# **Electronic Supplementary Information (ESI)**

## Anionic Exchange Membrane Water Electrolysis over Superparamagnetic Ferrites

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### TABLES

**Table S1.** Average particle diameters, calculated lattice parameters, specific surface area and optical bandgap of the CoFe<sub>2</sub>O<sub>4</sub>, NiFe<sub>2</sub>O<sub>4</sub>, ZnFe<sub>2</sub>O<sub>4</sub>, and Zn<sub>0.2</sub>Mn<sub>0.2</sub>Ni<sub>0.2</sub>Co<sub>0.2</sub>Fe<sub>2.2</sub>O<sub>4</sub> ( $4A_{1/4}$ Fe<sub>2.2</sub>O<sub>4</sub>) catalysts synthesized by coprecipitation method followed by calcination and ball milling.

Sample	Mean crystallite size* (nm)	Calculated lattice parameters (a = b = c) (Å)*	Mean particle radius (nm)**	Specific surface area S <sub>BET</sub> (m²/g)***	Optical bandgap (eV)
CoFe <sub>2</sub> O <sub>4</sub>	34.0+	8.3416	$20\pm7$	65	1.48
	32.1•	8.3432•			
NiFe <sub>2</sub> O <sub>4</sub>	24.9+	8.3445	$26\pm 6$	42	1.58
	28.2•	8.3461•			
ZnFe <sub>2</sub> O <sub>4</sub>	20.9+	8.4437	$18 \pm 4$	54	1.70
	23.8•	8.4629•			
$4A_{1/4}$ Fe <sub>2.2</sub> O <sub>4</sub>	25.9+	8.3832	21 ± 5	84	1.51

\* Calculated from the collected XRD data (+Scherrer Equation/•Rietveld Refinement).

\*\* Estimated by the analysis of TEM images (Figure S3).

\*\*\* Estimated by N<sub>2</sub> physisorption.

**Table S2.** Summary of the refined Mössbauer parameters (centroid shift,  $\delta$ , quadrupole shift,  $\varepsilon$ , magnetic hyperfine field,  $B_{\rm hf}$ , magnetic hyperfine field distribution,  $\sigma$ , intensity, *I*) for spectra collected at 6 K from CoFe<sub>2</sub>O<sub>4</sub>, NiFe<sub>2</sub>O<sub>4</sub>, ZnFe<sub>2</sub>O<sub>4</sub>, and Zn<sub>0.2</sub>Mn<sub>0.2</sub>Ni<sub>0.2</sub>Co<sub>0.2</sub>Fe<sub>2.2</sub>O<sub>4</sub> catalysts synthesized by coprecipitation method followed by calcination and ball milling. Estimated errors are  $\pm 3\%$  in *I*,  $\pm 0.005$  mm/s in  $\delta$  and  $\varepsilon$ , and  $\pm 0.2$  T in  $B_{\rm hf}$  and  $\sigma$ .

	Parameters	CoFe <sub>2</sub> O <sub>4</sub>	NiFe <sub>2</sub> O <sub>4</sub>	ZnFe <sub>2</sub> O <sub>4</sub>	Zn <sub>0.2</sub> Mn <sub>0.2</sub> Ni <sub>0.2</sub> Co <sub>0.2</sub> Fe <sub>2.2</sub> O <sub>4</sub>
	$\delta_{\rm l} \ ({\rm mm/s})$	0.524	0.468	0.452	0.627
	$B_{\rm hfl}$ (T)	52.2	54.9	50.9	52.3
$Q_1$	$\sigma_{l}(T)$	1.8	0.7	1.2	1.0
	$\varepsilon_1 \text{ (mm/s)}$	0.007	-0.004	0.069	0.042
	<i>I</i> <sub>1</sub> (%)	46	46	48	23
	$\delta_2 \text{ (mm/s)}$	0.328	0.361	0.442	0.337
	$B_{\rm hf2}$ (T)	50.7	50.7	50.1	51.5
$Q_2$	$\sigma_2(T)$	1.2	0.8	1.2	1.0
	$\mathcal{E}_2 \text{ (mm/s)}$	0.004	0.052	-0.127	-0.003
	I <sub>2</sub> (%)	32	39	32	45
	$\delta_3 (\text{mm/s})$	0.428	0.367	0.452	0.447
	$B_{\rm hf3}$ (T)	48.7	50.2	46.3	49.8
$Q_3$	$\sigma_3(T)$	3.3	0.7	3.6	2.8
	$\epsilon_3 \text{ (mm/s)}$	-0.026	-0.138	-0.006	-0.030
	I <sub>3</sub> (%)	22	15	20	32
	Absorption (%)	8.0	7.3	6.9	7.4

**Table S3.** Cation distributions within the spinel crystal structure estimated based on the 6 K Mössbauer data collected from the  $CoFe_2O_4$ ,  $NiFe_2O_4$ ,  $ZnFe_2O_4$ , and  $Zn_{0.2}Mn_{0.2}Ni_{0.2}Co_{0.2}Fe_{2.2}O_4$  catalysts synthesized by coprecipitation method followed by calcination and ball milling. A = tetrahedral sites, B = octahedral sites of the  $AB_2O_4$  spinel structure.

