFM, $T_N=4$ K, $\mu_{\text{eff}}=1.18$ μ_B /f.u., $E_a=0.18$ eV PM, $E_a=0.22$ eV, $\Theta_p = -0.773$ K	16
	Ba ₄ LuRu ₃ O ₁₂ Ba ₄ NdRu ₃ O ₁₂	Hexagonal, $R-3m$ Hexagonal, $C2/m$	AFM, $\mu_{\text{eff}}=2.86$ μ_B /f.u., $T_N=8$ K FiM, $\mu_{\text{eff}}=4.7$ μ_B /f.u., $T_N=11.5$ K	17
	Ba ₄ CuNb ₃ O ₁₂	Hexagonal, $P6_3/mmc$	-	18
	A-site ordered perovskite AA'B₄O₁₂			
Sol-gel method	CaCu ₂ MnTi ₃ MnO ₁₂	Cubic, $Im\bar{3}$	AFM, $\mu_{\text{eff}}=3.85$ μ_B /f.u., $\epsilon_r \sim 2040$	19
	CdCu ₃ Fe ₄ O ₁₂	Cubic, $Im\bar{3}$	FM/AFM, $T_c = 190$ K, $T_N=170$ K, $M_s=1.6$ μ_B /f.u.	20
	LaCu ₃ Mn ₃ TiO ₁₂ LaCu ₃ Mn _{3.5} Ti _{0.5} O ₁₂ LaCu ₂ Mn ₄ TiO ₁₂	Cubic, $Im\bar{3}$	AFM, $T_c=230$ K, $M_s=8.6$ μ_B /f.u., $M_{\text{cal}}=7$ μ_B /f.u. AFM, $T_c=235$ K, $M_s=10.4$ μ_B /f.u., $M_{\text{cal}}=8.5$ μ_B /f.u. AFM, $T_c=225$ K, $M_s=10.82$ μ_B /f.u., $M_{\text{cal}}=9$ μ_B /f.u.	21
	A- and B-site multiply ordered perovskite AA'B₂B'₂O₁₂			
	CaCu ₃ Fe ₂ Sb ₂ O ₁₂	Cubic, $Pn\bar{3}$	AFM, $T_N=160$ K, $M_s=5.35$ μ_B /f.u., $\rho > 10^7$ Ω	22
		A-site columnar-ordered perovskite A₂A'A''B₄O₁₂		
	Y ₂ CuMnMn ₄ O ₁₂	$Pm\bar{m}n$	PM, $T_N=175$ K/159K	26

High temperature and high pressure	$\text{Ho}_2\text{MnGaMn}_4\text{O}_{12}$	$P4_2/nmc$	$\mu_{\text{eff}}=18.428 \mu_{\text{B}}/\text{f.u.}$, $\Theta_{\text{p}} = -21.5(3) \text{ K}$	27
	$\text{Dy}_2\text{CuMnMn}_4\text{O}_{12}$	$Pm\bar{m}n$	$T_{\text{N}1}=160 \text{ K}$, $T_{\text{N}2}=125 \text{ K}$, $T_{\text{N}3}=21 \text{ K}$	27
	$\text{Y}_2\text{CuMnMn}_4\text{O}_{12}$	$Pm\bar{m}n$	PM, $T_{\text{N}}=175\text{K}/159\text{K}$	26
	A- and B-site multiply ordered perovskite $\text{AA}'_3\text{B}_2\text{B}'_2\text{O}_{12}$			
	$\text{CaCu}_3\text{Co}_2\text{Re}_2\text{O}_{12}$	Cubic, $Pn\bar{3}$	FiM/FM, $\mu_{\text{eff}}=10.09 \mu_{\text{B}}/\text{f.u.}$, $M_{\text{s}}=4 \mu_{\text{B}}/\text{f.u.}$, $T_{\text{c}}=20 \text{ K}$, $T_{\text{N}}=28 \text{ K}$, $C=12.1 \text{ emu K Oe}^{-1} \text{ mol}^{-1}$	28
	$\text{CaCu}_3\text{Fe}_2\text{Re}_2\text{O}_{12}$	Cubic, $Pn\bar{3}$	FiM, $M_{\text{s}}=8.7 \mu_{\text{B}}/\text{f.u.}$, $T_{\text{c}} = 560 \text{ K}$, $T_{\text{N}}= 28 \text{ K}$, $\rho=10 \text{ m}\Omega \cdot \text{cm}$	29
	$\text{LaMn}_3\text{Ni}_2\text{Mn}_2\text{O}_{12}$	Cubic, $Pn\bar{3}$	FM, $M_{\text{s}}=6.6 \mu_{\text{B}}/\text{f.u.}$, $T_{\text{c}}=34 \text{ K}$, $T_{\text{N}}= 46 \text{ K}$	30
$\text{NaCu}_3\text{Fe}_2\text{Os}_2\text{O}_{12}$	Cubic, $Pn\bar{3}$	FiM, $T_{\text{c}}=380 \text{ K}$, $M_{\text{s}}=5.5 \mu_{\text{B}}/\text{f.u.}$	31	

FM: Ferromagnetic; AFM: Antiferromagnetic; PM: Paramagnetic; FiM Ferrimagnetic, T_{N} : Neel temperature; T_{c} : Curie temperatures; ρ : Electrical resistivity; ρ_0 : Residual resistivity; Θ : Einstein temperature; E_{c} : Coercive field; P : Spontaneous Polarization; μ_{eff} : Effective moment; μ_{th} : Theoretical moment; μ_{exp} : Experimental moments; C : Curie constants; E_{a} : Activation energies; Θ_{p} : Curie-Weiss temperature; M_{cal} : Calculated magnetization; M_{s} : Saturation magnetization; ϵ : Dielectric constant; $\tan \delta$: Dielectric loss.

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