

## Supporting Information

# Emergence of the novel magnetic properties in ternary iron nitrides toward spintronics: first-principles calculations

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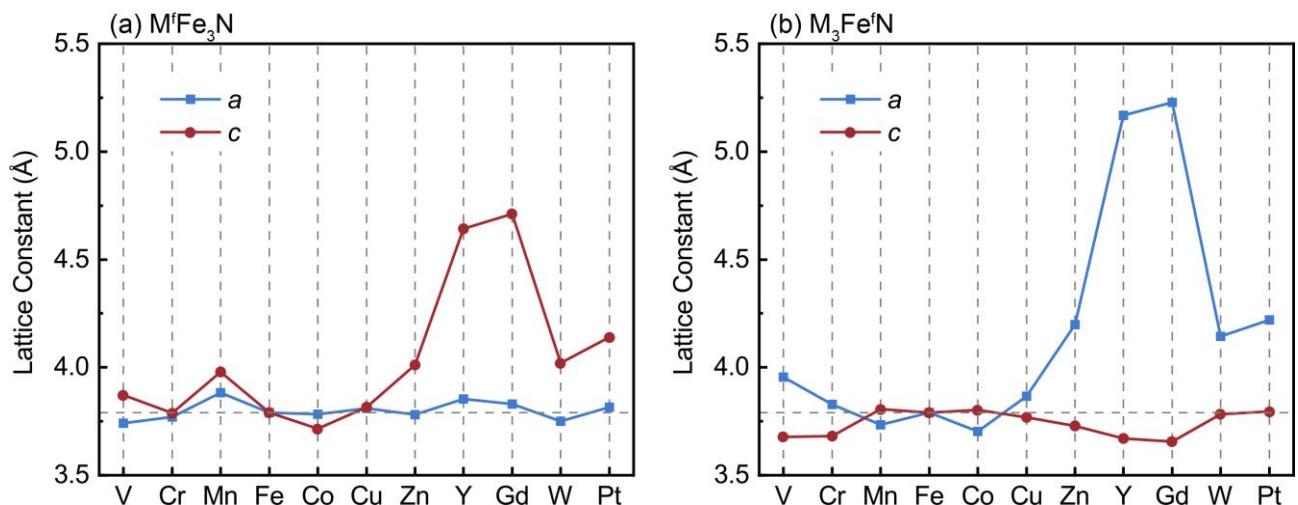
† Electronic supplementary information (ESI) available.

## S1. Valence electron configurations and $U$ and $J$ values of substitution atoms

**Table S1** The valence-electron configurations of substitution atoms and the values of  $U$  and  $J$  used for the Y, Gd, W, and Pt atoms.

Atoms	Valence-electron	$U$ (ev)	$J$ (ev)
V	$4s^23d^3$	-	-
Cr	$4s^13d^5$	-	-
Mn	$4s^23d^5$	-	-
Fe	$4s^23d^6$	-	-
Co	$4s^23d^7$	-	-
Cu	$4s^13d^{10}$	-	-
Zn	$4s^23d^{10}$	-	-
Y	$5s^24d^1$	6.50	0
Gd	$4f^75d^1$	6.70	0
W	$4f^{14}5d^4$	3.93	0
Pt	$4f^{14}5d^9$	2.18	0

## S2. Lattice constants of $M^f\text{Fe}_3\text{N}$ and $M_3\text{Fe}^f\text{N}$ in the $a$ and $c$ axis



**Figure S1** The lattice constants of (a)  $M^f\text{Fe}_3\text{N}$  and (b)  $M_3\text{Fe}^f\text{N}$ , where the lattice constants of  $a$  and  $c$  are marked as blue and red point.

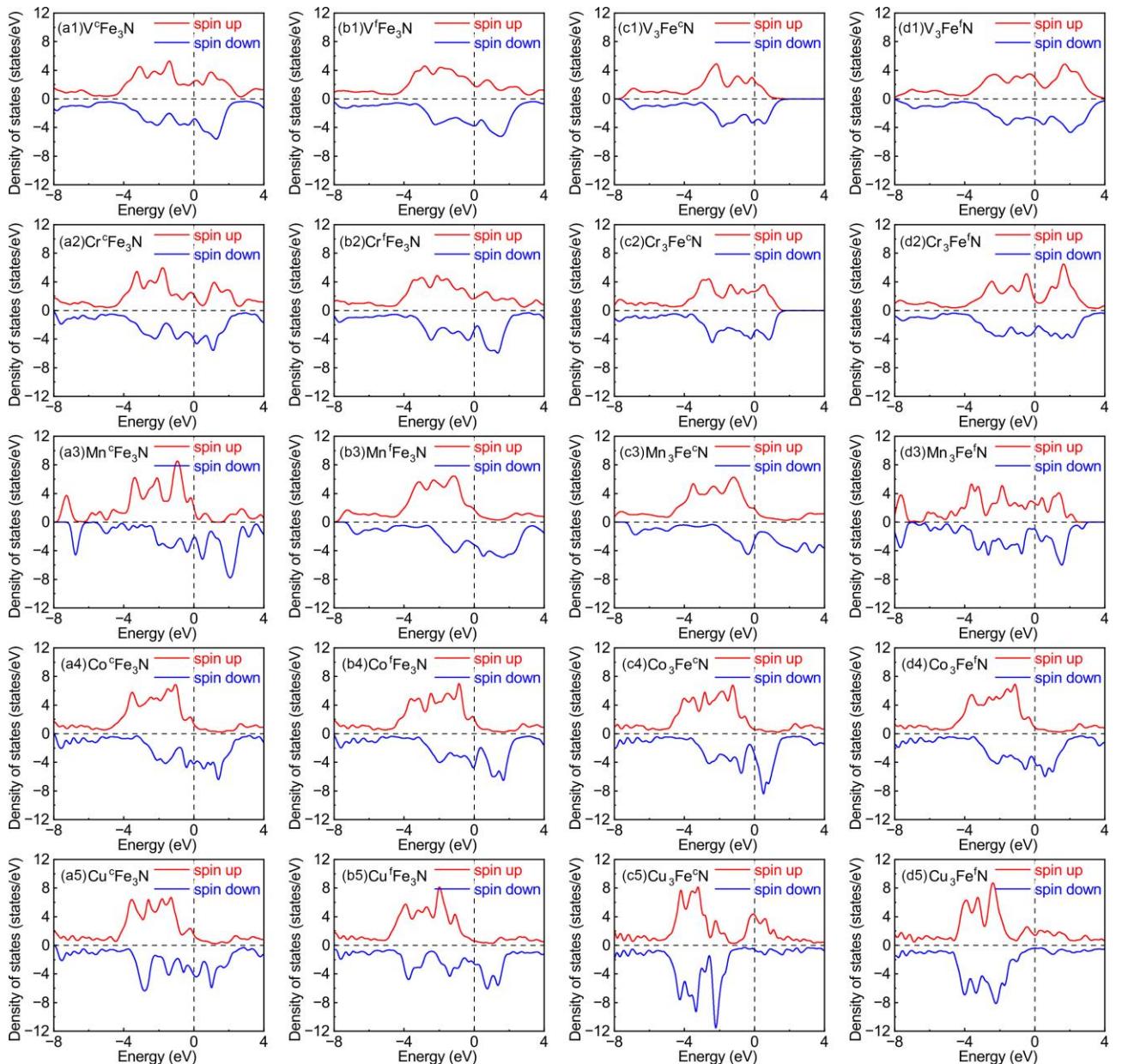
The  $a$ -axis of  $M^f\text{Fe}_3\text{N}$  exhibits minor expansion when  $M$  are Y and Gd elements because the substitution of  $\text{Fe}_{\text{IIIB}}$  sites not only change the  $c$ -axis lattice but also affect the bond lengths of the surrounding atoms. The change of bond lengths causes the  $a$ -axis expanding to accommodate the volume changes associated with the substitution elements. Compared to  $M^f\text{Fe}_3\text{N}$ , the local environment is significantly changed in  $M_3\text{Fe}^f\text{N}$ . Possible reason is the substitution of multiple Fe atoms lead to a rearrangement of the overall lattice structure, which causes the  $c$ -axis to contract and achieves structural stabilization.

### S3. Charge density difference of system Fe<sub>4</sub>N

**Table S2** Charge transfer situation of atoms at different sites of  $M_x\text{Fe}_{4-x}\text{N}$

	N (electrons /atom)	$M_{\text{IIAa}}$ (electrons /atom)	$M_{\text{IIBa}}$ (electrons /atom)	$M_{\text{IIBb}}$ (electrons /atom)	$M_{\text{I}}$ (electrons /atom)
Fe <sub>4</sub> N	1.33	-0.38	-0.38	-0.38	-0.18
Y <sup>c</sup> Fe <sub>3</sub> N	1.42	0.10	0.10	0.10	-1.71
Y <sub>3</sub> Fe <sup>f</sup> N	1.56	-1.19	-1.19	1.17	-0.36
Gd <sub>3</sub> Fe <sup>c</sup> N	1.81	-1.11	-1.11	-1.11	1.52
Gd <sub>3</sub> Fe <sup>f</sup> N	1.42	-0.81	-0.81	0.33	-0.14
W <sub>3</sub> Fe <sup>f</sup> N	1.69	-0.68	-0.68	-0.13	-0.19

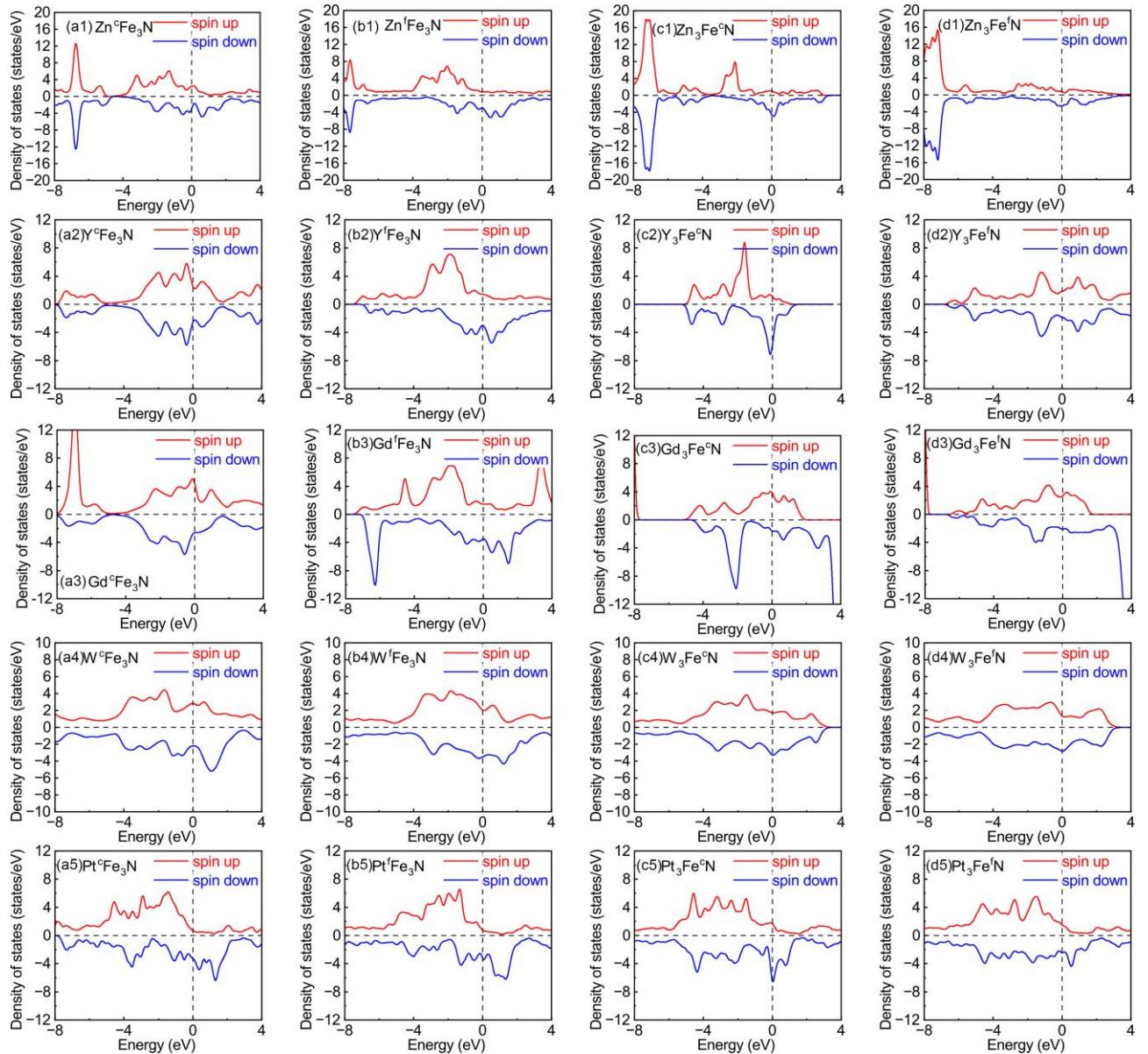
## S4. Total DOS of $M_xFe_{4-x}N$ ( $M = V, Cr, Mn, Co, Cu$ , and $Zn$ )



**Figure S2** Total DOS of (a1-d1)  $V_xFe_{4-x}N$ , (a2-d2)  $Cr_xFe_{4-x}N$ , (a3-d3)  $Mn_xFe_{4-x}N$ , (a4-d4)  $Co_xFe_{4-x}N$ , and (a5-d5)  $Cu_xFe_{4-x}N$  ( $x = 1$  or  $3$ ).

$Cu_xFe_{4-x}N$  ( $x = 1$  or  $3$ ).

