

## Supplementary Information

### Intrinsic Quantum Anomalous Hall Effect in TaPdXTe (X = S, Se) monolayer

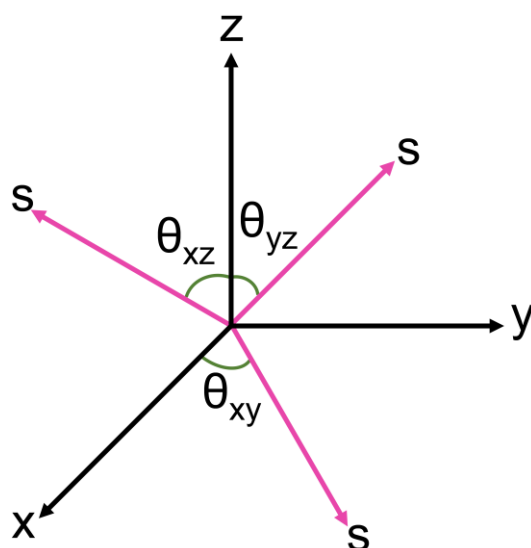
Haofeng Wei<sup>a</sup>, Yanzhao Wu<sup>a</sup>, Junwei Tong<sup>b</sup>, Li Deng<sup>a</sup>, Xiang Yin<sup>a</sup>, Zhijun Zhang<sup>c</sup>, and Xianmin Zhang<sup>a\*</sup>

<sup>a</sup>Key Laboratory for Anisotropy and Texture of Materials (Ministry of Education), School of Material Science and Engineering, Northeastern University, Shenyang, 110819, China

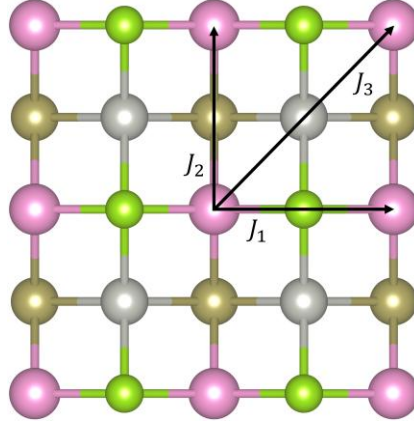
<sup>b</sup>Department of Physics, Freie Universität Berlin, Berlin, 14195, Germany

<sup>c</sup>Liaoning Institute of Science and Technology, Benxi 117004, China

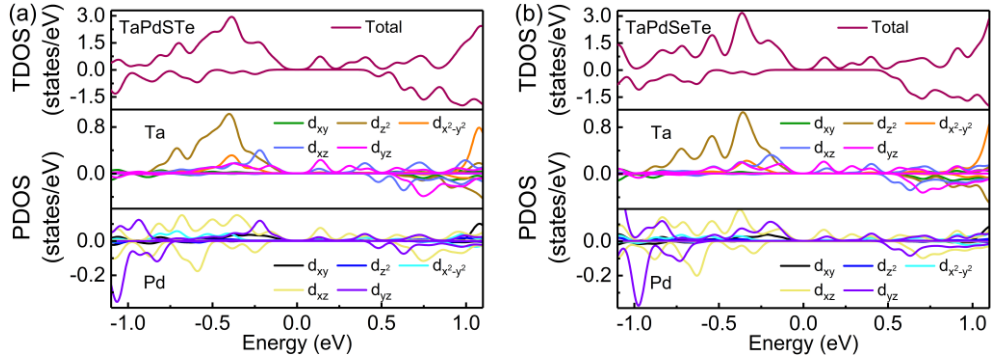
In this study, the first-principles calculations based on Density Functional Theory (DFT) are performed using the Vienna ab initio simulation package (VASP)<sup>[1, 2]</sup>. The interaction between electrons and ions is described using the projector-augmented wave (PAW) method<sup>[3, 4]</sup>. The generalized gradient approximation (GGA) with the Perdew-Burke-Ernzerhof (PBE) formalism is used to describe the exchange-correlation interaction<sup>[5]</sup>. A  $11 \times 11 \times 1$  Monkhorst-Pack k-point meshes is used to sample the Brillouin zone<sup>[6]</sup>. The cut-off energy is set to 500 eV. The convergence criteria for force and energy are  $0.005 \text{ eV/\AA}$  and  $10^{-8} \text{ eV}$ , respectively. The vacuum layer in the z direction is set to  $15 \text{ \AA}$ , thus avoiding interactions between neighboring layer atoms. The d orbitals of Ta and Pd atoms are treated using the PBE+ $U_{\text{eff}}$  method<sup>[7]</sup>, with the Hubbard  $U_{\text{eff}}$  parameter set to 4 eV<sup>[8]</sup>. Phonon spectrum is calculated using a  $3 \times 3 \times 1$  supercell and the PHONOPY package<sup>[9, 10]</sup>. Ab initio molecular dynamics simulations are performed under the NVT ensemble at 300 K<sup>[11]</sup>. The data for the calculations are processed using the VASPKIT package<sup>[12]</sup>. A maximized localization function is created using the WANNIER90 package<sup>[13]</sup>. The Berry curvature, anomalous Hall conductivity, and chiral edge state are calculated using the WannierTools package<sup>[14]</sup>. The  $T_C$  is calculated through Monte Carlo (MC) simulations, and MC simulations are performed using a  $32 \times 32 \times 1$  supercell and  $1 \times 10^7$  steps at each temperature.



