

**Improving electromagnetic engineering of thermal conductive composites by
establishing continuous thermal conductive networks with gradient impedance**

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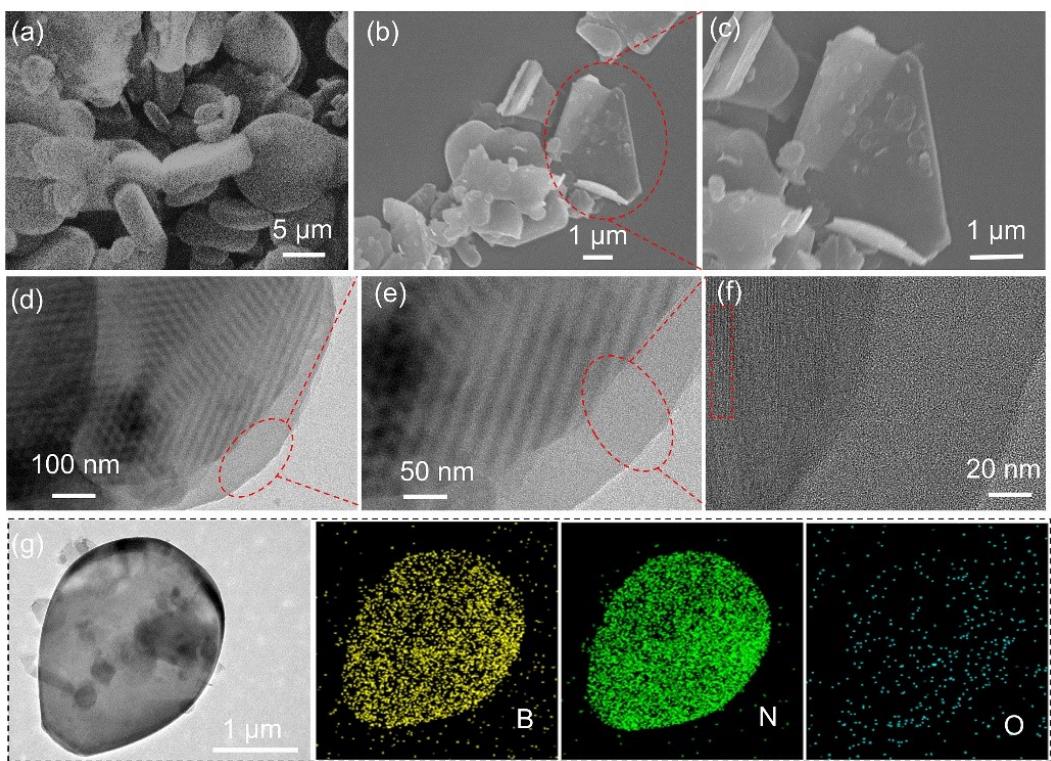


Fig. S1. SEM images of a) h-BN, b-c) few-layer BNNS. d-f) TEM images of few-layer BNNS and g) few-layer BNNS element mapping.