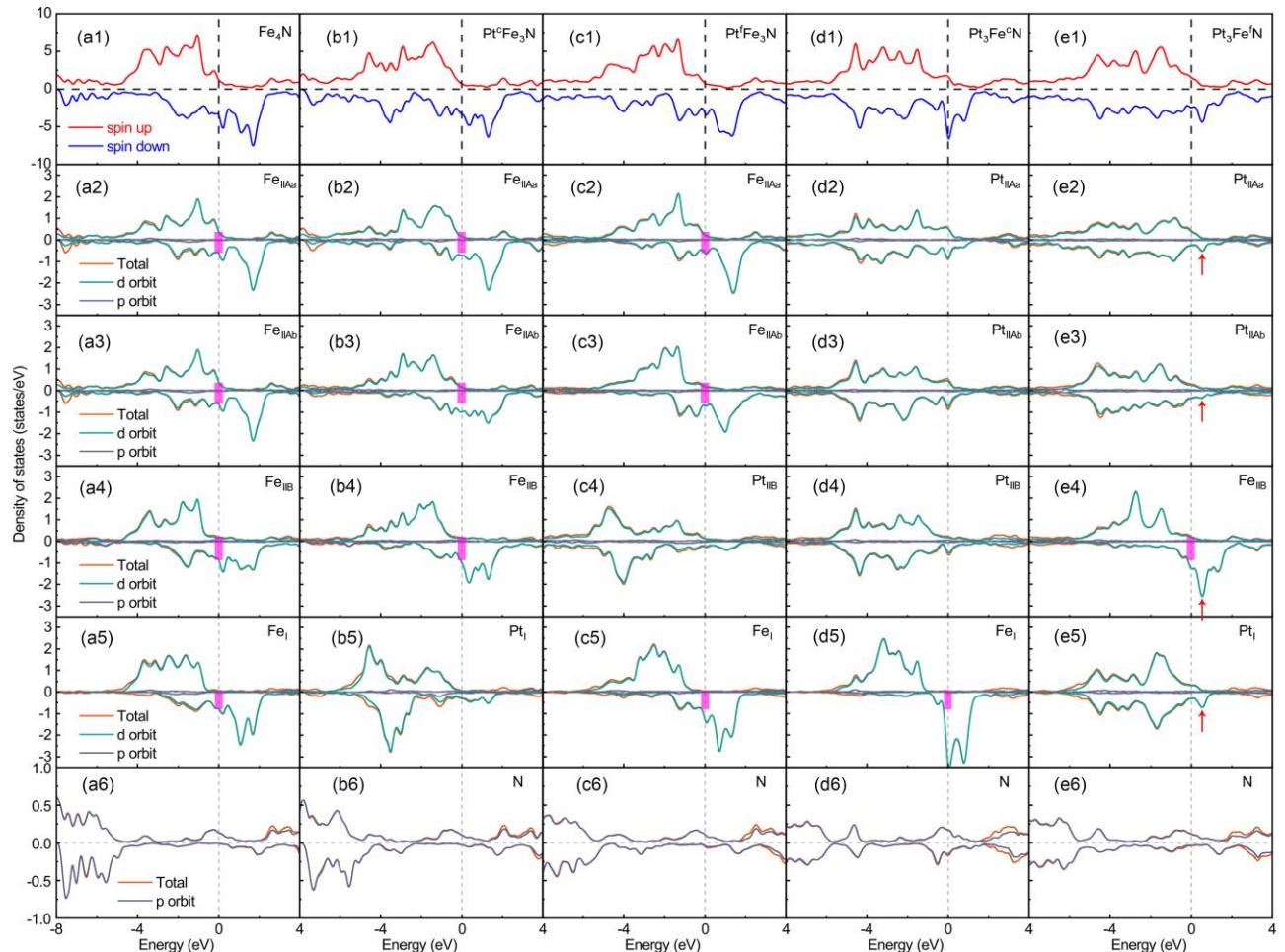
## S5. Total DOS of $M_xFe_{4-x}N$ ( $M = V, Zn, Y, Gd, W, \text{ and } Pt$ )



**Figure S3** Total DOS of (a1-d1)  $Zn_xFe_{4-x}N$ , (a2-d2)  $Y_xFe_{4-x}N$ , (a3-d3)  $Gd_xFe_{4-x}N$ , (a4-d4)  $W_xFe_{4-x}N$ , and (a5-d5)  $Pt_xFe_{4-x}N$  ( $x = 1 \text{ or } 3$ ).

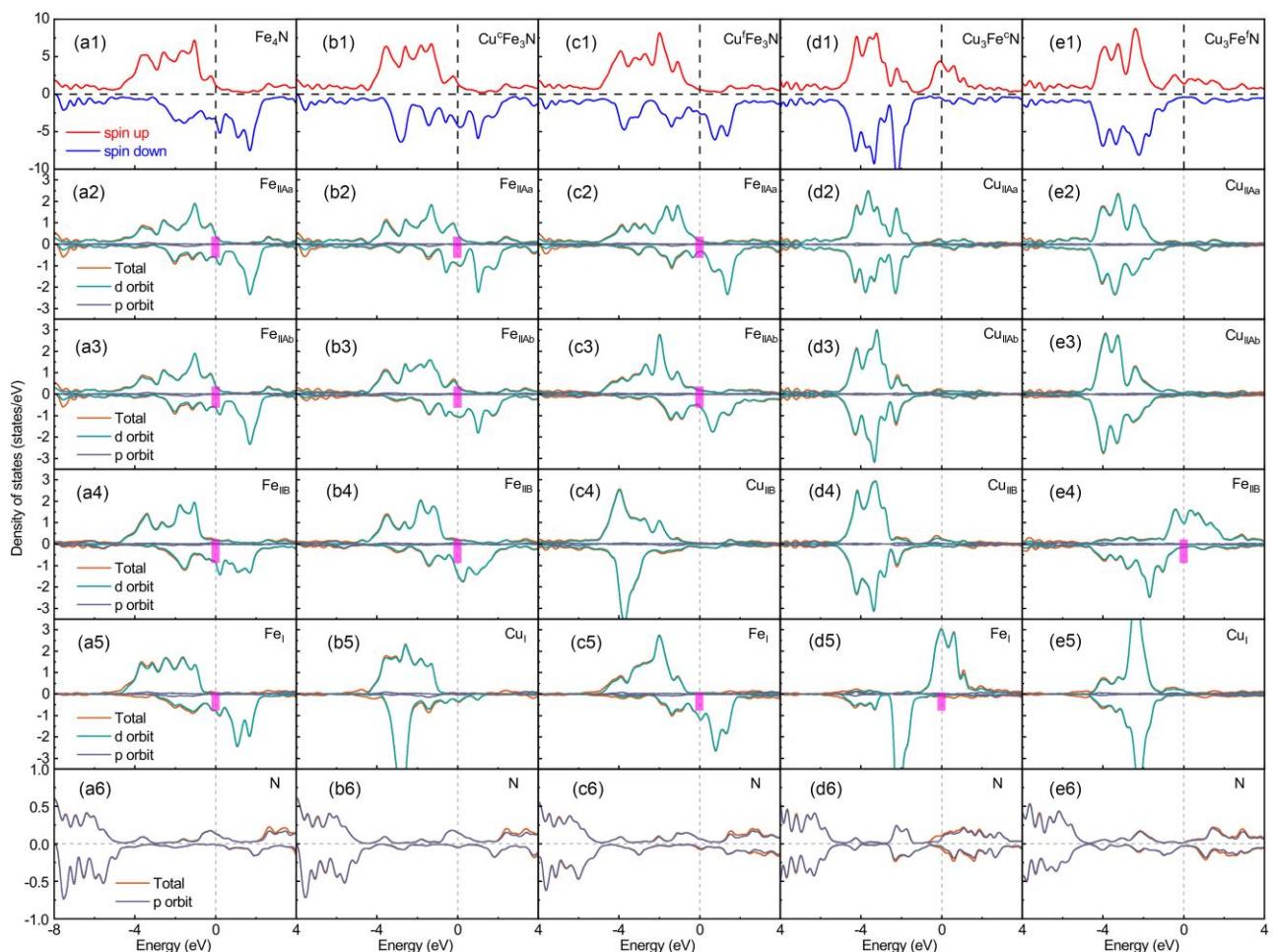
$Pt_xFe_{4-x}N$  ( $x = 1 \text{ or } 3$ ).

## S6. Total DOS, the atom-, orbital-resolved DOS of Fe<sub>4</sub>N and Pt<sub>x</sub>Fe<sub>4-x</sub>N ( $x = 1$ , or 3)



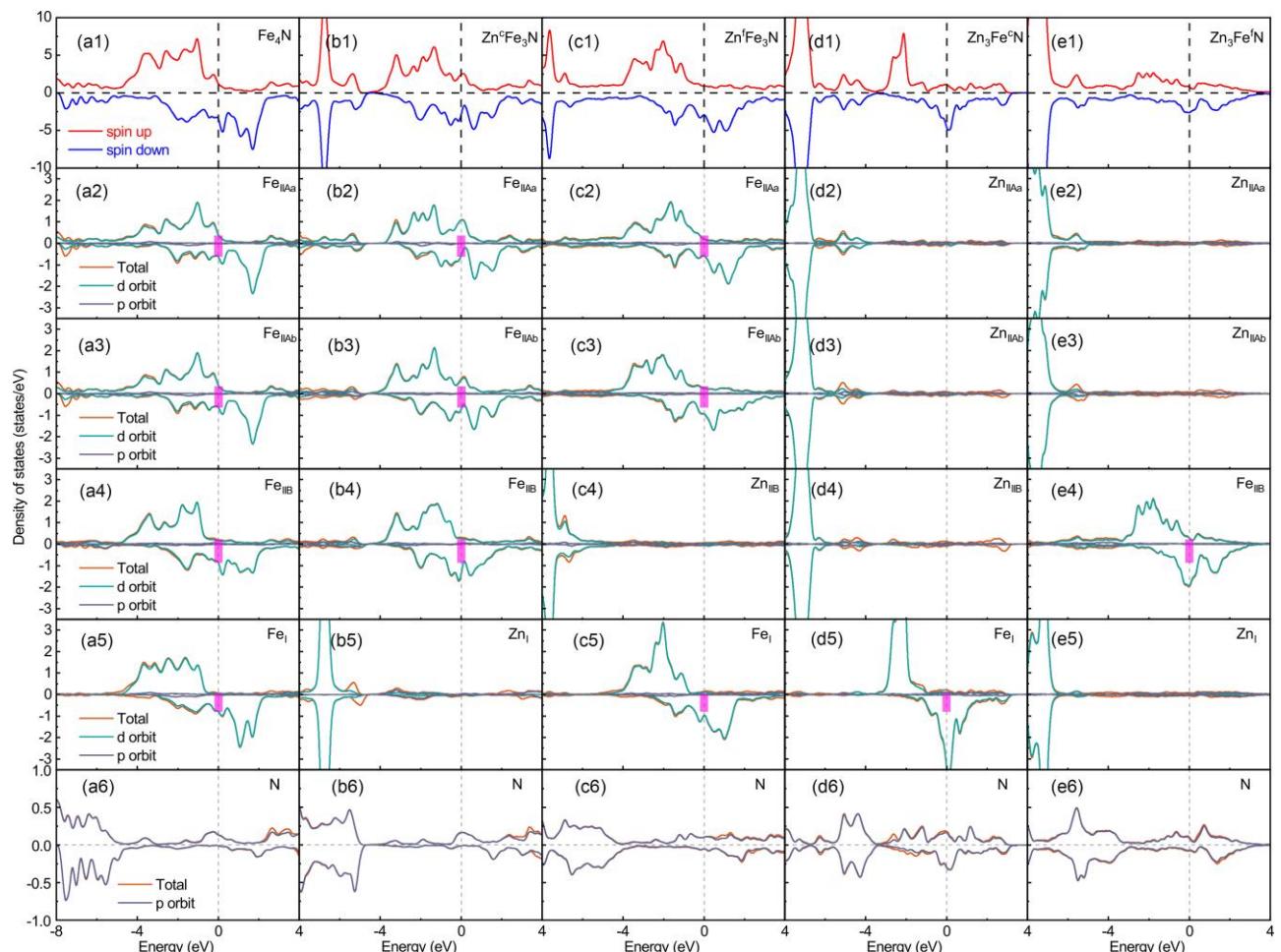
**Figure S4** The total DOS of (a1) Fe<sub>4</sub>N, (b1) Pt<sup>c</sup>Fe<sub>3</sub>N, (c1) Pt<sup>f</sup>Fe<sub>3</sub>N, (d1) Pt<sub>3</sub>Fe<sup>c</sup>N, and (e1) Pt<sub>3</sub>Fe<sup>f</sup>N. The atom-, *d*-orbital- and *p*- orbital-resolved DOS of (a2-e2) Fe<sub>IIA<sub>a</sub></sub>, (a3-e3) Fe<sub>IIAb</sub>, (a4-e4) Fe<sub>IIB</sub>, (a5-e5) Fe<sub>I</sub>, and (a6-e6) N sites.