Compound	Distributions
CoFe <sub>2</sub> O <sub>4</sub>	$[Co_{0.36}Fe_{0.64}]^{A}\{Co_{0.64}Fe_{1.36}\}^{B}O_{4}$
NiFe <sub>2</sub> O <sub>4</sub>	$[Fe]^{A}{NiFe}^{B}O_{4}$
ZnFe <sub>2</sub> O <sub>4</sub>	$[Zn_{0.36}Fe_{0.64}]^{A}\{Zn_{0.64}Fe_{1.36}\}^{B}O_{4}$
Zn <sub>0.2</sub> Mn <sub>0.2</sub> Ni <sub>0.2</sub> Co <sub>0.2</sub> Fe <sub>2.2</sub> O <sub>4</sub>	$[M_{0.10}Fe_{0.90}]^{A} \{M_{0.90}Fe_{1.10}\}^{B}O_{4}$

**Table S4.** Magnetic properties of the  $CoFe_2O_4$ ,  $NiFe_2O_4$ ,  $ZnFe_2O_4$ , and  $Zn_{0.2}Mn_{0.2}Ni_{0.2}Co_{0.2}Fe_{2.2}O_4$  catalysts synthesized by coprecipitation method followed by calcination and ball milling.

Catalyst	M <sub>s</sub> (emu/g <sub>sample</sub> )	<i>M</i> <sub>r</sub> (emu/g <sub>sample</sub> )	Hc (Oe)
CoFe <sub>2</sub> O <sub>4</sub>	38.5	15.9	600
NiFe <sub>2</sub> O <sub>4</sub>	44.2	5.7	72
ZnFe <sub>2</sub> O <sub>4</sub>	15.0	0.0	0
Zn <sub>0.2</sub> Mn <sub>0.2</sub> Ni <sub>0.2</sub> Co <sub>0.2</sub> Fe <sub>2.2</sub> O <sub>4</sub>	50.3	3.7	40

**Table S5.** ICP-OES analysis of detailing elemental composition of the catalysts explored in this work.

Element	Experimental Mole Fraction to Fe	Theoretical Mole Fraction to Fe	% diff.
Co (CoFe <sub>2</sub> O <sub>4</sub> )	2.00	2.00	0.00
Ni (NiFe <sub>2</sub> O <sub>4</sub> )	1.99	2.00	-0.08
Zn (ZnFe <sub>2</sub> O <sub>4</sub> )	2.04	2.00	+2.39
	Zn <sub>0.2</sub> Mn <sub>0.2</sub> Ni <sub>0.2</sub> Co <sub>0.2</sub>	Fe <sub>2.2</sub> O <sub>4</sub>	
Zn	0.095	0.091	+4.29
Mn	0.103	0.091	+13.66
Ni	0.100	0.091	+10.27
Со	0.099	0.091	+9.74

Catalyst	Support	Overpotential η <sub>10</sub> @ 10mA/cm <sup>2</sup>	Tafel slope (mV/dec)	Electrolyte	Ref.
H <sub>2</sub> -treated NiFe <sub>2</sub> O <sub>4</sub>	Glassy	389 mV	64	1 M KOH	[1]
	carbon				
CoFe <sub>2</sub> O <sub>4</sub> with carbon spheres	Glassy	390 mV	58	1 M KOH	[2]
	carbon				
Dual-phase MnCo <sub>2</sub> O <sub>4</sub>	Glassy	327 mV	79	1 M KOH	[3]
	carbon				
Mesoporous NiFe <sub>2</sub> O <sub>4</sub> nanorods	Glassy	342 mV	44	1 M KOH	[4]
	carbon				
Mesoporous NiFe <sub>2</sub> O <sub>4</sub>	Glassy	410 mV	50	1 M KOH	[5]
	carbon				
ZnFe <sub>2</sub> O <sub>4</sub> NPs on N-doped	Nickel	240 mV	64	1 M KOH	[6]
graphene	foam				
MnFe <sub>2</sub> O <sub>4</sub>	Glassy	600 mV	116	0.1 M KOH	[7]
	carbon				
CuFe <sub>2</sub> O <sub>4</sub> , NiFe <sub>2</sub> O <sub>4</sub> , CoFe <sub>2</sub> O <sub>4</sub>	Nickel	369 mV (CuFe <sub>2</sub> O <sub>4</sub> )	76 (CuFe <sub>2</sub> O <sub>4</sub> )	1 M KOH	[8]
	foam	386 mV (NiFe <sub>2</sub> O <sub>4</sub> )	86 (NiFe <sub>2</sub> O <sub>4</sub> )		
		448 mV (CoFe <sub>2</sub> O <sub>4</sub> )	148 (CoFe <sub>2</sub> O <sub>4</sub> )		
Mesoporous nanostructured	Glassy	412 mV (CoFe <sub>2</sub> O <sub>4</sub> )	_	0.1 M KOH	[9]
$AFe_2O_4$ ( $A = Co, Mn, Ni$ )	carbon	412 mV (NiFe <sub>2</sub> O <sub>4</sub> )			
		582 mV (MnFe <sub>2</sub> O <sub>4</sub> )			
CoFe <sub>2</sub> O <sub>4</sub> nanocubes on a N-	Glassy	320 mV	56	1 M KOH	[10]
doped graphene oxide	carbon				
Co <sub>0.8</sub> Zn <sub>0.2</sub> Fe <sub>2</sub> O <sub>4</sub>	Ni foam	317 mV	43	1 M KOH	[11]
Ni <sub>0.5</sub> Cu <sub>0.5</sub> Fe <sub>2</sub> O <sub>4</sub> anchored at S-	316 SSL	250 mV	45	1 M KOH	[12]
doped <i>g</i> -C <sub>3</sub> N <sub>4</sub>	mesh				
Co <sub>0.5</sub> Ni <sub>0.5</sub> Fe <sub>2</sub> O <sub>4</sub>	Ni foam	210 mV	35	1 M KOH	[13]
(NiCoMnCu) <sub>1</sub> Fe <sub>1</sub> Co <sub>1</sub> O <sub>4</sub>	Carbon	460 mV	_	1 M KOH	[14]
	paper				
(CoFeNiCrMn) <sub>3</sub> O <sub>4</sub>	FTO	307 mV	30	1 M KOH	[15]
(Co <sub>0.2</sub> Mn <sub>0.2</sub> Ni <sub>0.2</sub> Fe <sub>0.2</sub> Zn <sub>0.2</sub> )Fe <sub>2</sub> O <sub>4</sub>	CFP	326 mV	54	1 M KOH	[16]
(CoNiMnZnFe) <sub>3</sub> O <sub>3.2</sub>	CFP	336 mV	48	1 M KOH	[17]
CoFe <sub>2</sub> O <sub>4</sub>	Glassy	484 mV	103	1 M KOH	This
	carbon				work
NiFe <sub>2</sub> O <sub>4</sub>	Glassy	455 mV	108	1 M KOH	This
	carbon				work
Zn <sub>0.2</sub> Mn <sub>0.2</sub> Ni <sub>0.2</sub> Co <sub>0.2</sub> Fe <sub>2.2</sub> O <sub>4</sub>	Glassy	432 mV	86	1 M KOH	This
	carbon				work