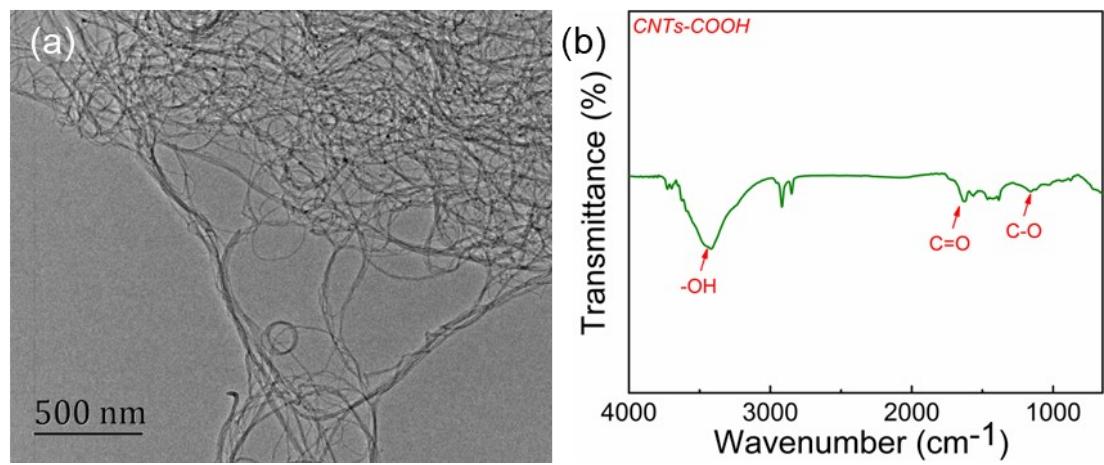


Fig. S2. (a) TEM images of CNTs-COOH, (b) FT-IR spectrum of CNTs-COOH.

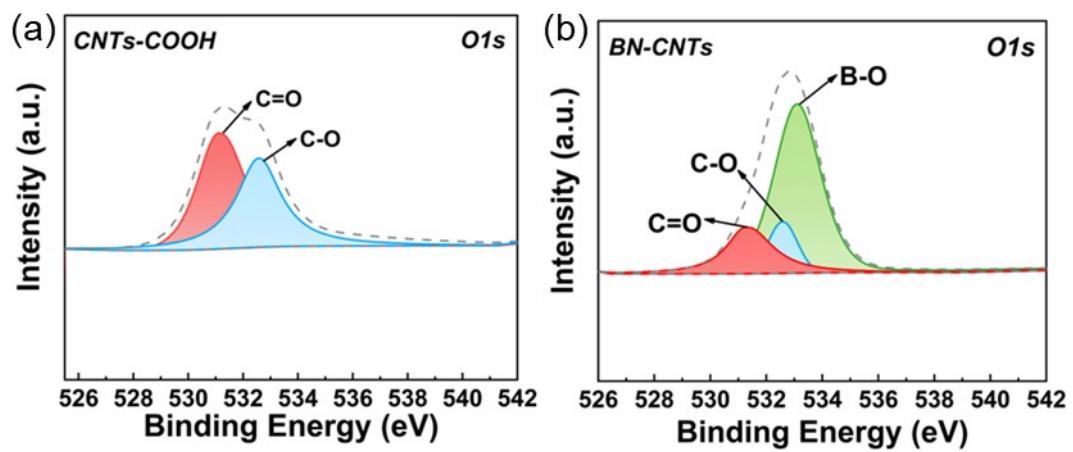


Fig. S3. XPS spectrums of O1s for CNTs-COOH and BN-CNTs hybrids, respectively.