## S7. Total DOS, the atom-, orbital-resolved DOS of Fe<sub>4</sub>N and Cu<sub>x</sub>Fe<sub>4-x</sub>N ( $x = 1$ , or 3)



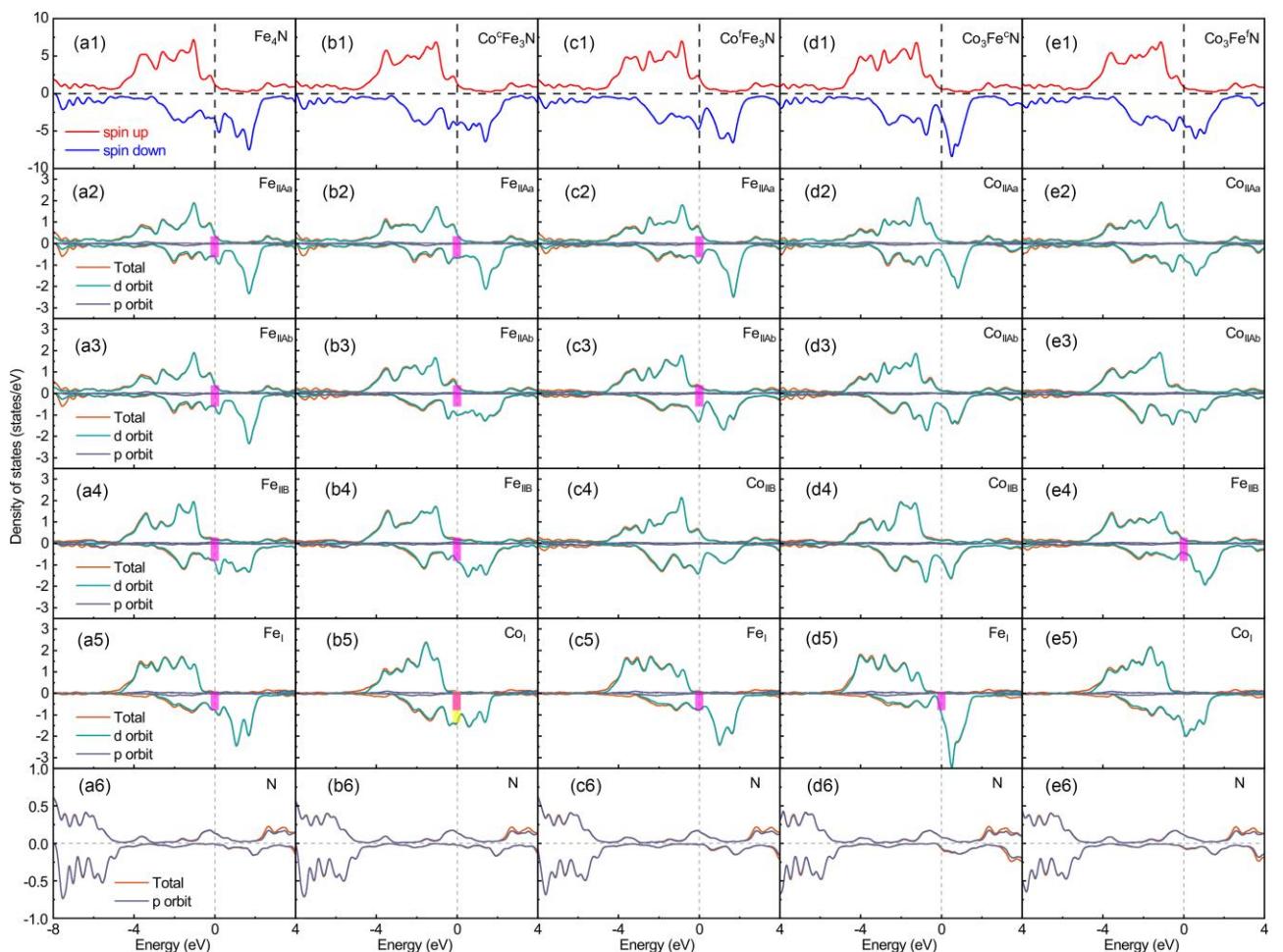
**Figure S5** The total DOS of (a1) Fe<sub>4</sub>N, (b1) Cu<sup>c</sup>Fe<sub>3</sub>N, (c1) Cu<sup>f</sup>Fe<sub>3</sub>N, (d1) Cu<sub>3</sub>Fe<sup>c</sup>N, and (e1) Cu<sub>3</sub>Fe<sup>f</sup>N. The atom-, *d*-orbital- and *p*- orbital-resolved DOS of (a2-e2) Fe<sub>IIAa</sub>, (a3-e3) Fe<sub>IIBa</sub>, (a4-e4) Fe<sub>IIBB</sub>, (a5-e5) Fe<sub>I</sub>, and (a6-e6) N sites.

## S8. Total DOS, the atom-, orbital-resolved DOS of Fe<sub>4</sub>N and Zn<sub>x</sub>Fe<sub>4-x</sub>N ( $x = 1$ , or 3)



**Figure S6** The total DOS of (a1) Fe<sub>4</sub>N, (b1) Zn<sup>c</sup>Fe<sub>3</sub>N, (c1) Zn<sup>f</sup>Fe<sub>3</sub>N, (d1) Zn<sub>3</sub>Fe<sup>c</sup>N, and (e1) Zn<sub>3</sub>Fe<sup>f</sup>N. The atom-, *d*-orbit- and *p*- orbital-resolved DOS of (a2-e2) Fe<sub>IIAa</sub>, (a3-e3) Fe<sub>IIB</sub>, (a4-e4) Fe<sub>IIB</sub>, (a5-e5) Fe<sub>I</sub>, and (a6-e6) N sites.

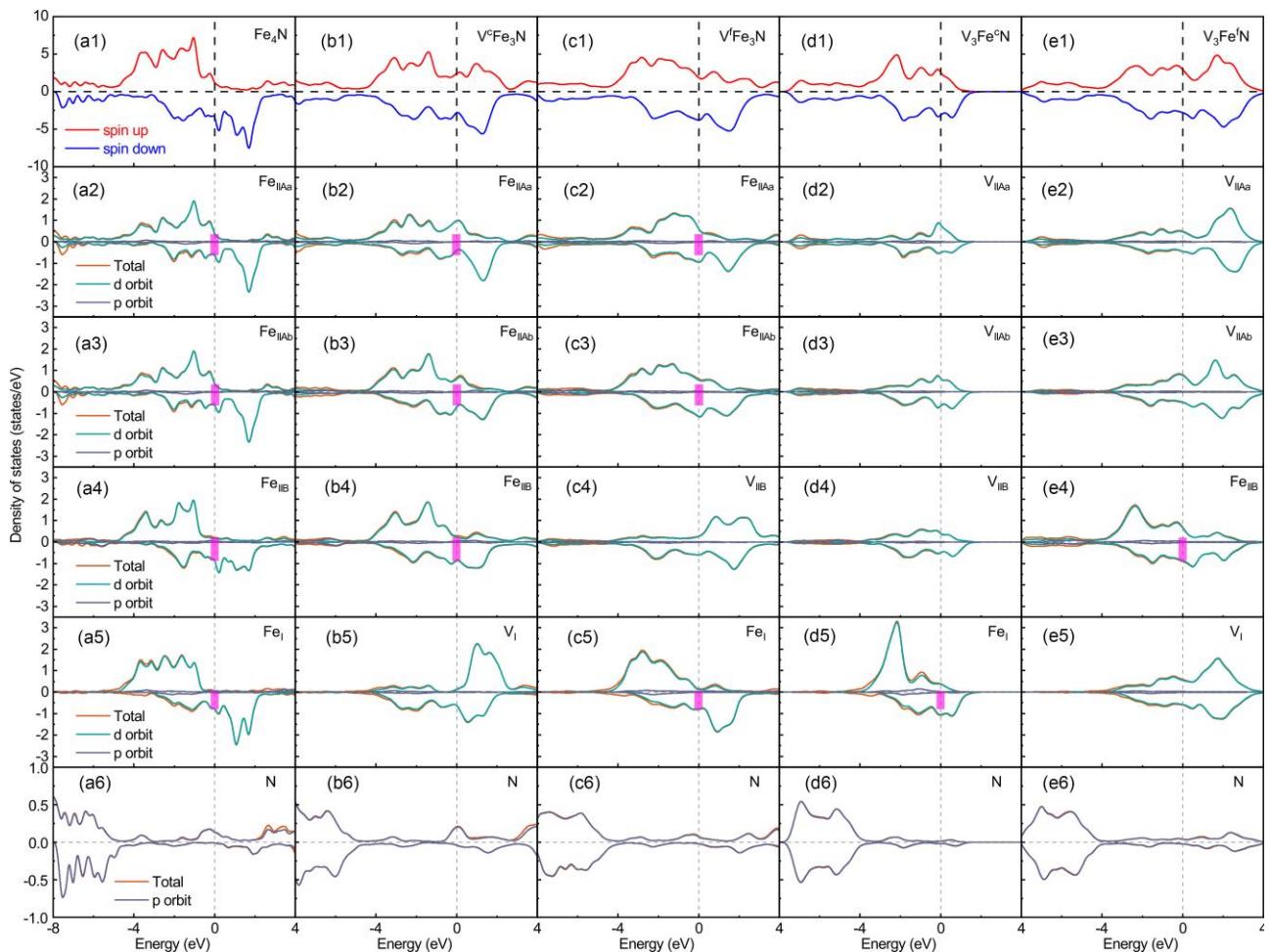
## S9. Total DOS, the atom-, orbital-resolved DOS of Fe<sub>4</sub>N and Co<sub>x</sub>Fe<sub>4-x</sub>N ( $x = 1$ , or 3)



**Figure S7** The total DOS of (a1) Fe<sub>4</sub>N, (b1) Co<sup>c</sup>Fe<sub>3</sub>N, (c1) Co<sup>f</sup>Fe<sub>3</sub>N, (d1) Co<sub>3</sub>Fe<sup>c</sup>N, and (e1) Co<sub>3</sub>Fe<sup>f</sup>N. The atom-,

*d*-orbit- and *p*- orbital-resolved DOS of (a2-e2) Fe<sub>IIAa</sub>, (a3-e3) Fe<sub>IIAb</sub>, (a4-e4) Fe<sub>IIB</sub>, (a5-e5) Fe<sub>I</sub>, and (a6-e6) N sites.

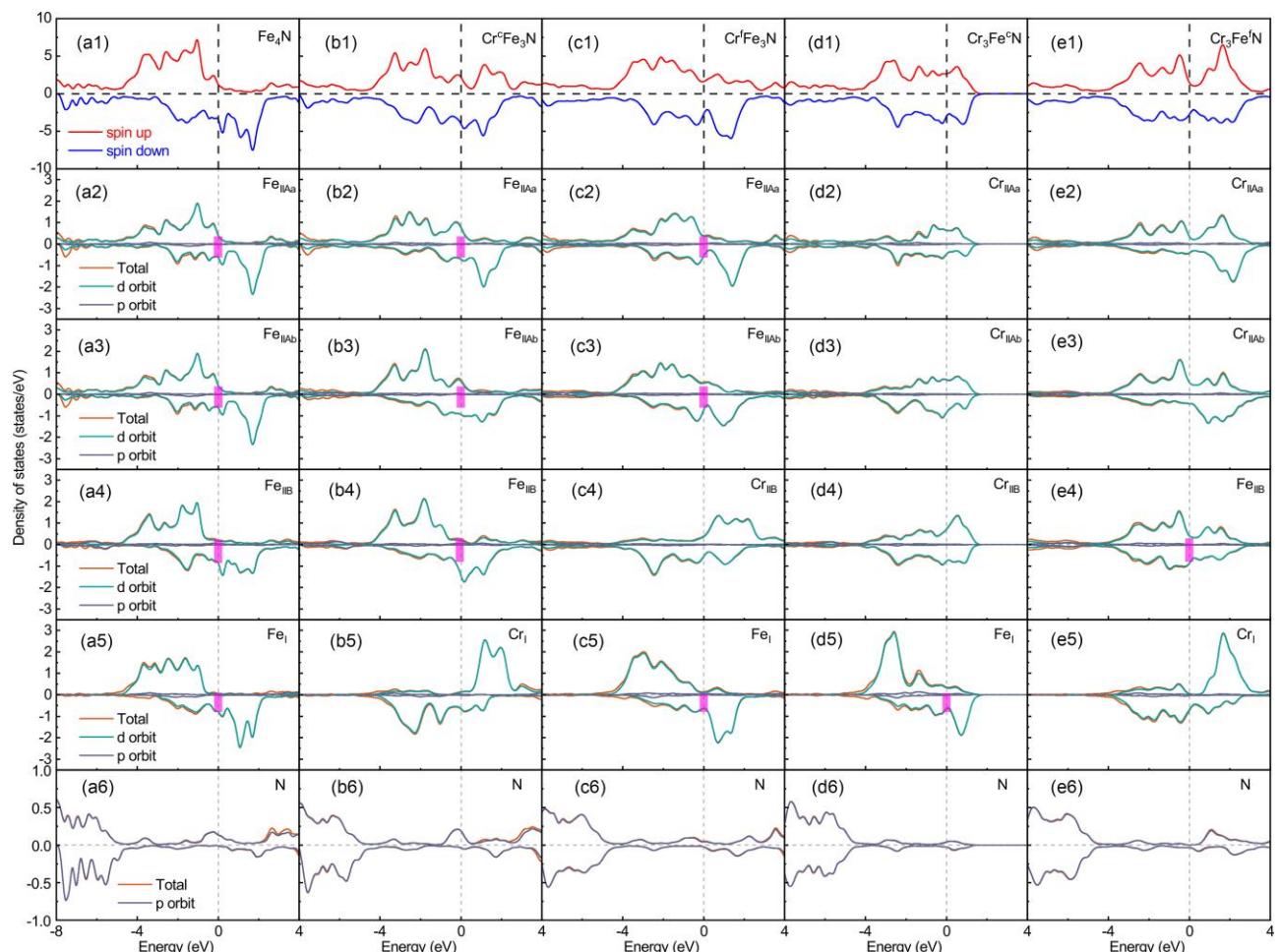
## S10. Total DOS, the atom-, orbital-resolved DOS of Fe<sub>4</sub>N and V<sub>x</sub>Fe<sub>4-x</sub>N ( $x = 1$ , or 3)



**Figure S8** The total DOS of (a1) Fe<sub>4</sub>N, (b1) V<sup>c</sup>Fe<sub>3</sub>N, (c1) V<sup>f</sup>Fe<sub>3</sub>N, (d1) V<sub>3</sub>Fe<sup>c</sup>N, and (e1) V<sub>3</sub>Fe<sup>f</sup>N. The atom-,