**Table S6.** Comparison of alkaline OER activity for several reported simple, as well as highentropy spinels and metal oxides.

Anode material	Membrane/ Supporting electrolyte	Loading Cell size	Performance @~2V	Electrolyte	Stabilit y test	Ref
NiFe <sub>2</sub> O <sub>4</sub>	Fumasep® FAA3-50	$\begin{array}{c} 3 \text{ mg/cm}^2 \\ 5 \text{ cm}^2 \end{array}$	2.7 A/cm <sup>2</sup> 60 °C	1 M KOH	70 h	[18]
NiFeO <sub>x</sub>	SustainionTM X37-50	2.5 mg/cm <sup>2</sup> 5 cm <sup>2</sup>	0.650 A/cm <sup>2</sup> 50 °C	1 M KOH	500 h	[19]
NiFe <sub>2</sub> O <sub>4</sub>	Fumasep® FAA3-50	$\begin{array}{c} 3  mg/cm^2 \\ 5 \ cm^2 \end{array}$	2.5 A/cm <sup>2</sup> 60 °C	1 M KOH	100 h	[20]
NiMn <sub>2</sub> O <sub>4</sub>	Fumasep® FAA3-50	3 mg/cm <sup>2</sup> 5 cm <sup>2</sup>	0.530 A/cm <sup>2</sup> 80 °C	1 M KOH	1000 h	[21]
Ce <sub>0.2</sub> MnFe <sub>1.8</sub> O <sub>4</sub>	Fumasep® FAA-3-PK- 130	3.5 mg/cm <sup>2</sup> 4 cm <sup>2</sup>	0.300 A/cm <sup>2</sup> (@ 1.8 V) 25 °C	1 M KOH	100 h	[22]
Ni <sub>0.75</sub> Fe <sub>2.25</sub> O <sub>4</sub>	X37-50 Grade T	4 mg/cm <sup>2</sup> 7.1 cm <sup>2</sup>	2.5 A/cm <sup>2</sup> (@1.9V) 45 °C	1 М КОН	21 h	[23]
NiFe-oxide	Fumasep® FAA3-50	5 cm <sup>2</sup>	3.25 A/cm <sup>2</sup> at 2.2 V 60°C	1 M KOH	100 h	[24]
NiCo <sub>2</sub> O <sub>4</sub> /CNF	Fumasep® FAA3-50	3 mg/cm <sup>2</sup>	0.303 A/cm <sup>2</sup> at 1.8 V 50°C	6 М КОН	-	[25]
Ni <sub>0.6</sub> Co <sub>0.2</sub> Fe <sub>0.2</sub>	Fumapem-3-PE-30	5 mg/cm <sup>2</sup> 25 cm <sup>2</sup>	2 A/cm <sup>2</sup> 50 °C	1 M KOH	50 h	[26]
$Zn_{0.2}Mn_{0.2}Ni_{0.2}Co_{0.2}Fe_{2.2}O_4$	Proprietary Hydrolite Membrane B 70 µm	3 mg/cm <sup>2</sup> 4 cm <sup>2</sup>	1.5 A/cm <sup>2</sup> 80 °C	1 M KOH	20 h	This work
NiFe <sub>2</sub> O <sub>4</sub>	Proprietary Hydrolite Membrane B 70 μm	$\frac{3 \text{ mg/cm}^2}{4 \text{ cm}^2}$	1.9 A/cm <sup>2</sup> 80 °C	1 M KOH	20 h	This work

 Table S7. Comparison of full-cell AEMEL performance of several spinels reported to date.