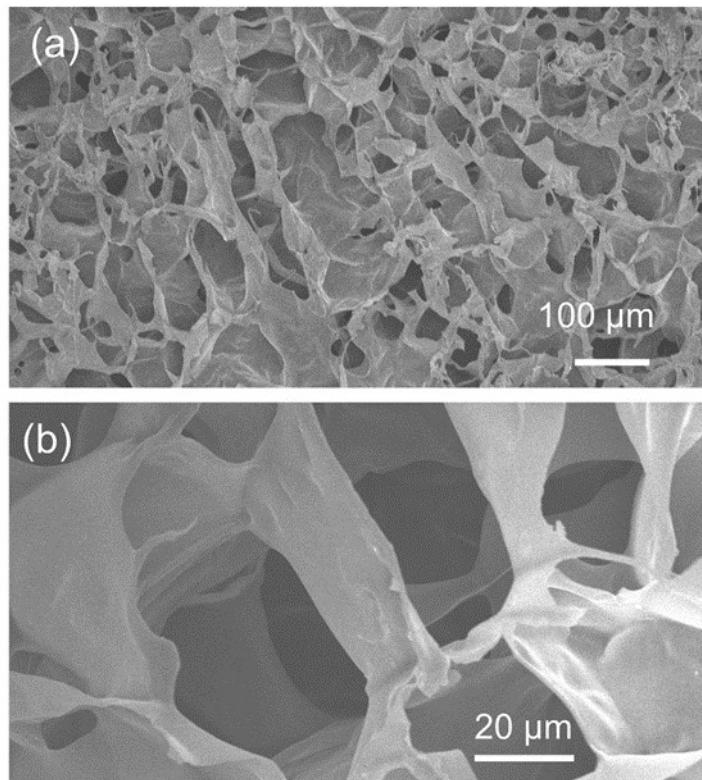


Figure S4. SEM images of CMC aerogel.

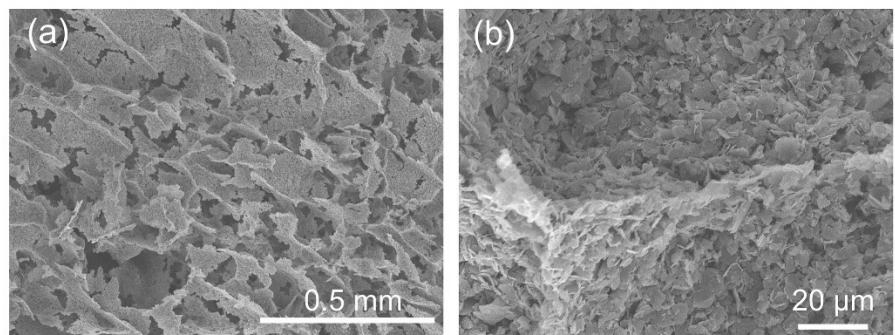


Figure S5. SEM images of CMC/BN aerogel.

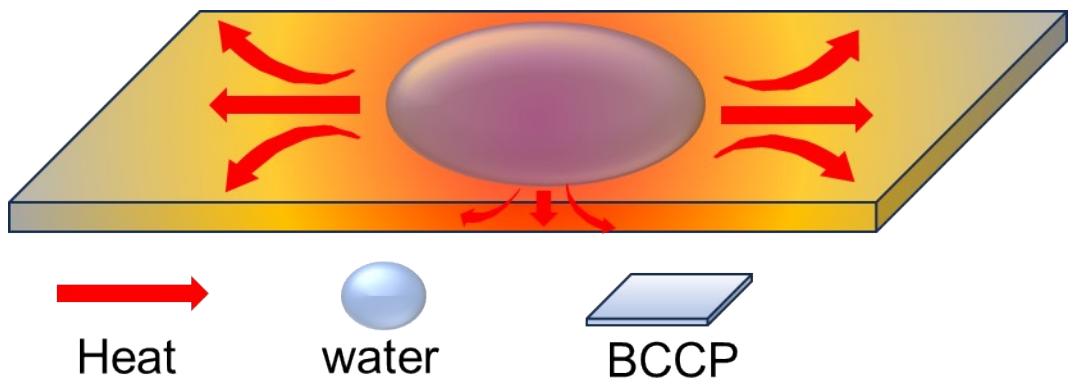


Figure S6. the diagram of heat dissipation of the water with composites.

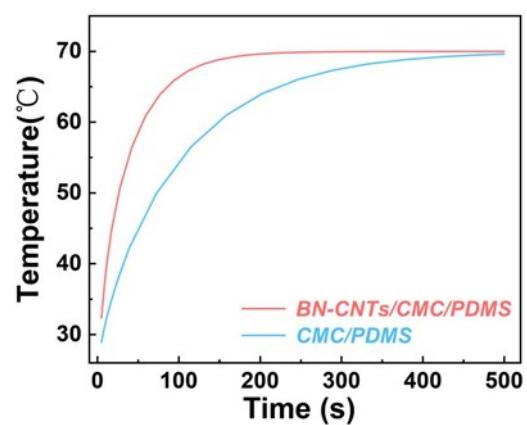


Figure S7. the change of surface temperature with the heating time.