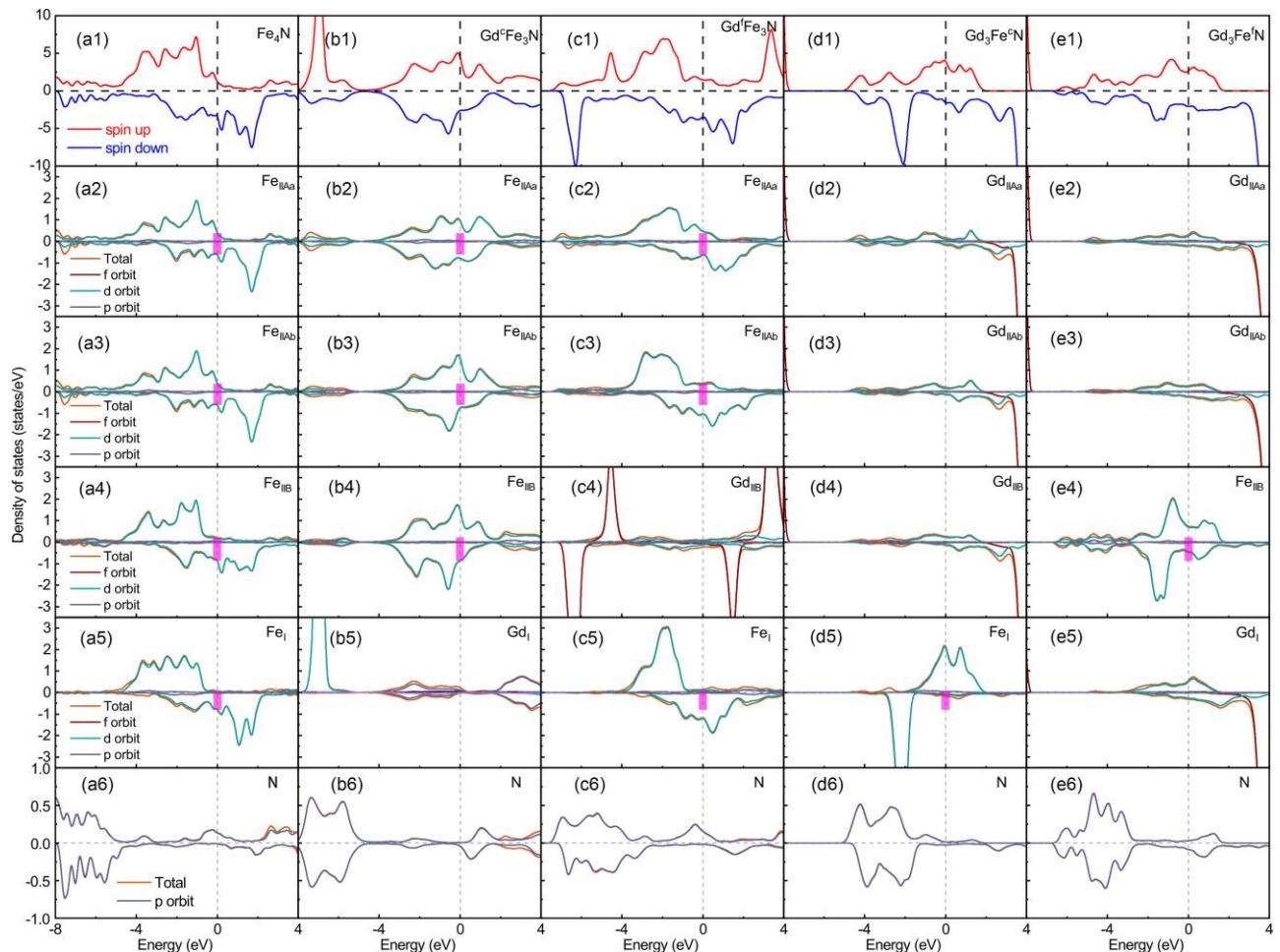
*d*-orbit- and *p*- orbital-resolved DOS of (a2-e2) Fe<sub>IIAa</sub>, (a3-e3) Fe<sub>IIBa</sub>, (a4-e4) Fe<sub>IIBb</sub>, (a5-e5) Fe<sub>I</sub>, and (a6-e6) N sites.

**S11. Total DOS, the atom-, orbital-resolved DOS of Fe<sub>4</sub>N and Cr<sub>x</sub>Fe<sub>4-x</sub>N ( $x = 1$ , or 3)**



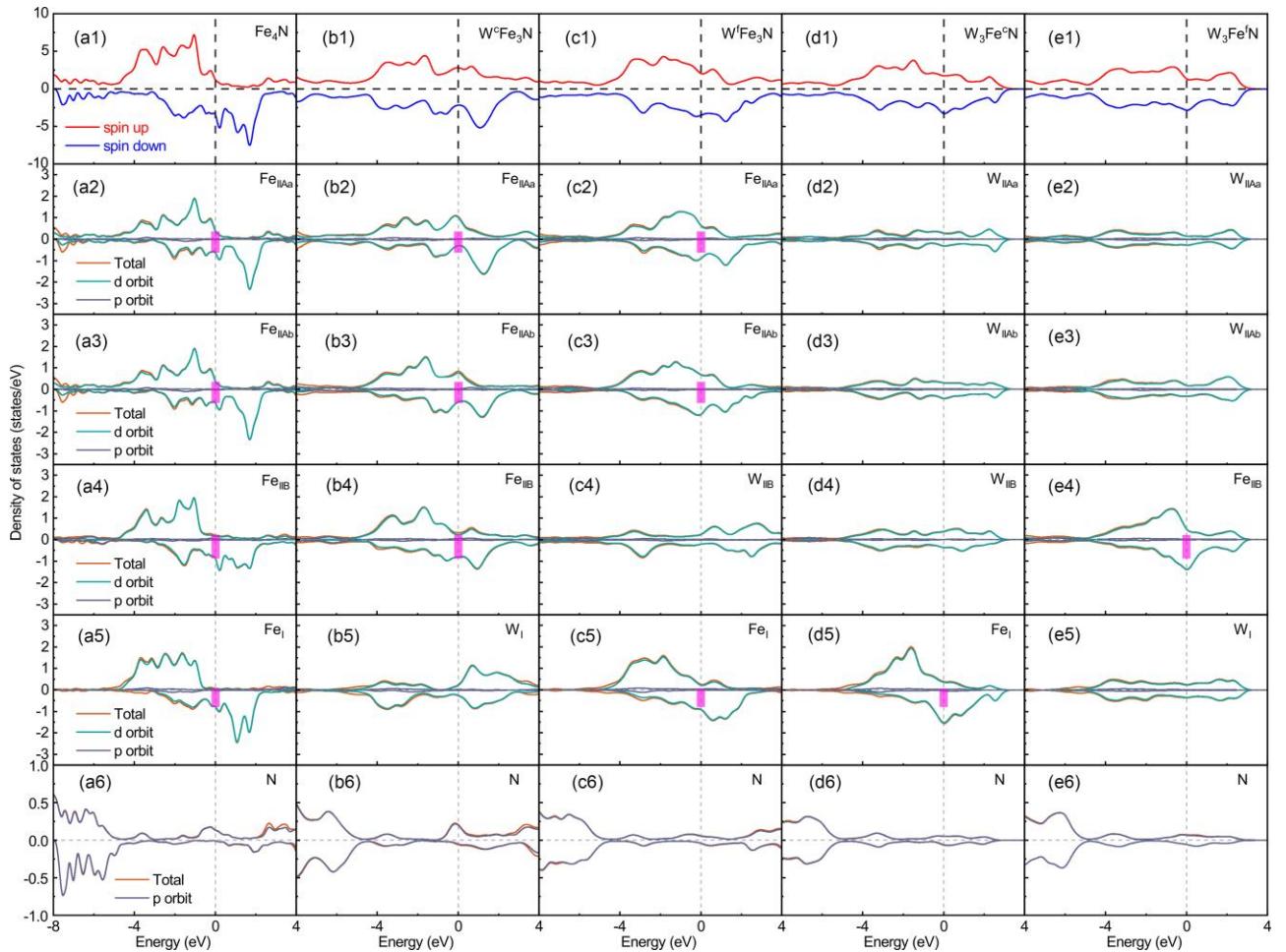
**Figure S9** The total DOS of (a1) Fe<sub>4</sub>N, (b1) Cr<sup>c</sup>Fe<sub>3</sub>N, (c1) Cr<sup>f</sup>Fe<sub>3</sub>N, (d1) Cr<sub>3</sub>Fe<sup>c</sup>N, and (e1) Cr<sub>3</sub>Fe<sup>f</sup>N. The atom-, *d*-orbital- and *p*- orbital-resolved DOS of (a2-e2) Fe<sub>IIAa</sub>, (a3-e3) Fe<sub>IAb</sub>, (a4-e4) Fe<sub>IIB</sub>, (a5-e5) Fe<sub>I</sub>, and (a6-e6) N sites.

## S12. Total DOS, the atom-, orbital-resolved DOS of Fe<sub>4</sub>N and Gd<sub>x</sub>Fe<sub>4-x</sub>N ( $x = 1$ , or 3)



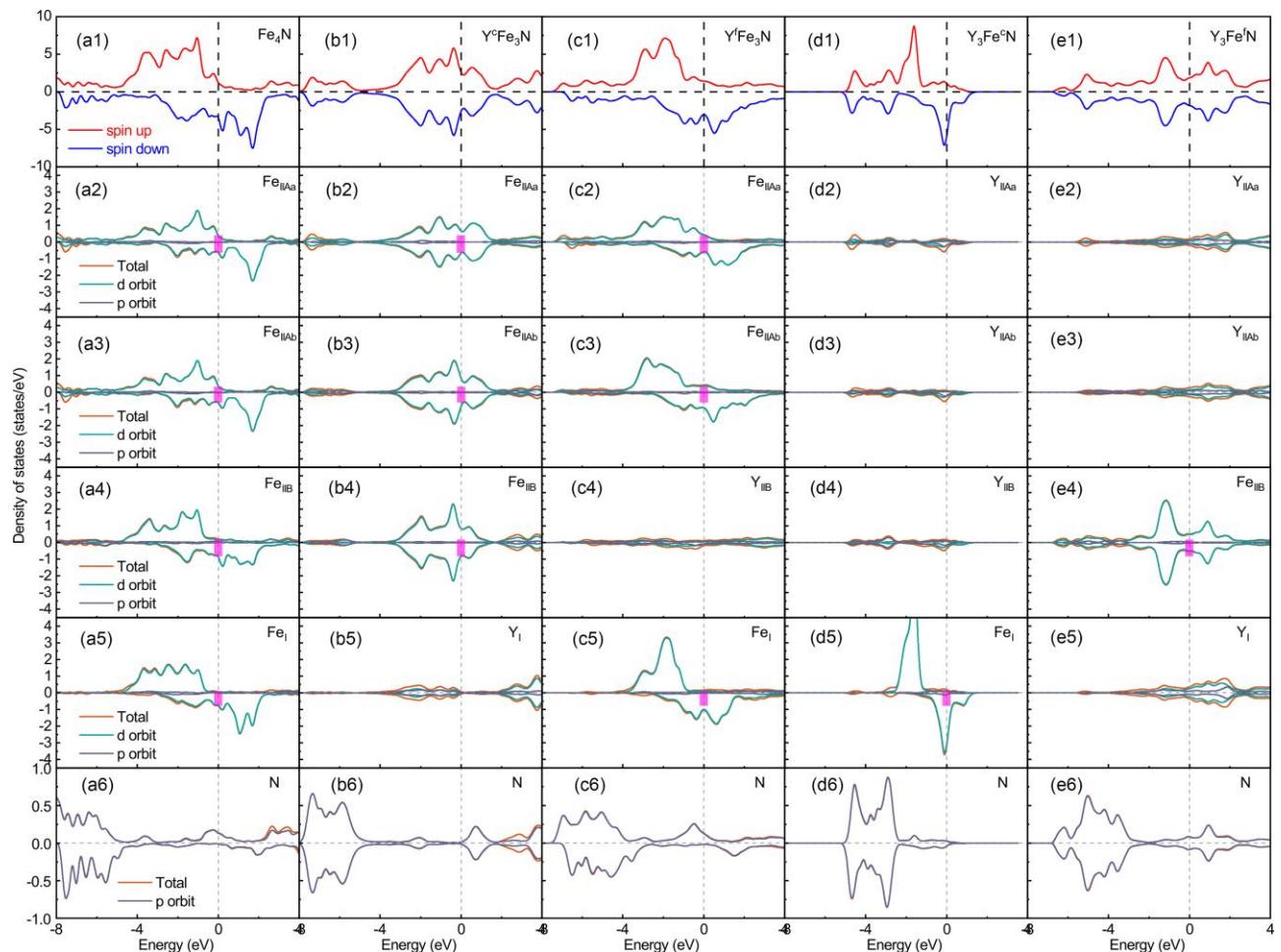
**Figure S10** The total DOS of (a1) Fe<sub>4</sub>N, (b1) Gd<sup>c</sup>Fe<sub>3</sub>N, (c1) Gd<sup>f</sup>Fe<sub>3</sub>N, (d1) Gd<sub>3</sub>Fe<sup>c</sup>N, and (e1) Gd<sub>3</sub>Fe<sup>f</sup>N. The atom-, *d*-orbital- and *p*- orbital-resolved DOS of (a2-e2) Fe<sub>IIAa</sub>, (a3-e3) Fe<sub>IIB</sub>, (a4-e4) Fe<sub>IIB</sub>, (a5-e5) Fe<sub>I</sub>, and (a6-e6) N sites.