#### FIGURES



**Figure S1.** XRD patterns for  $CoFe_2O_4$  (ICDD no. 01-090-3471, cubic, *Fd*-3*m*), NiFe<sub>2</sub>O<sub>4</sub> (ICDD no. 01-078-3741, cubic, *Fd*-3*m*), ZnFe<sub>2</sub>O<sub>4</sub> (ICDD no. 04-008-5691, cubic, *Fd*-3*m*), and Zn<sub>0.2</sub>Mn<sub>0.2</sub>Ni<sub>0.2</sub>Co<sub>0.2</sub>Fe<sub>2.2</sub>O<sub>4</sub> catalysts synthesized by coprecipitation method followed by calcination and ball milling.



**Figure S2.** Room temperature Raman spectra for  $CoFe_2O_4$ ,  $NiFe_2O_4$ ,  $ZnFe_2O_4$ , and  $Zn_{0.2}Mn_{0.2}Ni_{0.2}Co_{0.2}Fe_{2.2}O_4$  catalysts synthesized by coprecipitation method followed by calcination and ball milling.



**Figure S3.** Histograms of particle-size distribution as determined from several TEM images of  $CoFe_2O_4$ ,  $NiFe_2O_4$ ,  $ZnFe_2O_4$ , and  $Zn_{0.2}Mn_{0.2}Ni_{0.2}Co_{0.2}Fe_{2.2}O_4$  catalysts synthesized by coprecipitation method followed by calcination and ball milling, n = 100. The curve shows a fit using the Gaussian distribution function. The mean particle size is indicated in the respective plot where the error is the standard deviation.



**Figure S4.** Representative SEM and SEM–EDX data of  $CoFe_2O_4$ ,  $NiFe_2O_4$ ,  $ZnFe_2O_4$ , and  $Zn_{0.2}Mn_{0.2}Ni_{0.2}Co_{0.2}Fe_{2.2}O_4$  catalysts synthesized by coprecipitation method followed by calcination and ball milling.



Figure S5. HAADF–STEM image and the corresponding EDX elemental mapping of  $CoFe_2O_4$  (top),  $NiFe_2O_4$  (middle), and  $ZnFe_2O_4$  (bottom) catalysts.



Figure S6. HAADF–STEM image and the corresponding EDX elemental mapping of the compositionally complex  $Zn_{0.2}Mn_{0.2}Ni_{0.2}Co_{0.2}Fe_{2.2}O_4$  ferrite catalyst.



**Figure S7.** XPS survey data for the key constituting elements of  $CoFe_2O_4$ ,  $NiFe_2O_4$ ,  $ZnFe_2O_4$ , and  $Zn_{0.2}Mn_{0.2}Ni_{0.2}Co_{0.2}Fe_{2.2}O_4$  catalysts synthesized by coprecipitation method followed by calcination and ball milling.



**Figure S8.** UV/Vis diffuse reflectance spectra of  $CoFe_2O_4$ ,  $NiFe_2O_4$ ,  $ZnFe_2O_4$ , and  $Zn_{0.2}Mn_{0.2}Ni_{0.2}Co_{0.2}Fe_{2.2}O_4$  catalysts synthesized by coprecipitation method followed by calcination and ball milling, together with the corresponding Tauc plots (inset) used for the determination of the optical band gap.

#### **COMPUTATIONAL STUDY ON SPINEL FERRITES**

#### **Computational method**

The study was performed by periodic DFT calculations using QUANTUM ESPRESSO 6.8 (QE) GPU-enabled version.<sup>[27]</sup> The DFT+U+J approach<sup>[28]</sup> was applied to account for the strong correlation among the electrons in the 3*d*-metals (U = 2.5 eV, J = 0.4 eV,  $U_{eff}$  = 2.5 eV) during the geometry optimization of the lattice parameters (atomic positions + cell). U<sub>eff</sub> follows the Dudarev et al formulation<sup>[28c]</sup>. All the calculations were carried out with spin polarization and by applying the collinear magnetic model (i.e., all atomic magnetic moments are aligned with the z-axis), unless specified. The exchange-correlation energy was calculated within the generalized gradient approximation using the optB86b functional.<sup>[29]</sup> The electron-ion interactions for the atoms were described by the Ultrasoft (US) method developed by Vanderbilt.<sup>[30]</sup> The US pseudopotentials used in this work were generated by using the ld1.xincluded in atomic package the Quantum **ESPRESSO** distribution (https://www.quantum-espresso.org/documentation/package-specific-documentation/). The pseudopotentials were recompiled for optB86b from Andrea Dal Corso's schemes (proposed for PBE and PBEsol) in pslibrary<sup>[31]</sup> (https://github.com/dalcorso/pslibrary.git). The kinetic energy cut-offs used in optimization were set to 60 Ry for wavefunction and 600 Ry for charge density and potential. A single point energy refinement of optimized structures was carried out for each of the most stable entries. The Monkhorst-Pack scheme was chosen for the integration in the reciprocal space.<sup>[32]</sup> The reciprocal space of all investigated structures was generally sampled with a 0.20 Å<sup>-1</sup>-spaced k-points grid for optimizations and energy refinements. The projectors for U on localized orbitals were based on Löwdin orthogonalized atomic wavefunctions orbitals ("ortho-atomic" option in QE). Marzari-Vanderbilt-Devita-Payne smearing<sup>[33]</sup> was used for all the calculations. The computational studies presented in this article are carried out at 0 K and under vacuum condition.