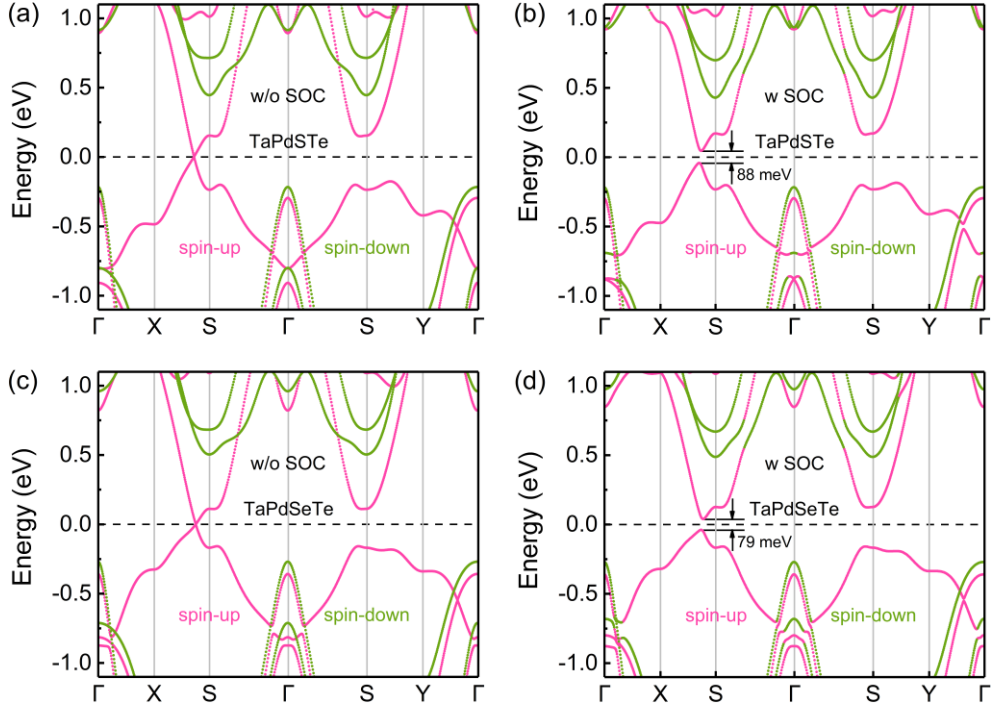
**Fig. S1.** The Schematic diagram shows the spin vector  $S$  rotating at an angle  $\theta$  from 0 to  $180^\circ$  in  $xy$ ,  $xz$ , and  $yz$  planes.



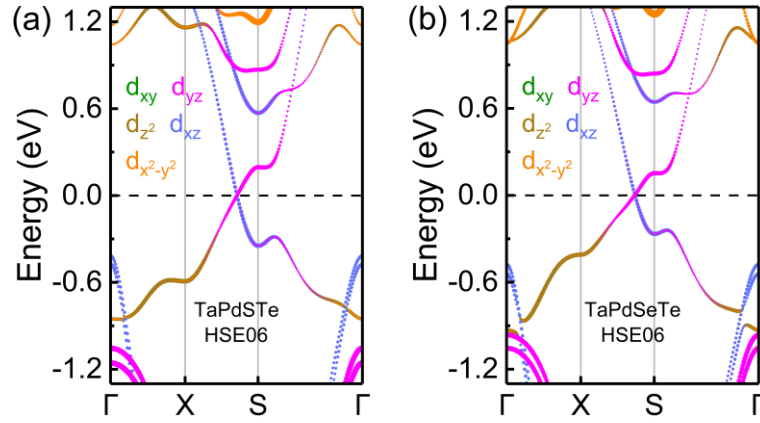
**Fig. S2.** Schematic diagram of the three exchange parameters ( $J_1$ ,  $J_2$ , and  $J_3$ ) for TaPdSTe (TaPdSeTe) monolayer.