### S13. Total DOS, the atom-, orbital-resolved DOS of Fe<sub>4</sub>N and W<sub>x</sub>Fe<sub>4-x</sub>N ( $x = 1$ , or 3)



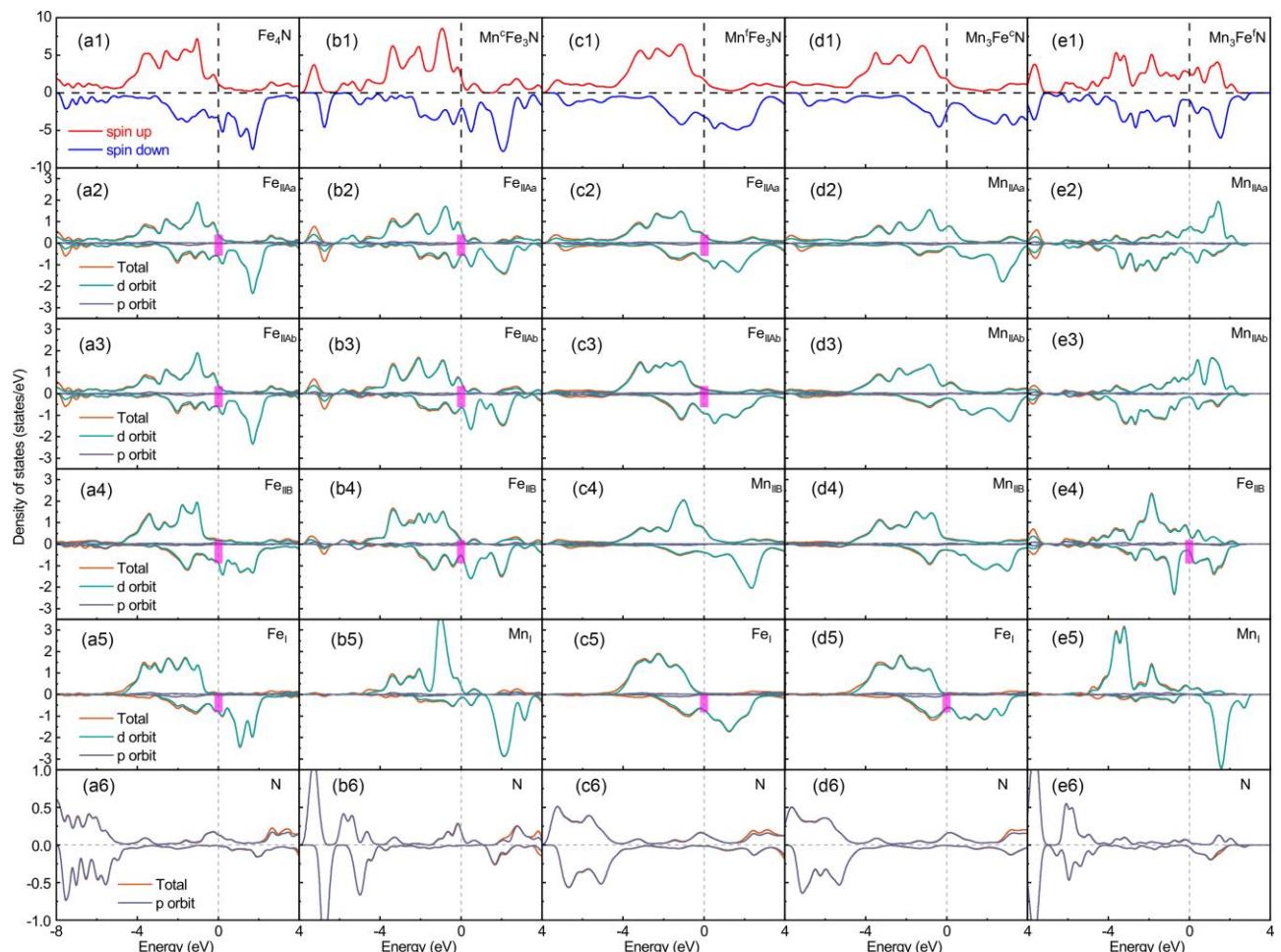
**Figure S11** The total DOS of (a1) Fe<sub>4</sub>N, (b1) W<sup>c</sup>Fe<sub>3</sub>N, (c1) W<sup>f</sup>Fe<sub>3</sub>N, (d1) W<sub>3</sub>Fe<sup>c</sup>N, and (e1) W<sub>3</sub>Fe<sup>f</sup>N. The atom-, *d*-orbital- and *p*- orbital-resolved DOS of (a2-e2) Fe<sub>IIAa</sub>, (a3-e3) Fe<sub>IIB</sub>, (a4-e4) Fe<sub>IAb</sub>, (a5-e5) Fe<sub>I</sub>, and (a6-e6) N sites.

**S14. Total DOS, the atom-, orbital-resolved DOS of Fe<sub>4</sub>N and Y<sub>x</sub>Fe<sub>4-x</sub>N ( $x = 1$ , or 3)**



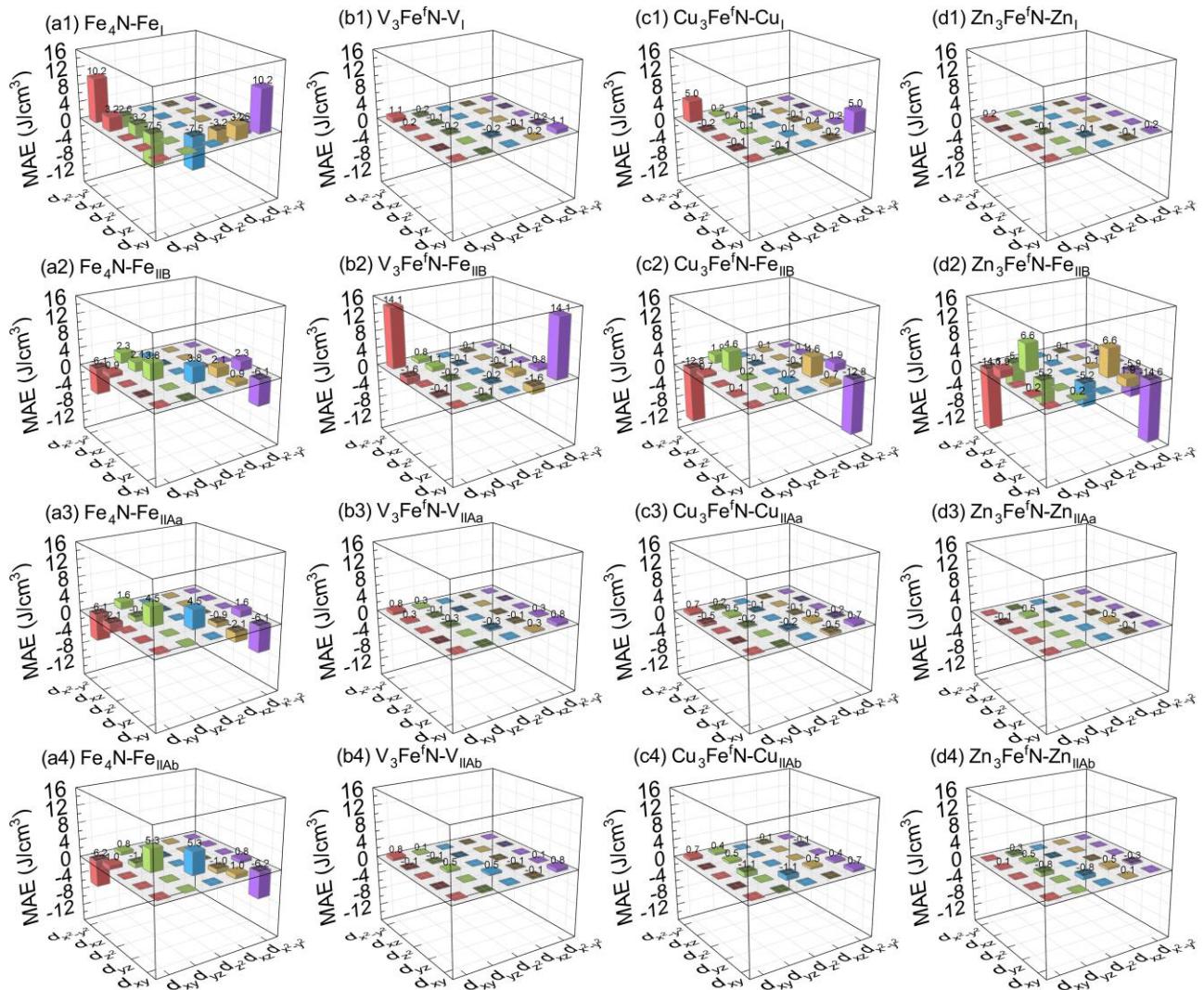
**Figure S12** The total DOS of (a1) Fe<sub>4</sub>N, (b1) Y<sup>c</sup>Fe<sub>3</sub>N, (c1) Y<sup>f</sup>Fe<sub>3</sub>N, (d1) Y<sub>3</sub>Fe<sup>c</sup>N, and (e1) Y<sub>3</sub>Fe<sup>f</sup>N. The atom-, *d*-orbital- and *p*- orbital-resolved DOS of (a2-e2) Fe<sub>IIAa</sub>, (a3-e3) Fe<sub>IIBa</sub>, (a4-e4) Fe<sub>IIBb</sub>, (a5-e5) Fe<sub>I</sub>, and (a6-e6) N sites.

**S15. Total DOS, the atom-, orbital-resolved DOS of Fe<sub>4</sub>N and Mn<sub>x</sub>Fe<sub>4-x</sub>N ( $x = 1$ , or 3)**



**Figure S13** The total DOS of (a1) Fe<sub>4</sub>N, (b1) Mn<sup>c</sup>Fe<sub>3</sub>N, (c1) Mn<sup>f</sup>Fe<sub>3</sub>N, (d1) Mn<sub>3</sub>Fe<sup>c</sup>N, and (e1) Mn<sub>3</sub>Fe<sup>f</sup>N. The atom-, *d*-orbital- and *p*- orbital-resolved DOS of (a2-e2) Fe<sub>IIAa</sub>, (a3-e3) Fe<sub>IAb</sub>, (a4-e4) Fe<sub>IIB</sub>, (a5-e5) Fe<sub>I</sub>, and (a6-e6) N sites.

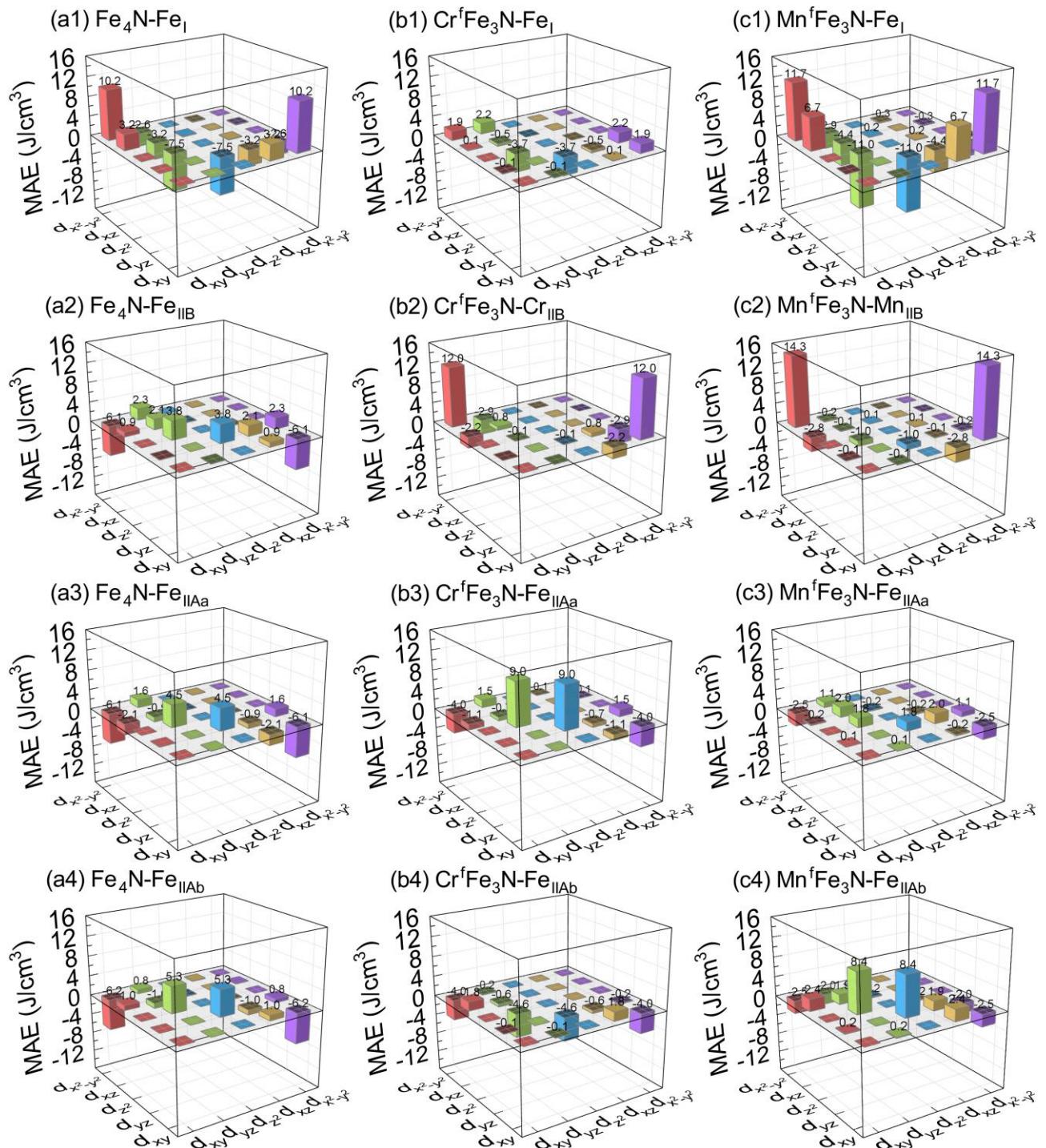
## S16. The orbital-resolved MAE of $\text{Fe}_4\text{N}$ and $M_3\text{Fe}^{\text{f}}\text{N}$ ( $M = \text{V}, \text{Cu}, \text{and Zn}$ )



**Figure S14** The orbital-resolved MAE of (a1-a4)  $\text{Fe}_4\text{N}$ , (b1-b4)  $\text{V}_3\text{Fe}^{\text{f}}\text{N}$ , (c1-c4)  $\text{Cu}_3\text{Fe}^{\text{f}}\text{N}$ , and (d1-d4)  $\text{Zn}^{\text{f}}\text{Fe}_3\text{N}$ .

The orbital-resolved MAE of (a1-e1)  $\text{Fe}_{\text{I}}$ , (a2-e2)  $\text{Fe}_{\text{IIB}}$ , (a3-e3)  $\text{Fe}_{\text{IIAa}}$ , and (a4-e4)  $\text{Fe}_{\text{IIAb}}$  sites.