#### **Computational remarks**

The computational models were built based on the cation distribution data obtained from Mössbauer spectroscopy (see Table S3). The space groups are reported in Hermann–Mauguin symmetry symbols. CS and C indicate the Crystallographic System and the cubic symmetry, respectively. The cell parameters are indicated as a;b;c (in Å),  $\alpha;\beta;\gamma$  (in °) and the cell volume is in Å. Average M–O bond distances are reported in Å, where M is the *3d*-transition metal in

the octahedral ( $O_h$ ) or tetrahedral ( $T_d$ ) site. Magnetic orderings are labelled as: FM (ferromagnetic), AFM (antiferromagnetic), ferri (ferrimagnetic), NM (non-magnetic, non-spinpolarized calculation), while the types of conduction are indicated as M (metallic), HM (half metallic), S (semiconduction) and I (insulator). For all entries only the spin components of the magnetic moments ( $\mu$ , in  $\mu_B$ ) are reported.<sup>[34]</sup>

Pictures and surfaces are created using VESTA<sup>[35]</sup> program. Mn, Fe, Co, Ni, Zn, and O are colored in pink, brown, blue, silver, dark grey, and red, respectively. The isosurfaces in the density spin plots are shown at 0.004  $a_0^{-3}(a_0)$  is the Bohr radius). Density of states (DOS) are generated with Gnuplot v. 5.4<sup>[36]</sup> (http://www.gnuplot.info/).

### **Computational data tables**

# $CoFe_2O_4$ ([ $Co_{0.375}Fe_{0.625}$ ]<sup>A</sup>{ $Co_{0.625}Fe_{1.375}$ }<sup>B</sup>O<sub>4</sub>)

**Table S8.** Optimized computational data on <u>partially inverse</u> CoFe<sub>2</sub>O<sub>4</sub> bulk (T = 0 K). The most stable ground state is referred to as 0.00 eV. The experimental lattice parameters are a = b = c = 8.3416 Å, as reported in Table S1.

CS (C)	Magn. Struc. type	Δ <i>E</i> (eV)	Cell parameters (Å)	Cell volume (Å <sup>3</sup> )	Average M–O distance (Å)	Abs. Averag e Mag. Mom. ( μ <sub>B</sub>  )
	NM	37.01	a=8.06291; b=7.69179; c=8.08933; $\alpha$ =89.82°; $\beta$ =90.64°; $\gamma$ =89.93°	501.65	1.83 (Fe-O T <sub>d</sub> ) 1.92 (Fe-O O <sub>h</sub> ) 1.88 (Co-O T <sub>d</sub> ) 1.91 (Co-O O <sub>h</sub> )	-
	FM		No conve			
Fd-3m	Ferri1	0.00	a=8.40838; b=8.37131; c=8.36615; α=90.39°; β=89.85°; γ=90.00°	588.87	1.89 (Fe-O T <sub>d</sub> ) 2.03 (Fe-O O <sub>h</sub> ) 1.95 (Co-O T <sub>d</sub> ) 2.06 (Co-O O <sub>h</sub> )	4.0 (Fe) 2.5 (Co)
	Ferri2	2.98	a=8.42534; b=8.44037; c=8.42766; $\alpha$ =90.06°; $\beta$ =89.92°; $\gamma$ =89.93°	599.32	1.91 (Fe-O T <sub>d</sub> ) 2.03 (Fe-O O <sub>h</sub> ) 1.96 (Co-O T <sub>d</sub> ) 2.07 (Co-O O <sub>h</sub> )	4.1 (Fe) 2.5 (Co)



**Figure S9.** Optimized cell (right) and spin density plot (left) of ferrimagnetic (Ferri 1) bulk  $CoFe_2O_4$  partially inverse spinel (yellow = spin up, cyan = spin down).



**Figure S10.** Density of states (DOS) between -3 eV and 3 eV of ferrimagnetic (Ferri 1) bulk CoFe<sub>2</sub>O<sub>4</sub> partially inverse spinel.

# $NiFe_2O_4$ ([Fe]<sup>A</sup>{NiFe}<sup>B</sup>O<sub>4</sub>)

**Table S9.** Optimized computational data on <u>inverse spinel</u> NiFe<sub>2</sub>O<sub>4</sub> bulk (T = 0 K). The most stable ground state is referred to as 0.00 eV. The experimental lattice parameters are a = b = c = 8.3445 Å, as reported in Table S1.