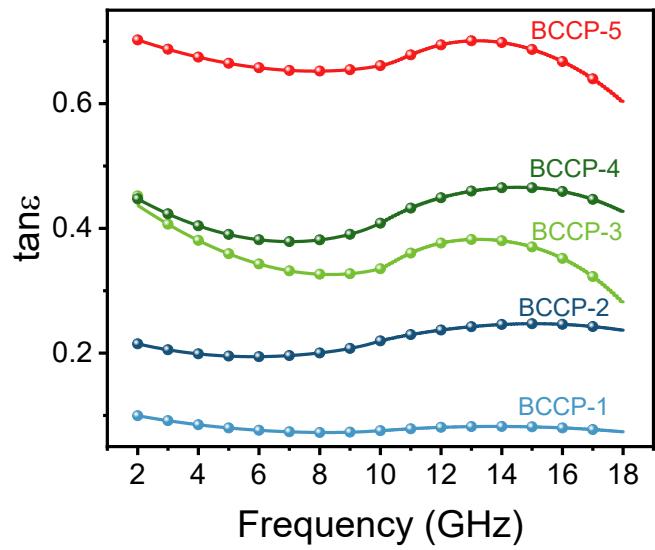


Figure S8. $\tan \epsilon$ of BCCP composites.

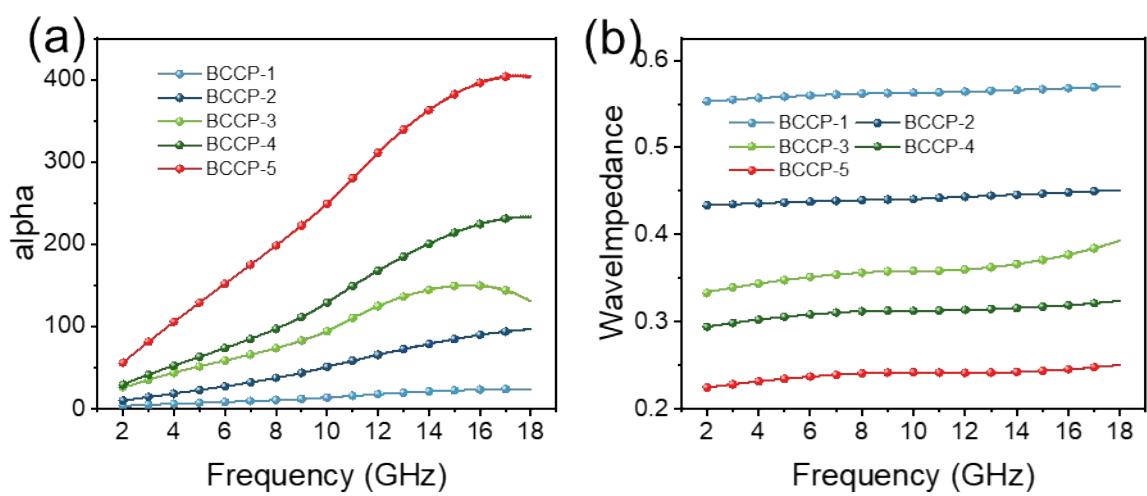


Fig. S9. Alpha and wave impedance of BCCP composites.