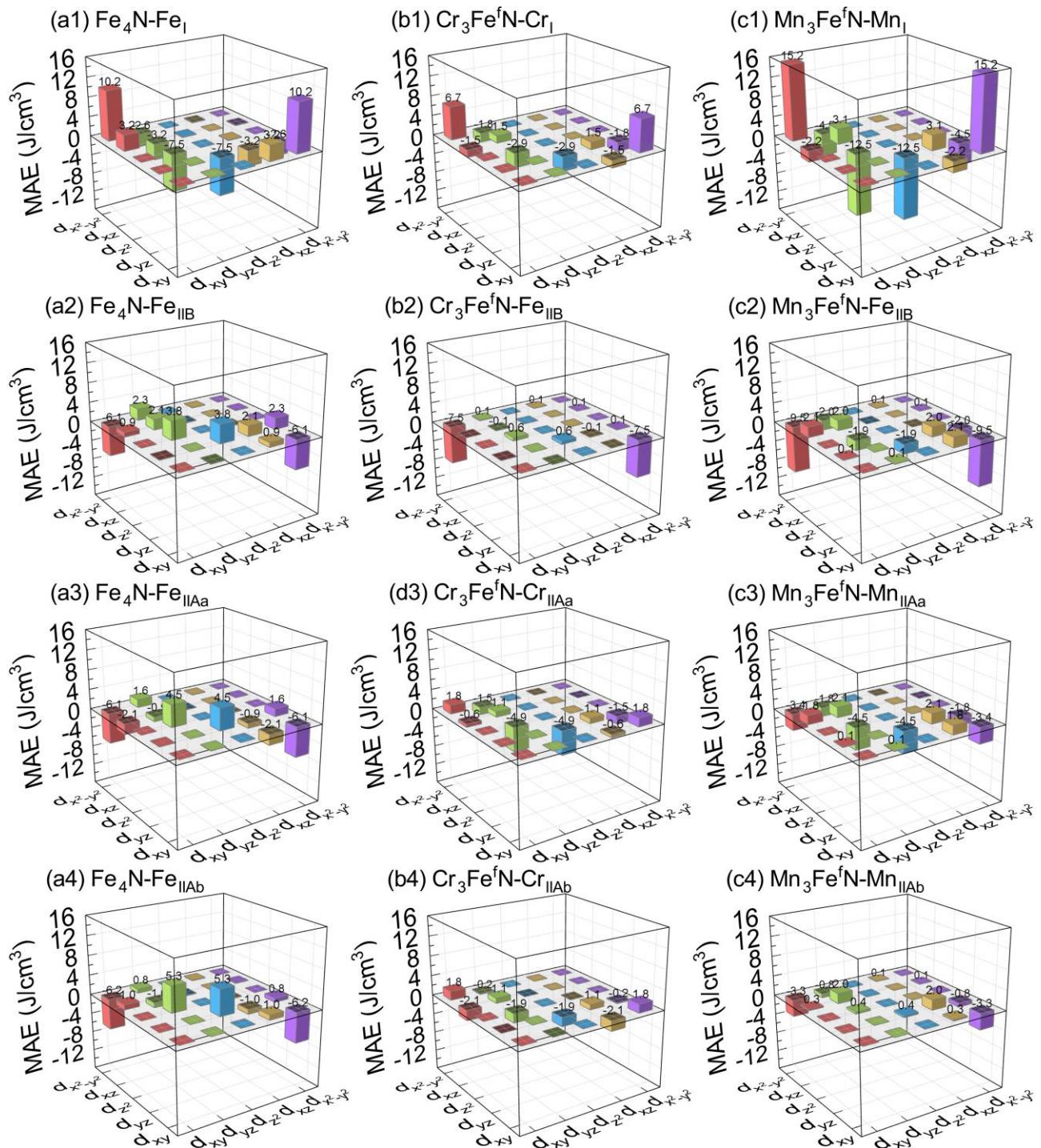
## S17. The orbital-resolved MAE of Fe<sub>4</sub>N and M<sup>f</sup>Fe<sub>3</sub>N ( $M = \text{Cr}$ and $\text{Mn}$ )



**Figure S15** The orbital-resolved MAE of (a1-a4) Fe<sub>4</sub>N, (b1-b4) Cr<sup>f</sup>Fe<sub>3</sub>N, and (c1-c4) Mn<sup>f</sup>Fe<sub>3</sub>N. The

orbital-resolved MAE of (a1-c1) Fe<sub>I</sub>, (a2-c2) Fe<sub>IIIB</sub>, (a3-c3) Fe<sub>IIAa</sub>, and (a4-c4) Fe<sub>IIAb</sub> sites.

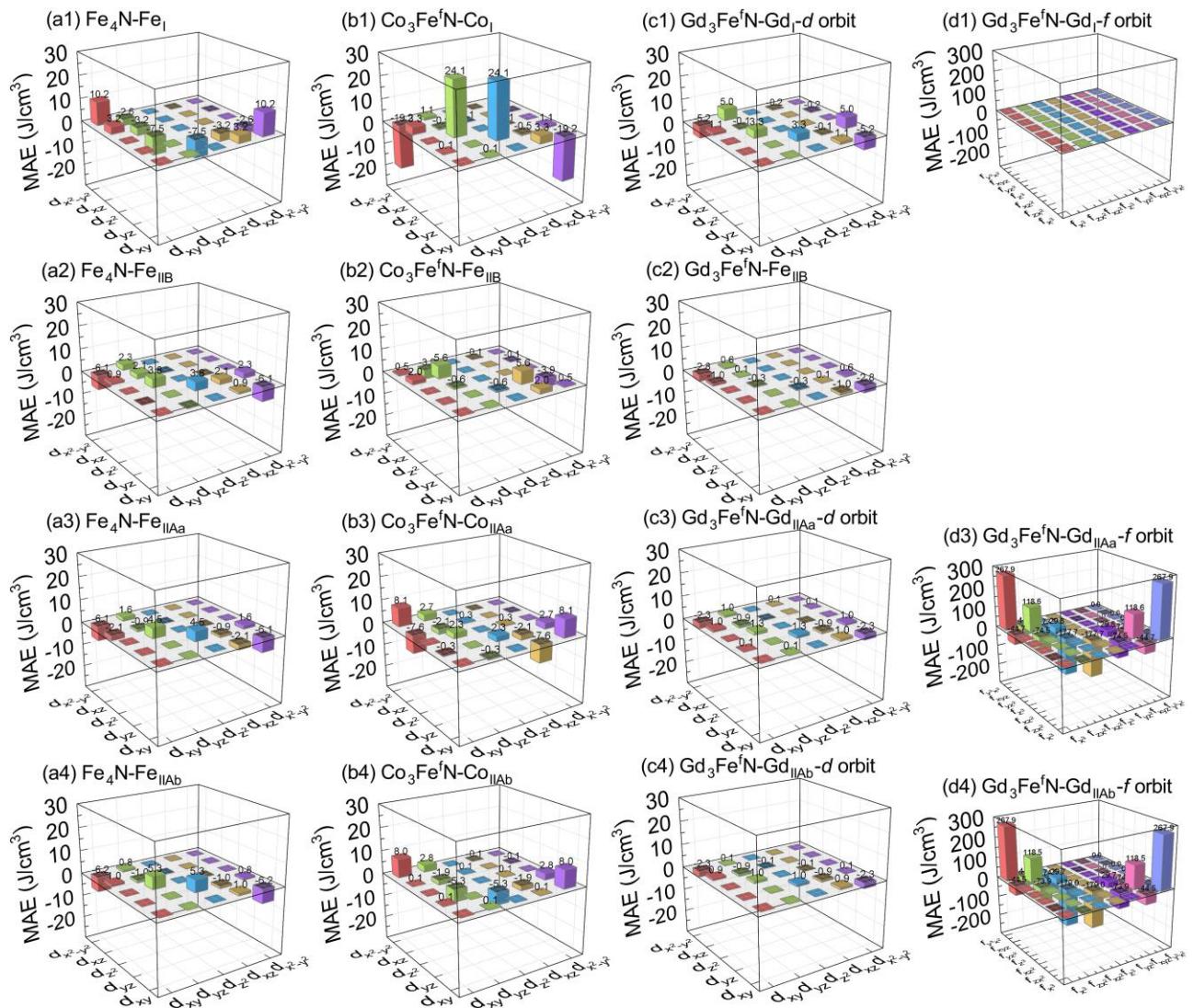
## S18. The orbital-resolved MAE of Fe<sub>4</sub>N and M<sub>3</sub>Fe<sup>f</sup>N (M = Cr and Mn)



**Figure S16** The orbital-resolved MAE of (a1-a4) Fe<sub>4</sub>N, (b1-b4) Cr<sub>3</sub>Fe<sup>f</sup>N, and (c1-c4) Mn<sub>3</sub>Fe<sup>f</sup>N. The

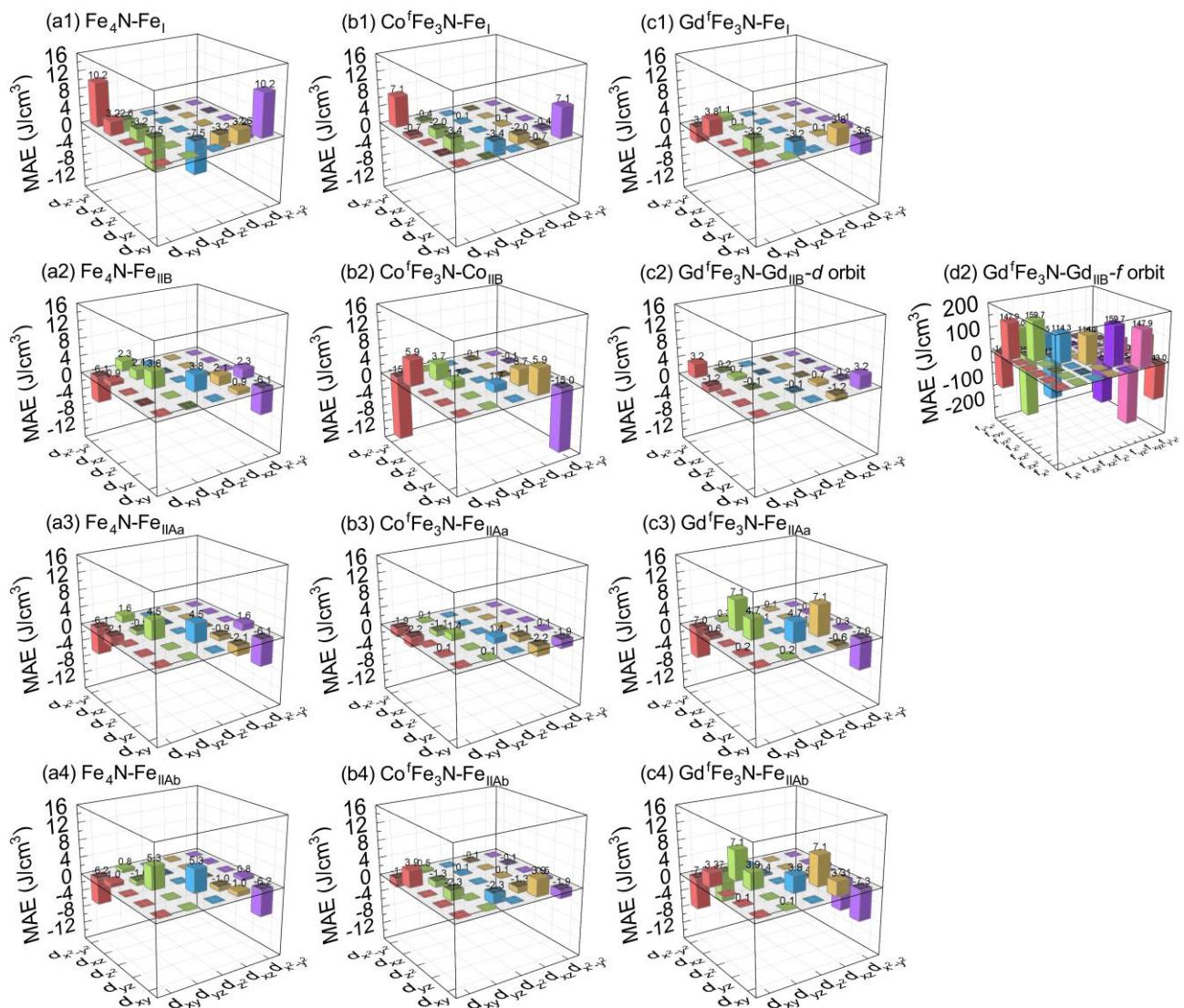
orbital-resolved MAE of (a1-c1) Fe<sub>I</sub>, (a2-c2) Fe<sub>IIIB</sub>, (a3-c3) Fe<sub>IIIAa</sub>, and (a4-c4) Fe<sub>IIAb</sub> sites.