CS (C)	Magn. Struc. type	Δ <i>E</i> (eV)	Cell parameters (Å)	Cell volume (Å <sup>3</sup> )	Average M–O distance (Å)	Abs. Averag e Mag. Mom. ( μ <sub>B</sub>  )		
	NM	39.70	a=8.06116; b=7.81116; c=8.08496; α=89.70°; β=90.15; γ=89.89°	509.08	1.81 (Fe-O T <sub>d</sub> ) 1.93 (Fe-O O <sub>h</sub> ) 1.96 (Ni-O O <sub>h</sub> )	-		
	FM		No conver	gence	gence			
Fd-3m	AFM	1.17	a=8.34447; b=8.32816; c=8.35281; α=90.36°; β=90.15°; γ=90.46°	580.44	1.90 (Fe-O T <sub>d</sub> )           2.02 (Fe-O O <sub>h</sub> )           2.05 (Ni-O O <sub>h</sub> )	4.0 (Fe) 1.6 (Ni)		
	Ferri	0.00	a=8.33734; b=8.30763; c=8.34308; α=90.00°; β=90.08°; γ=90.06°	577.87	1.89 (Fe-O T <sub>d</sub> ) 2.02 (Fe-O O <sub>h</sub> ) 2.04 (Ni-O O <sub>h</sub> )	4.0 (Fe) 1.5 (Ni)		



**Figure S11.** Optimized cell (right) and spin density plot (left) of ferrimagnetic bulk  $NiFe_2O_4$  inverse spinel (yellow = spin up, cyan = spin down).



**Figure S12.** Density of states (DOS) between -3 eV and 3 eV of ferrimagnetic bulk NiFe<sub>2</sub>O<sub>4</sub> inverse spinel.

### NiFe<sub>2-x</sub>O<sub>4</sub> (x = 0.125) ([Fe]<sup>A</sup>{NiFe<sub>0.875</sub>}<sup>B</sup>O<sub>4</sub>)

**Table S10.** Optimized computational data on <u>inverse spinel</u> NiFe<sub>2-x</sub>O<sub>4</sub> (x = 0.125) bulk (T = 0 K). The most stable ground state is referred to as 0.00 eV. The experimental lattice parameters are a = b = c = 8.3445 Å, as reported in Table S1.

CS (C)	Magn. Struc. type	Δ <i>E</i> (eV)	Cell parameters (Å)	Cell volume (Å <sup>3</sup> )	Average M–O distance (Å)	Abs. Averag e Mag. Mom. ( µ <sub>B</sub>  )
	NM	34.54	a=8.03199; b=7.80771; c=8.06645; α=90.06°; β=90.50°; γ=89.80°	505.84	1.80 (Fe-O T <sub>d</sub> ) 1.91 (Fe-O O <sub>h</sub> ) 1.97 (Ni-O O <sub>h</sub> )	-
Fd-3m	FM		No conver			
	Ferri	0.00	a=8.24776; b=8.33943; c=8.30065; α=89.82°; β=89.91°; γ=90.33°	570.92	1.88 (Fe-O T <sub>d</sub> ) 2.05 (Fe-O O <sub>h</sub> ) 1.99 (Ni-O O <sub>h</sub> )	4.0 (Fe) 1.2 (Ni)



**Figure S13.** Optimized cell (right) and spin density plot (left) of ferrimagnetic bulk  $NiFe_{2-x}O_4$  (x = 0.125) inverse spinel (yellow = spin up, cyan = spin down).



**Figure S14.** Density of states (DOS) between -3 eV and 3 eV of ferrimagnetic bulk NiFe<sub>2-x</sub>O<sub>4</sub> (x = 0.125) inverse spinel (cyan = spin up, red = spin down).

# ZnFe<sub>2</sub>O<sub>4</sub> ([Zn<sub>0.375</sub>Fe<sub>0.625</sub>]<sup>A</sup>{Zn<sub>0.625</sub>Fe<sub>1.375</sub>}<sup>B</sup>O<sub>4</sub>)

**Table S11.** Optimized computational data on <u>partially inverse</u>  $ZnFe_2O_4$  bulk (T = 0 K). The most stable ground state is referred to as 0.00 eV. The experimental lattice parameters are a = b = c = 8.4437 Å, as reported in Table S1.

CS (C)	Magn. Struc. type	Δ <i>E</i> (eV)	Cell parameters (Å)	Cell volume (Å <sup>3</sup> )	Average M–O distance (Å)	Abs. Average Mag. Mom. ( µ <sub>B</sub>  )
	NM	33.18	a=8.17364; b=8.07584; c=7.99209; α=90.15°; β=90.48°; γ=90.70°	527.49	1.81 (Fe-O T <sub>d</sub> ) 1.94 (Fe-O O <sub>h</sub> )	-
Fd-3m	FM	4.15	a=8.46152; b=8.45668; c=8.45897; α=90.10°; β=90.03°; γ=89.94°	605.29	1.91 (Fe-O T <sub>d</sub> ) 2.04 (Fe-O O <sub>h</sub> )	4.1 (Fe)
ru-siii	AFM	1.46	a=8.42173; b=8.43019; c=8.42671; α=89.97°; β=90.05°; γ=89.96°	598.27	1.90 (Fe-O T <sub>d</sub> ) 2.04 (Fe-O O <sub>h</sub> )	4.0 (Fe)
	Ferri	0.00	a=8.41588; b=8.41537; c=8.41910; α=90.06°; β=90.04°; γ=90.02°	596.26	1.89 (Fe-O T <sub>d</sub> ) 2.04 (Fe-O O <sub>h</sub> )	4.0 (Fe)



**Figure S15.** Optimized cell (right) and spin density plot (left) of ferrimagnetic bulk  $ZnFe_2O_4$  partially inverse spinel (yellow = spin up, cyan = spin down).



**Figure S16.** Density of states (DOS) between -3 eV and 3 eV of ferrimagnetic bulk  $\text{ZnFe}_2\text{O}_4$  partially inverse spinel.