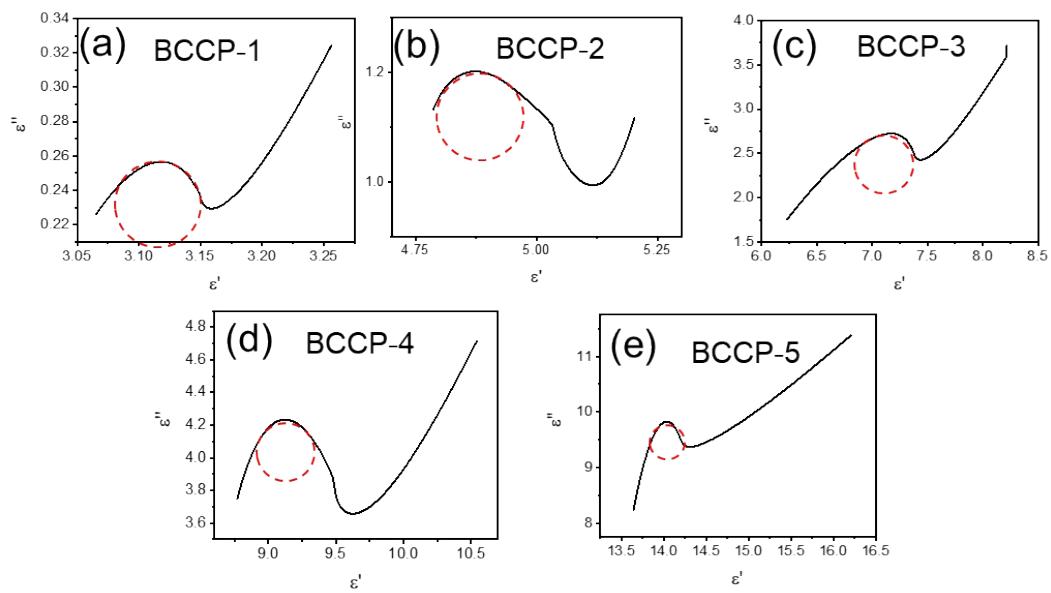


Fig. S10. Typical Cole-Cole semicircles (ε' versus ε'') of BCCP composites.

Table S1. Thermal conductivity of BCCP composites.

Sample	Thermal conductivity (W·m ⁻¹ ·K ⁻¹)
BCCP-1	3.56±0.26
BCCP-2	3.87±0.19
BCCP-3	4.26±0.15
BCCP-4	4.78±0.22
BCCP-5	5.07±0.18

Table S2 Comparison of wave absorption and thermal conduction of PCBC composites with those of relevant composites reported in the literature.

Filler	Matrix	Filler proportion (%)	Thermal conductivity ($\text{W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$)	RL_{\min} (dB)	$\text{R}_L < 10 \text{ dB}$		
					Thickness (mm)	EAB (GHz)	
CNF@C-Ni	Epoxy	5	0.5	-49.77	2.2	5.44	¹
BN-MXene	PDMS	15	2.03	-49.37	2.0	5.8	²
SiC@BN	Epoxy	16.69	2.21	-21.5	3.0	2.8	³
BCN@LDH	EP	10	0.49	-55.75	2.1	6.43	⁴
BCN	Natural rubber	2.86	0.338	-54.24	1.4	4.16	⁵
CNF/Fe _x O _y	Wafers	30	3.22	-41.16	3.3	10.72	⁶
SG@SiC	Silicone rubber	73.3	3.28	-31.9	2	2.9	⁷
GN/PPy/Al ₂ O ₃	Silicone rubber	50	4.649	-14.78	2	6.48	⁸
Ni@C	Natural rubber	-	0.2	-54.8	1.9	7.8	⁹
BNNS@Fe ₃ O ₄	-	100	1.75	-45.31	2	2.5	¹⁰
Ni@GNP	PMMA	30	1.29	-30	2	1.4	¹¹
NPC@MoSe ₂	PDMS	15	0.97	-51.6	2.6	7.1	¹²
MDCF@BN	EP	25	0.99	-52.77	3	5.6	¹³
CNT@NiO	natural rubber	5	1.05	-47.1	1.5	4.24	¹⁴
Mxene/Co	PVDF	12	1.36	-45.6	4	-	¹⁵
TiO ₂ @C–Ni/CNTs	natural rubber	3	0.25	-32.3	1.8	5.5	¹⁶
BCCP-4	PDMS	8	3.56	-63.34	1.7	4.81	This work

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