## S19. The orbital-resolved MAE of Fe<sub>4</sub>N and M<sub>3</sub>Fe<sup>f</sup>N ( $M = \text{Co}$ and Gd)



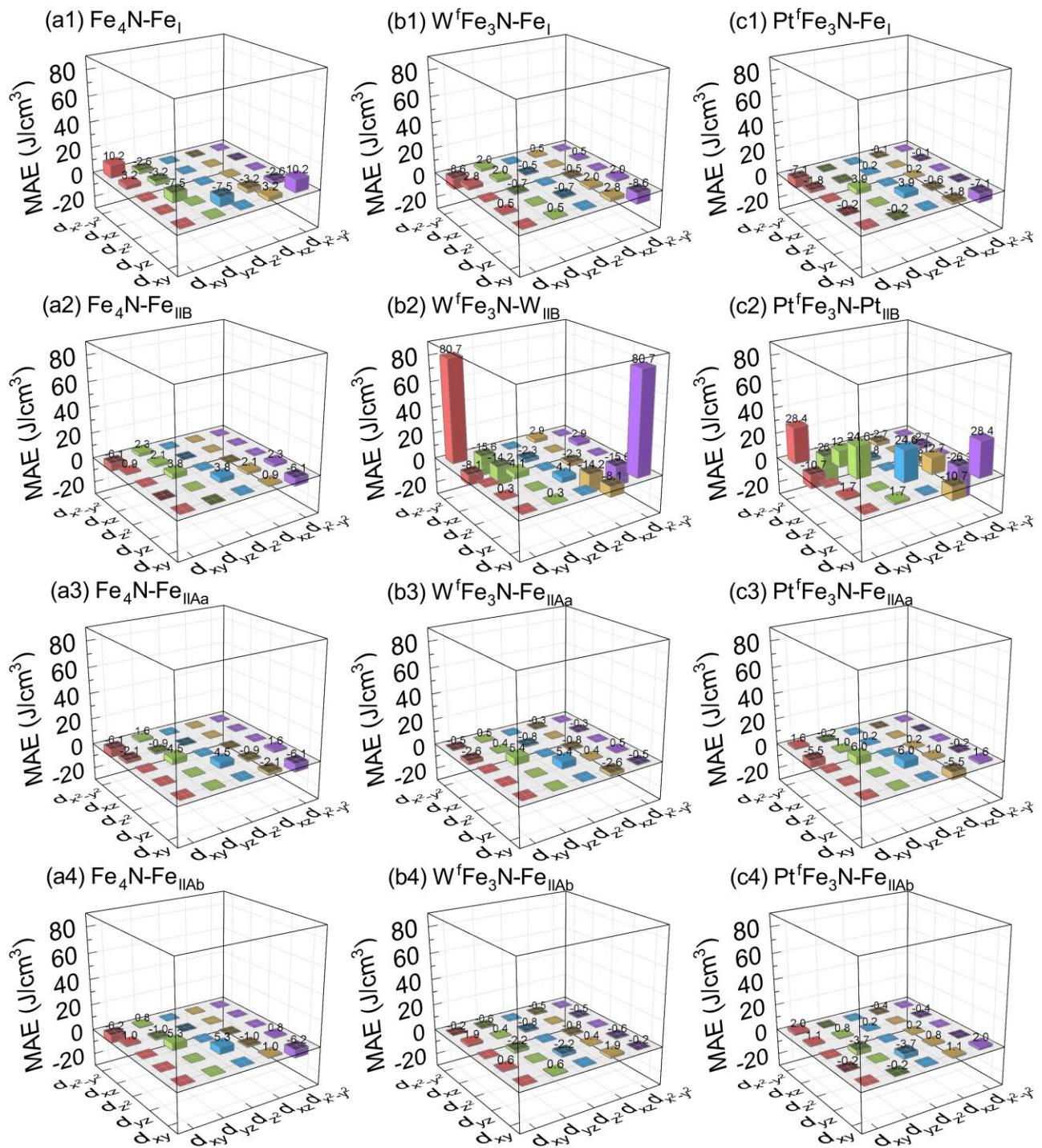
**Figure S17** The orbital-resolved MAE of (a1-a4) Fe<sub>4</sub>N, (b1-b4) Co<sub>3</sub>Fe<sup>f</sup>N, and (c1-c4) Gd<sub>3</sub>Fe<sup>f</sup>N. The orbital-resolved MAE of (a1-d1) Fe<sub>I</sub>, (a2-c2) Fe<sub>IIB</sub>, (a3-d3) Fe<sub>IIAa</sub>, and (a4-d4) Fe<sub>IIAb</sub> sites.

## S20. The orbital-resolved MAE of $\text{Fe}_4\text{N}$ and $M^f\text{Fe}_3\text{N}$ ( $M = \text{Co}$ and $\text{Gd}$ )



**Figure S18** The orbital-resolved MAE of (a1-a4)  $\text{Fe}_4\text{N}$ , (b1-b4)  $\text{Co}^f\text{Fe}_3\text{N}$ , and (c1-c4)  $\text{Gd}^f\text{Fe}_3\text{N}$ . The orbital-resolved MAE of (a1-c1)  $\text{Fe}_I$ , (a2-d2)  $\text{Fe}_{\text{IIIB}}$ , (a3-c3)  $\text{Fe}_{\text{IIIAa}}$ , and (a4-c4)  $\text{Fe}_{\text{IIAb}}$  sites.

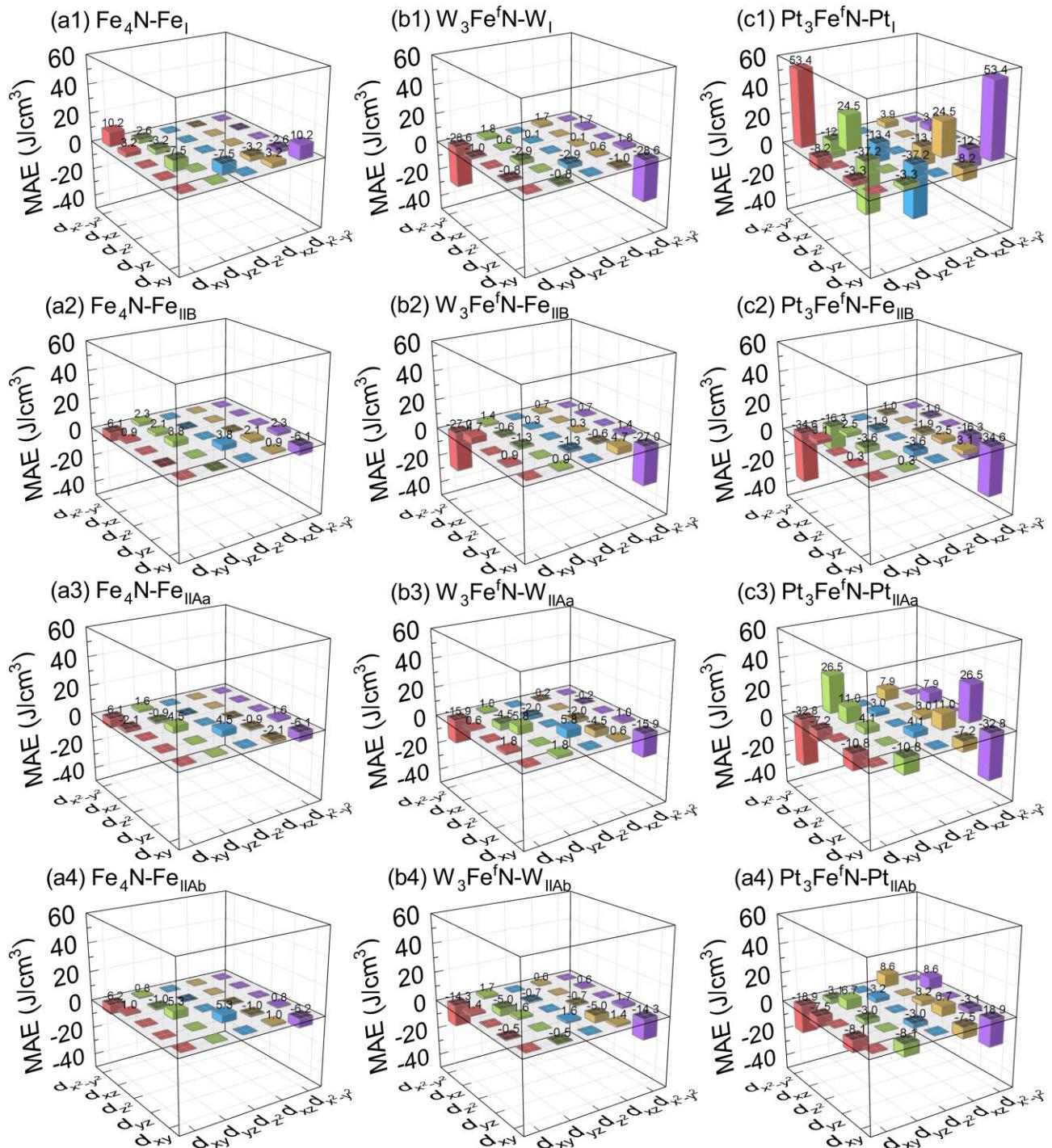
## S21. The orbital-resolved MAE of $\text{Fe}_4\text{N}$ and $M^f\text{Fe}_3\text{N}$ ( $M = \text{W}$ and $\text{Pt}$ )



**Figure S19** The orbital-resolved MAE of (a1-a4)  $\text{Fe}_4\text{N}$ , (b1-b4)  $\text{W}^f\text{Fe}_3\text{N}$ , and (c1-c4)  $\text{Pt}^f\text{Fe}_3\text{N}$ . The

orbital-resolved MAE of (a1-c1)  $\text{Fe}_\text{I}$ , (a2-c2)  $\text{Fe}_\text{IIIB}$ , (a3-c3)  $\text{Fe}_\text{IIIAa}$ , and (a4-c4)  $\text{Fe}_\text{IIAb}$  sites.

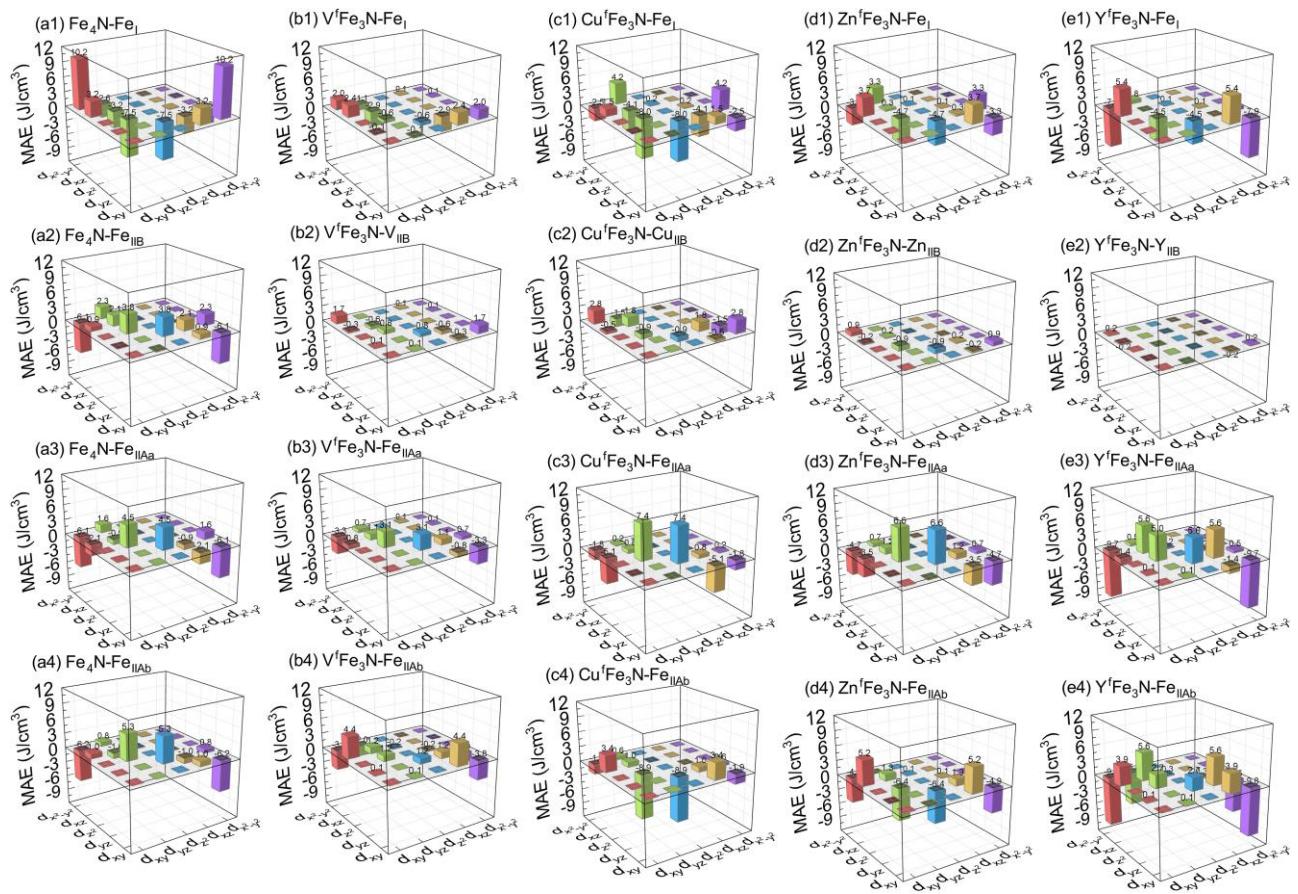
## S22. The orbital-resolved MAE of Fe<sub>4</sub>N and M<sub>3</sub>Fe<sup>f</sup>N (*M* = W and Pt)



**Figure S20** The orbital-resolved MAE of (a1-a4) Fe<sub>4</sub>N, (b1-b4) W<sub>3</sub>Fe<sup>f</sup>N, and (c1-c4) Pt<sub>3</sub>Fe<sup>f</sup>N. The

orbital-resolved MAE of (a1-c1) Fe<sub>I</sub>, (a2-c2) Fe<sub>IIIB</sub>, (a3-c3) Fe<sub>IIIAa</sub>, and (a4-c4) Fe<sub>IIAb</sub> sites.

## S23. The orbital-resolved MAE of Fe<sub>4</sub>N and M<sup>f</sup>Fe<sub>3</sub>N ( $M = \text{V, Cu, Zn, and Y}$ )



**Figure S21** The orbital-resolved MAE of (a1-a4) Fe<sub>4</sub>N, (b1-b4) V<sup>f</sup>Fe<sub>3</sub>N, (c1-c4) Cu<sup>f</sup>Fe<sub>3</sub>N, (d1-d4) Zn<sup>f</sup>Fe<sub>3</sub>N, and

(e1-e4) Y<sup>f</sup>Fe<sub>3</sub>N. The orbital-resolved MAE of (a1-e1) Fe<sub>I</sub>, (a2-e2) Fe<sub>IIB</sub>, (a3-e3) Fe<sub>IIAa</sub>, and (a4-e4) Fe<sub>IIAb</sub>

sites.