### $Zn_{0.2}Mn_{0.2}Ni_{0.2}Co_{0.2}Fe_{2.2}O_4$ ([ $M_{0.125}Fe_{0.875}$ ]<sup>A</sup>{ $M_{0.750}Fe_{1.250}$ }<sup>B</sup>O<sub>4</sub>)

Two models are built based also on the high-resolution XPS data shown in Figure 4 of the main text.

**Table S12.** Optimized computational data on <u>partially inverse</u>  $Zn_{0.2}Mn_{0.2}Ni_{0.2}Co_{0.2}Fe_{2.2}O_4$  bulk (T = 0 K). The most stable ground state is referred to as 0.00 eV. Some authors reported that the inclusion of  $Zn^{2+}$  and  $Ni^{2+}$  is difficult in this type of spinel.<sup>[38]</sup> This was considered for the building of the computational models. The experimental lattice parameters are a=b=c=8.3832 Å as reported in Table S1.

CS (C)	Magn. Struc. type	Δ <i>E</i> (eV)	Cell parameters (Å)	Cell volume (Å <sup>3</sup> )	Average M–O distance (Å)	Abs. Average Mag. Mom. ( µ <sub>B</sub>  )
	NM FM	42.51	a=8.03986; b=7.98983; c=7.91408; α=89.63°; β=89.04°; γ=89.63° No conv	508.29 /ergence	1.95 (Mn-O O <sub>h</sub> ) 1.83 (Fe-O T <sub>d</sub> ) 1.93 (Fe-O O <sub>h</sub> ) 1.91 (Co-O O <sub>h</sub> ) 1.95 (Ni-O O <sub>h</sub> )	-
ra-sm	AFM	Not possible				
	Ferri	0.00	a=8.39186; b=8.41341; c=8.39763; α=90.04°; β=90.38°; γ=90.16°	592.87	2.11 (Mn-O O <sub>h</sub> ) 1.89 (Fe-O T <sub>d</sub> ) 2.03 (Fe-O O <sub>h</sub> ) 2.07 (Co-O O <sub>h</sub> ) 2.06 (Ni-O O <sub>h</sub> )	4.5 (Mn) 4.0 (Fe) 2.6 (Co) 1.6 (Ni)

### Model a: $[Zn_{0.125}Fe_{0.875}]^{A} \{M_{0.750}Fe_{1.250}\}^{B}O_{4}$ (M= Co,Ni, Mn)



**Figure S17.** Optimized cell (right) and spin density plot (left) of <u>model a</u> ferrimagnetic bulk  $Zn_{0.2}Mn_{0.2}Ni_{0.2}Co_{0.2}Fe_{2.2}O_4$  partially inverse spinel (yellow = spin up, cyan = spin down).



Figure S18. Density of states (DOS) between -3 eV and 3 eV of model a ferrimagnetic bulk  $Zn_{0.2}Mn_{0.2}Ni_{0.2}Co_{0.2}Fe_{2.2}O_4$  partially inverse spinel.

# Model b: $[Co_{0.125}Fe_{0.875}]^{A} \{M_{0.750}Fe_{1.250}\}^{B}O_{4} (M = Co, Ni, Mn, Zn)$

**Table S13.** Optimized computational data on <u>partially inverse</u>  $Zn_{0.2}Mn_{0.2}Ni_{0.2}Co_{0.2}Fe_{2.2}O_4$  bulk (T = 0 K). The most stable ground state is referred to as 0.00 eV.

CS (C)	Magn. Struc. type	Δ <i>E</i> (eV)	Cell parameters (Å)	Cell vol. (Å <sup>3</sup> )	Average M–O distance (Å)	Abs. Averag e Mag. Mom. ( μ <sub>B</sub>  )		
Fd-3m	NM	43.37	a=7.87034; b=8.09461; c=7.96987; α=90.21°; β=89.35°; γ=89.40°	507.67	1.94 (Mn-O O <sub>h</sub> ) 1.83 (Fe-O T <sub>d</sub> ) 1.92 (Fe-O O <sub>h</sub> ) 1.86 (Co-O T <sub>d</sub> ) 1.92 (Co-O O <sub>h</sub> ) 1.94 (Ni-O O <sub>h</sub> )	-		
	FM	No convergence						
	AFM	Not possible						
	Ferri 1	0.29	a=8.40296; b=8.41844; c=8.40276; α=90.26°; β=90.48°; γ=89.91°	594.38	2.12 (Mn-O O <sub>h</sub> ) 1.89 (Fe-O T <sub>d</sub> ) 2.04 (Fe-O O <sub>h</sub> ) 1.97 (Co-O T <sub>d</sub> ) 2.08 (Co-O O <sub>h</sub> ) 2.06 (Ni-O O <sub>h</sub> )	4.5 (Mn) 4.0 (Fe) 2.6 (Co) 1.6 (Ni)		
	Ferri 2	0.00	a=8.39750; b=8.41351; c=8.39746; α=90.26°; β=90.48°; γ=89.91°	593.27	2.12 (Mn-O O <sub>h</sub> ) 1.89 (Fe-O T <sub>d</sub> ) 2.06 (Fe-O O <sub>h</sub> ) 1.95 (Co-O T <sub>d</sub> ) 2.08 (Co-O O <sub>h</sub> ) 2.06 (Ni-O O <sub>h</sub> )	4.5 (Mn) 4.0 (Fe) 2.6 (Co) 1.6 (Ni)		



**Figure S19.** Optimized supercell (right) and spin density plot (left) of <u>model b</u> ferrimagnetic bulk  $Zn_{0.2}Mn_{0.2}Ni_{0.2}Co_{0.2}Fe_{2.2}O_4$  partially inverse spinel (yellow = spin up, cyan = spin down).