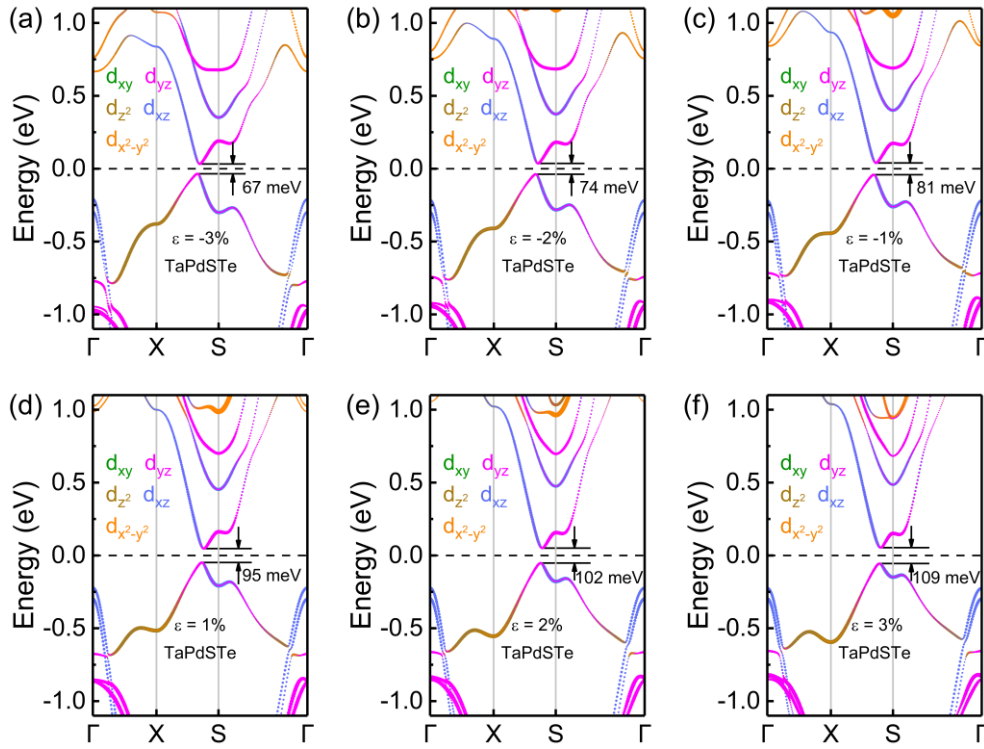
**Fig. S3.** Total density of states (TDOS) and projected density of states (PDOS) for the Ta and Pd atoms of (a) TaPdSTe and (b) TaPdSeTe monolayers.



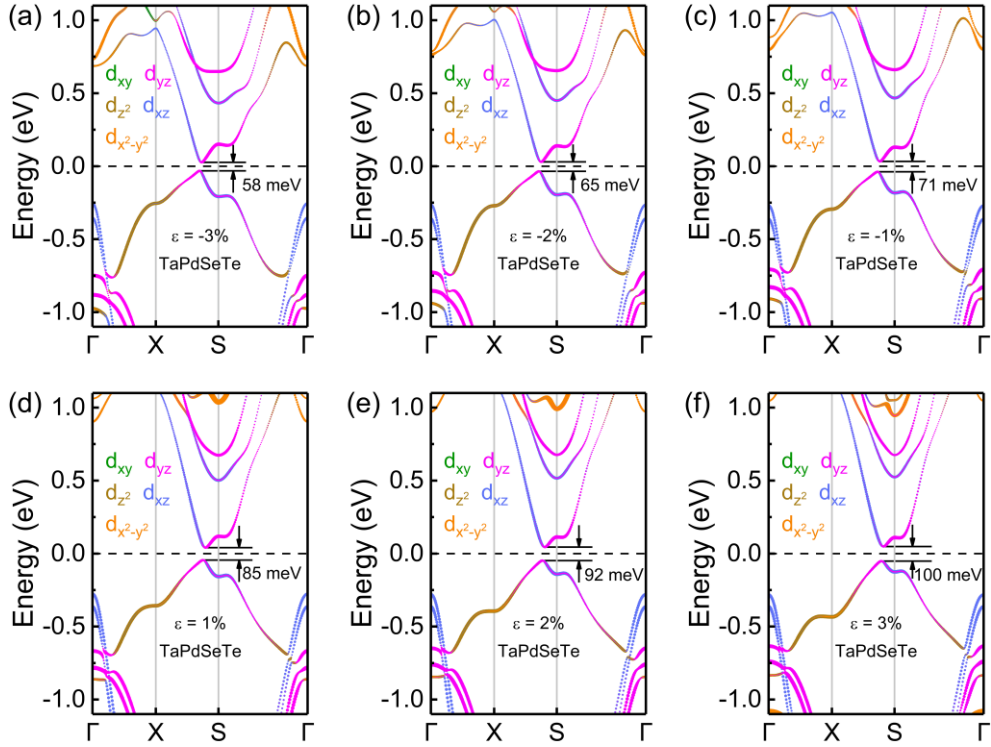
**Fig. S4.** The spin-resolved energy bands for TaPdSTe monolayer (a) without SOC and (b) with SOC effect. The spin-resolved energy bands for TaPdSeTe monolayer (c) without SOC and (d) with SOC effect.