## S24. The priority occupancy of $M^cFe_3N$

**Table S3** The energy difference  $\Delta E = E(M^cFe_3N) - E(M^fFe_3N)$ , where  $E(M^cFe_3N)$  represents the energy of  $M^cFe_3N$  with cubic structure, and  $E(M^fFe_3N)$  represents the energy of  $M^fFe_3N$  with tetragonal structure.

Substitution element	$E(M^cFe_3N)$	$E(M^fFe_3N)$	$\Delta E = E(M^cFe_3N) - E(M^fFe_3N)$	Preferential occupancy site
Gd	-46.845632	-41.178468	-5.667164	$Gd^cFe_3N$
Pt	-38.479763	-37.078104	-1.401659	$Pt^cFe_3N$
Zn	-34.527096	-33.164175	-1.362921	$Zn^cFe_3N$
Cu	-36.888784	-36.192724	-0.696060	$Cu^cFe_3N$
Mn	-42.122090	-42.045820	-0.076269	$Mn^cFe_3N$
Co	-40.209929	-40.264990	0.055063	$Co^fFe_3N$
Y	-36.274933	-36.485999	0.211066	$Y^fFe_3N$
W	-41.081847	-41.536768	0.454921	$W^fFe_3N$
Cr	-42.386732	-42.943333	0.556601	$Cr^fFe_3N$
V	-42.431843	-43.040928	0.609085	$V^fFe_3N$

The energy difference  $\Delta E = E(M^cFe_3N) - E(M^fFe_3N)$ , where  $E(M^cFe_3N)$  represents the energy of  $M^cFe_3N$  with cubic structure, and  $E(M^fFe_3N)$  represents the energy of  $M^fFe_3N$  with tetragonal structure. When  $\Delta E < 0$ , the element  $M$  tends to replace  $Fe_I$ , showing space group of  $Pm-3m$ . When  $\Delta E > 0$ , the element  $M$  tends to replace  $Fe_{IIIB}$ , showing space group of  $P4/mmm$ .

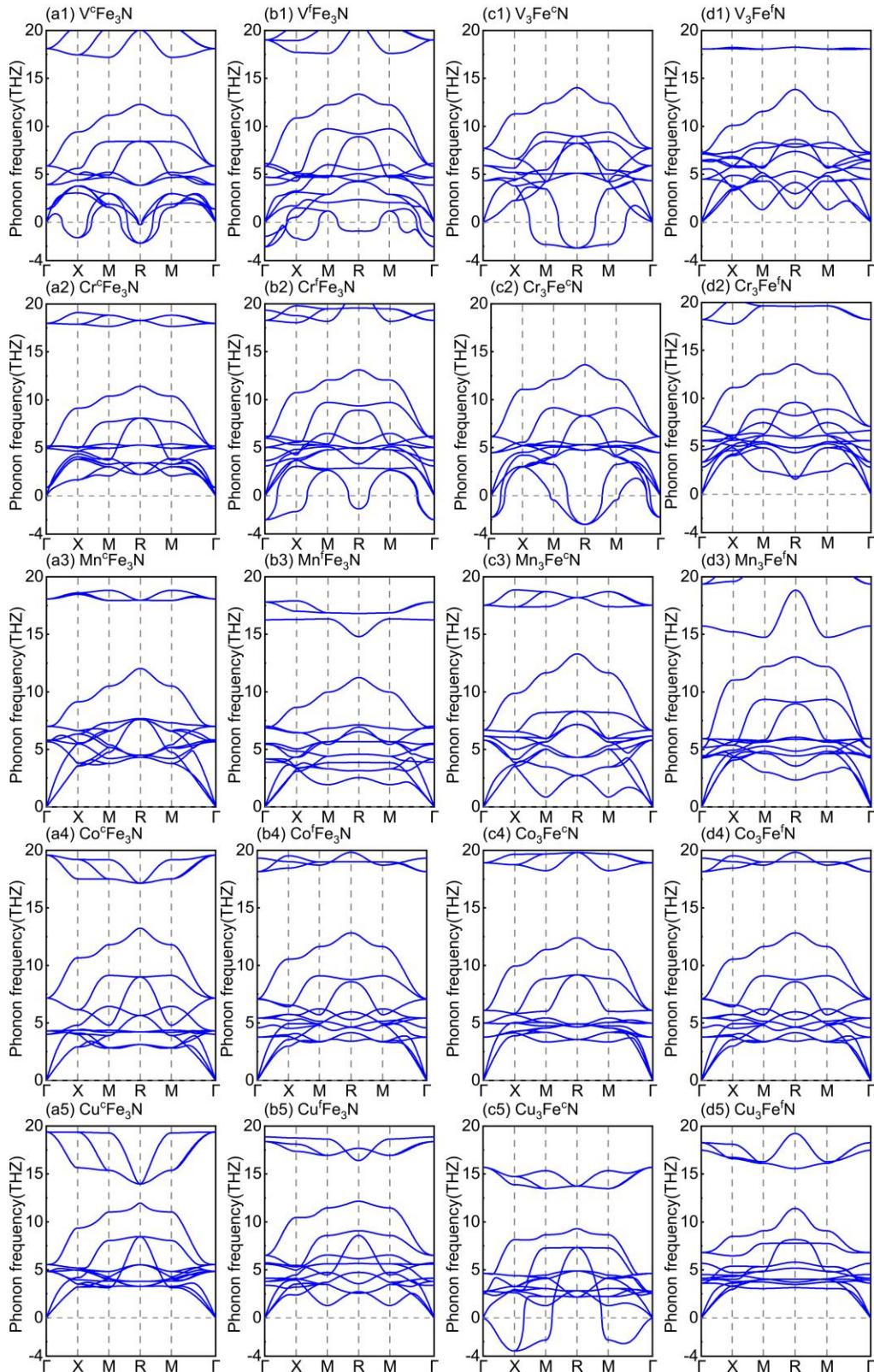
## S25. The priority occupancy of $M_3\text{FeN}$

**Table S4** The energy difference  $\Delta E = E_{(M_3\text{Fe}^c\text{N})} - E_{(M_3\text{Fe}^f\text{N})}$ , where  $E_{(M_3\text{Fe}^c\text{N})}$  represents the energy of  $M_3\text{Fe}^c\text{N}$  with cubic structure, and  $E_{(M_3\text{Fe}^f\text{N})}$  represents the energy of  $M_3\text{Fe}^f\text{N}$  with tetragonal structure. When  $\Delta E < 0$ , the element  $M$  tends to replace  $\text{Fe}_{\text{IIB}}$  and  $\text{Fe}_{\text{IIA}}$ , showing space group of  $Pm-3m$ . When  $\Delta E > 0$ , the element  $M$  tends to replace  $\text{Fe}_{\text{IIA}}$  and  $\text{Fe}_{\text{I}}$ , showing space group of  $P4/mmm$ .

Substitution element	$E_{(M_3\text{Fe}^c\text{N})}$	$E_{(M_3\text{Fe}^f\text{N})}$	$\Delta E = E_{(M_3\text{Fe}^c\text{N})} - E_{(M_3\text{Fe}^f\text{N})}$	Preferential occupancy site
Y	-30.514946	-28.535864	-1.979082	$\text{Y}_3\text{Fe}^c\text{N}$
Gd	-60.553204	-59.635418	-0.917786	$\text{Gd}_3\text{Fe}^c\text{N}$
V	-45.925756	-45.449720	-0.476036	$\text{V}_3\text{Fe}^c\text{N}$
Co	-37.674500	-37.592495	-0.082005	$\text{Co}_3\text{Fe}^c\text{N}$
Cr	-45.801819	-45.725603	-0.076216	$\text{Cr}_3\text{Fe}^c\text{N}$
Mn	-43.859310	-44.229587	0.370276	$\text{Mn}_3\text{Fe}^f\text{N}$
W	-41.509129	-42.308742	0.799613	$\text{W}_3\text{Fe}^f\text{N}$
Pt	-27.385084	-28.933959	1.548875	$\text{Pt}_3\text{Fe}^f\text{N}$
Cu	-25.067883	-26.830467	1.762584	$\text{Cu}_3\text{Fe}^f\text{N}$
Zn	-16.692228	-18.478715	1.786487	$\text{Zn}_3\text{Fe}^f\text{N}$

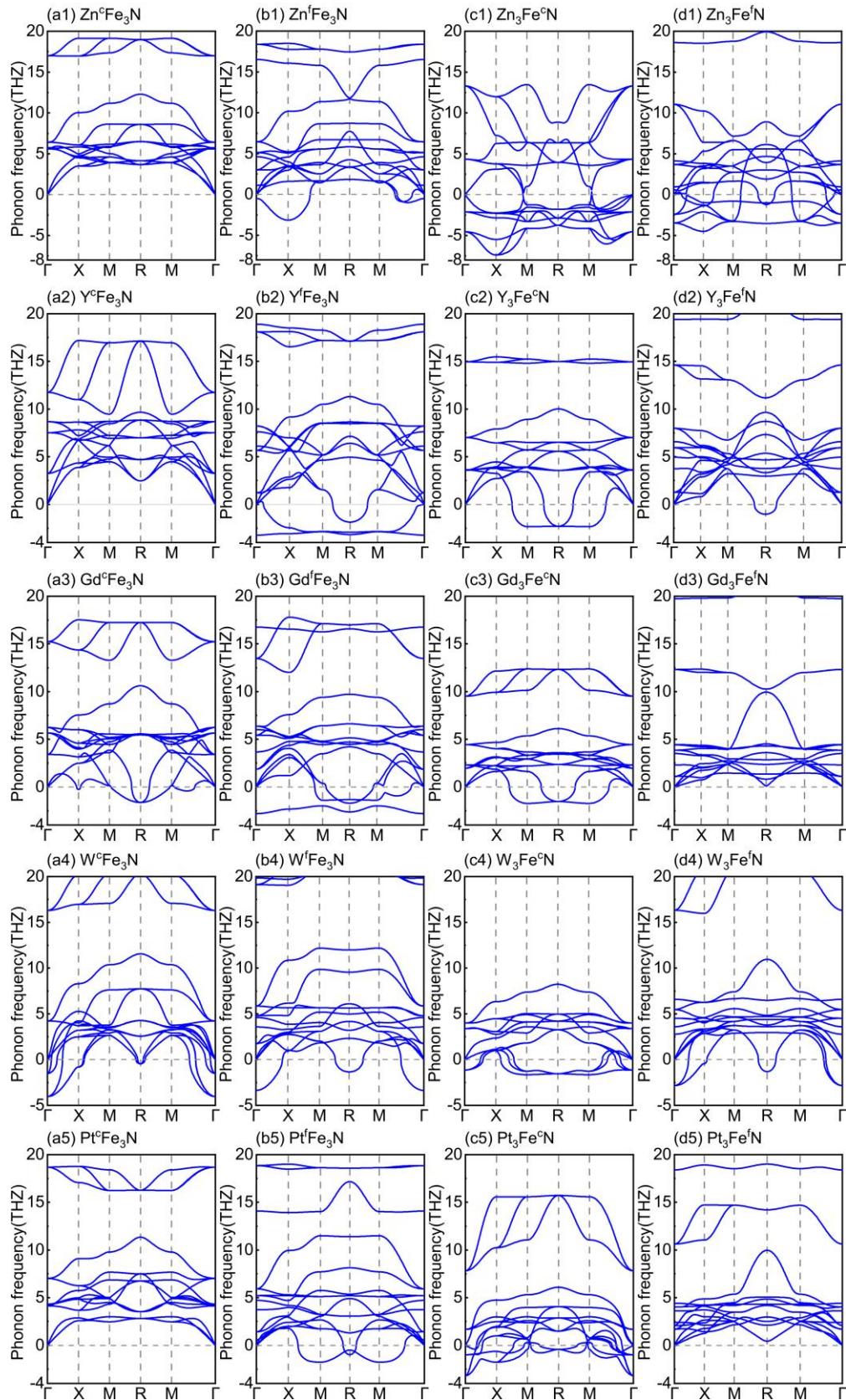
The energy difference  $\Delta E = E_{(M_3\text{Fe}^c\text{N})} - E_{(M_3\text{Fe}^f\text{N})}$ , where  $E_{(M_3\text{Fe}^c\text{N})}$  represents the energy of  $M_3\text{Fe}^c\text{N}$  with cubic structure, and  $E_{(M_3\text{Fe}^f\text{N})}$  represents the energy of  $M_3\text{Fe}^f\text{N}$  with tetragonal structure. When  $\Delta E < 0$ , the element  $M$  tends to replace  $\text{Fe}_{\text{IIB}}$  and  $\text{Fe}_{\text{IIA}}$ , showing space group of  $Pm-3m$ . When  $\Delta E > 0$ , the element  $M$  tends to replace  $\text{Fe}_{\text{IIA}}$  and  $\text{Fe}_{\text{I}}$ , showing space group of  $P4/mmm$ .

## S26. The phonopy of $M_xFe_{4-x}N$ ( $M = V, Cr, Mn, Co$ , and $Cu$ )



**Figure S22** The phonopy of (a1-d1)  $V_xFe_{4-x}N$ , (a2-d2)  $Cr_xFe_{4-x}N$ , (a3-d3)  $Mn_xFe_{4-x}N$ , (a4-d4),  $Co_xFe_{4-x}N$ , and (a5-d5)  $Cu_xFe_{4-x}N$  ( $x = 1$  or  $3$ ).

## S27. The phonopy of $M_xFe_{4-x}N$ ( $M = V, Cr, Mn, Co$ , and $Cu$ )



**Figure S23** The phonopy of (a1-d1)  $Zn_xFe_{4-x}N$ , (a2-d2)  $Y_xFe_{4-x}N$ , (a3-d3)  $Gd_xFe_{4-x}N$ , (a4-d4)  $W_xFe_{4-x}N$ , and (a5-d5)  $Pt_xFe_{4-x}N$  ( $x = 1$  or  $3$ ).