**Figure S20.** Density of states (DOS) between -3 eV and 3 eV of <u>model b</u> ferrimagnetic bulk  $Zn_{0.2}Mn_{0.2}Ni_{0.2}Co_{0.2}Fe_{2.2}O_4$  partially inverse spinel.

**Table S14.** Calculated minimum band gaps for the spinels under study ( $E_g$  in eV). NR = data not been reported in literature.

System	Calc. minimum band gaps (Eg, eV) (this work)	Exp. band gaps (Eg, eV) (this work)	Reported calculated band gaps (Eg, eV)
NiFe <sub>2</sub> O <sub>4</sub> (inverse)	1.55 (spin ↑)⁄ 1.14 (spin ↓)	1.58	$\begin{array}{c} 1.56 \; (\text{spin})/\; 2.26 \; (\text{spin} \uparrow) \; \text{inverse} \\ \text{spinel} \; (\text{mBJLDA potential});^{[39]} \\ 1.6 \; (\text{spin})/\; 1.9 \; (\text{spin} \uparrow) \\ (\text{LSDA+U}, \text{U for Fe/Ni= 4.5/4.0} \\ \; \text{eV});^{[40]} \\ 1.10 \; (\text{GGA+U}, \text{U= 3 eV});^{[41]} \\ 2.2 \; (\text{spin})/\; 1.6 \; (\text{spin} \uparrow) \; \text{inv. spinel} \\ (\text{PBE+U}, \text{U}_{\text{Ni}}=\! 6 \; \text{eV}, \text{U}_{\text{Fe}}\!=\! 4.5 \; \text{eV})^{[42]} \end{array}$
NiFe <sub>2-x</sub> O <sub>4</sub> (x= $0.125$ ) (inverse)	0.37 (spin ↑)/ 0.73 (spin ↓)	1.58	N.R.
CoFe <sub>2</sub> O <sub>4</sub> (partially Inverse)	0.66 (spin ↑)/ 0.49 (spin ↓)	1.48	$\begin{array}{c} 0.63 \ (LMTO+LSDA+U, U=4eV);^{[43]} \\ 1.8 \ (spin \uparrow)/ \ 0.9 \ (spin \downarrow) \\ (LSDA+U, U \ Fe/Co=4.5/4.0 \ eV);^{[44]} \\ 0.09 \ (Co)_{Td}(Fe_2)_{Oh}O_4 \ (normal \ spinel);^{[45]} \\ 0.08, \ 0.00 \ for \ two \ possible \ Co \ ions \ distribution \ of \\ (Co_{0.75}Fe_{0.25})_{Td}(Co_{0.25}Fe_{1.75})_{Oh}O_4;^{[45]} \\ 0.16, \ 0.24, \ 0.00 \ for \ three \ possible \ Co \ ions \ distribution \ of \\ (Co_{0.5}Fe_{0.5})_{Td}(Co_{0.5}Fe_{1.5})_{Oh}O_4;^{[45]} \\ 0.30, \ 0.00, \ 0.00 \ for \ three \ possible \ Co \ ions \ distribution \ of \\ (Co_{0.25}Fe_{0.5})_{Td}(Co_{0.75}Fe_{1.25})_{Oh}O_4;^{[45]} \\ 0.30, \ 0.00, \ 0.00 \ for \ three \ possible \ Co \ ions \ distribution \ of \\ (Co_{0.25}Fe_{0.75})_{Td}(Co_{0.75}Fe_{1.25})_{Oh}O_4;^{[45]} \\ 0.72 \ (Fe)_{Td}(CoFe)_{Oh}O_4 \ (inv. \ spinel)^{[45]} \\ (PBE+U+J, \ for \ Fe \ U=4.22 \ and \ J=0.80 \ eV \ and \ for \ Co \ U=4.08 \ and \ J=0.79 \ eV)^{[45]} \end{array}$
ZnFe <sub>2</sub> O <sub>4</sub> (partially Inverse)	1.46 (spin ↑)/ 1.42 (spin ↓)	1.70	3.21 normal spinel (B3LYP); <sup>[46]</sup> 4.06 normal spinel (PBE0); <sup>[46]</sup> 3.31 normal spinel (PBE0); <sup>[47]</sup> 2.21 normal spinel (PBE+U, U= 5.25 eV); <sup>[47]</sup> 2.89 normal spinel (PBE+U/eV/cvGW/BSE, U=1eV); <sup>[48]</sup> 3.83 normal spinel (PBE+U/ eV/cvGW/BSE, U=3eV) <sup>[48]</sup>
Zn <sub>0.2</sub> Mn <sub>0.2</sub> Ni <sub>0.2</sub> Co <sub>0.2</sub> Fe <sub>2.2</sub> O <sub>4</sub> (partially Inverse)	Model a : 1.19 (spin ↑)/ 0.30 (spin ↓) Model b : 1.16 (spin ↑)/ 0.34 (spin ↓)	1.51	NR

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