

## Supplementary Material

### Modeling the properties of lanthanoid single-ion magnets using an effective point-charge approach

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Energy (cm <sup>-1</sup> )	Wave function			
0	<b>1.00</b>   <b>-5</b> >	0.01·  <b>-1</b> >		
0	0.01·  <b>1</b> >	<b>1.00</b>   <b>5</b> >		
25	<b>0.71</b> ·  <b>-6</b> >	0.39·  <b>-2</b> >	0.39·  <b>2</b> >	<b>0.71</b> ·  <b>6</b> >
25	<b>0.71</b> ·  <b>-6</b> >	0.37·  <b>-2</b> >	0.37·  <b>2</b> >	<b>0.71</b> ·  <b>6</b> >
31	0.04·  <b>-8</b> >	<b>0.71</b> ·  <b>-4</b> >	<b>0.71</b> ·  <b>4</b> >	0.04·  <b>8</b> >
31	0.04·  <b>-8</b> >	<b>0.70</b> ·  <b>-4</b> >	<b>0.70</b> ·  <b>4</b> >	0.04·  <b>8</b> >
89	<b>0.79</b> ·  <b>-7</b> >	0.61·  <b>-3</b> >	0.01·  <b>1</b> >	
89	0.01·  <b>-1</b> >	0.61·  <b>3</b> >	<b>0.79</b> ·  <b>7</b> >	
110	0.61·  <b>-7</b> >	<b>0.79</b> ·  <b>-3</b> >	0.02·  <b>1</b> >	
110	0.02·  <b>-1</b> >	<b>0.79</b> ·  <b>3</b> >	0.61·  <b>7</b> >	
162	<b>0.92</b>   <b>-8</b> >	0.06  <b>-4</b> >	0.06  <b>4</b> >	0.39  <b>8</b> >
162	0.39  <b>-8</b> >	0.02  <b>-4</b> >	0.06  <b>4</b> >	<b>0.92</b>   <b>8</b> >
179	0.04·  <b>-6</b> >	<b>0.71</b> ·  <b>-2</b> >	<b>0.71</b> ·  <b>2</b> >	0.04·  <b>6</b> >
190	0.04·  <b>-6</b> >	<b>0.71</b> ·  <b>-2</b> >	<b>0.71</b> ·  <b>2</b> >	0.04·  <b>6</b> >
247	0.02·  <b>-5</b> >	<b>1.00</b>   <b>-1</b> >	0.03·  <b>3</b> >	
247	0.03·  <b>-3</b> >	<b>1.00</b>   <b>1</b> >	0.02·  <b>5</b> >	
270	<b>1.00</b>   <b>0</b> >			

**Table S.1:** Energies and modulus of the contribution of each  $M_J$  to the wave-functions of the ground state multiplets of HoPc<sub>2</sub>

Energy (cm <sup>-1</sup> )	Wave function			
0	0.01· -9/2>	<b>1.00· -1/2&gt;</b>	0.01· 7/2>	
0	0.01· -7/2>	<b>1.00· 1/2&gt;</b>	0.01· 9/2>	
58	0.05· -11/2>	<b>1.00· -3/2&gt;</b>	0.06· 5/2>	0.01· 13/2>
58	0.01· -13/2>	0.06· 5/2>	<b>1.00· 3/2&gt;</b>	0.05· 11/2>
79	<b>1.00· -15/2&gt;</b>	0.06· -7/2>		
79	0.06· 7/2>	<b>1.00· 15/2&gt;</b>		
129	<b>0.89· -13/2&gt;</b>	0.46· -5/2>	0.04· 3/2>	
129	0.04· -3/2>	0.46· 5/2>	<b>0.89· 13/2&gt;</b>	
159	0.46· -13/2>	<b>0.89· -5/2&gt;</b>	0.04· 3/2>	
159	0.04· -3/2>	<b>0.89· 5/2&gt;</b>	0.46· 13/2>	
234	<b>1.00· -11/2&gt;</b>	0.05· -3/2>		
234	0.05· -3/2>	<b>1.00· 11/2&gt;</b>		
240	0.06· -13/2>	<b>1.00· -7/2&gt;</b>	0.01· 1/2>	
240	0.01· -1/2>	<b>1.00· 7/2&gt;</b>	0.06· 13/2>	
275	<b>1.00· -9/2&gt;</b>	0.01· -1/2>		
275	0.01· 1/2>	<b>1.00· 9/2&gt;</b>		

**Table S.2:** Energies and modulus of the contribution of each  $M_J$  to the wave-functions of the ground state multiplets of ErPc<sub>2</sub>

Energy (cm <sup>-1</sup> )	Wave function			
0	0.01· -4>	<b>1.00· 0&gt;</b>	0.01· 4>	
3	<b>0.71· -6&gt;</b>	0.05· -2>	0.05· 2>	<b>0.71· 6&gt;</b>
3	<b>0.71· -6&gt;</b>	0.05· -2>	0.05· 2>	<b>0.71· 6&gt;</b>
18	0.01· -5>	<b>1.00· -1&gt;</b>	0.05· 3>	
18	0.05· -3>	<b>1.00· 1&gt;</b>	0.01· 5>	
69	0.07· -6>	<b>0.70· -2&gt;</b>	<b>0.70· 2&gt;</b>	0.07· 6>
88	0.05· -6>	<b>0.71· -2&gt;</b>	<b>0.71· 2&gt;</b>	0.05· 6>
178	<b>1.00· -3&gt;</b>	0.05· 1>		
178	0.05· -1>	<b>1.00· 3&gt;</b>		
291	<b>0.71· -4&gt;</b>	<b>0.71· 4&gt;</b>		
291	<b>0.71· -4&gt;</b>	<b>0.71· 4&gt;</b>		
312	<b>1.00· -5&gt;</b>	0.01· 1>		
312	0.01· -1>	<b>1.00· 5&gt;</b>		

**Table S.3:** Energies and modulus of the contribution of each  $M_J$  to the wave-functions of the ground state multiplets of TmPc<sub>2</sub>

Energy ( $\text{cm}^{-1}$ )	Wave function	
0	<b>1.00</b> · $ -5/2\rangle$	0.04· $ 3/2\rangle$
0	0.04· $ -3/2\rangle$	<b>1.00</b> · $ 5/2\rangle$
224	<b>1.00</b> · $ -3/2\rangle$	0.04· $ 5/2\rangle$
224	0.04· $ -5/2\rangle$	<b>1.00</b> · $ 3/2\rangle$
366	<b>0.92</b> · $ -7/2\rangle$	0.38· $ 1/2\rangle$
366	0.38· $ -1/2\rangle$	<b>0.92</b> · $ 7/2\rangle$
372	0.38· $ -7/2\rangle$	<b>0.92</b> · $ 3/2\rangle$
372	<b>0.92</b> · $ -3/2\rangle$	0.38· $ 7/2\rangle$

**Table S.4:** Energies and modulus of the contribution of each  $M_J$  to the wave-functions of the ground state multiplets of  $\text{YbPc}_2$