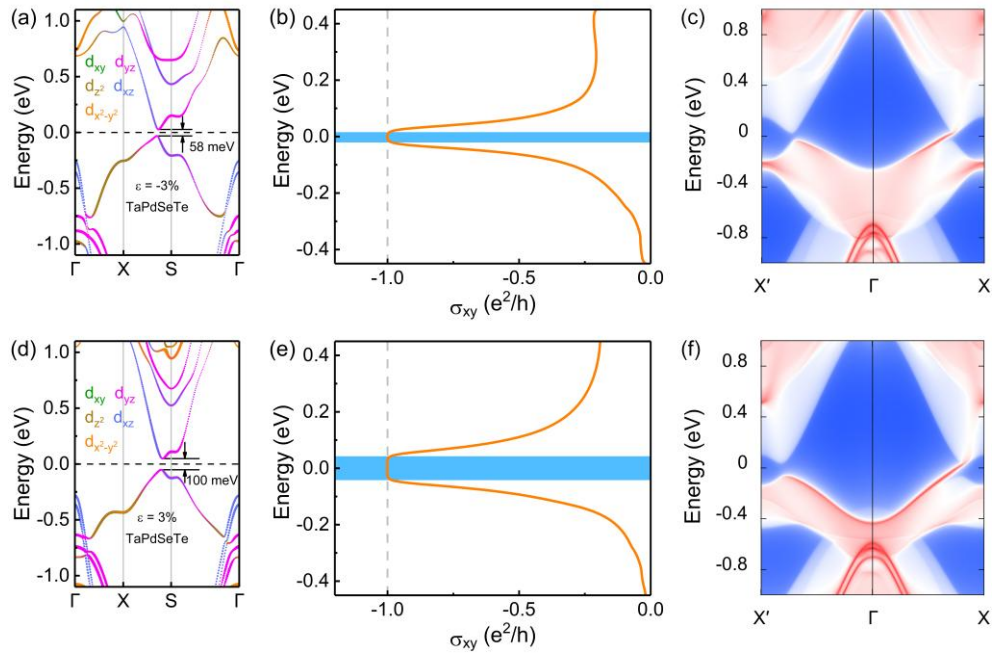
**Fig. S5.** (a) Orbit-resolved energy bands for TaPdSTe monolayer without considering SOC effect from HSE06 method. (b) Orbit-resolved energy bands for TaPdSeTe monolayer without considering SOC effect from HSE06 method.



**Fig. S6.** Orbit-resolved energy bands for TaPdSTe monolayer with SOC effect under (a) -3%, (b) -2%, (c) -1%, (d) 1%, (e) 2%, and (f) 3% strains.



**Fig. S7.** Orbit-resolved energy bands for TaPdSeTe monolayer with SOC effect under (a) -3%, (b) -2%, (c) -1%, (d) 1%, (e) 2%, and (f) 3% strains.



**Fig. S8.** (a) Orbit-resolved energy bands with SOC effect, (b) AHC, and (c) chiral edge state for TaPdSeTe monolayer under -3% strain. (d) Orbit-resolved energy bands with SOC effect, (e) AHC, and (f) chiral edge state for TaPdSeTe monolayer under 3% strain.

## References

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