

Supplementary Information Figures S1-S5

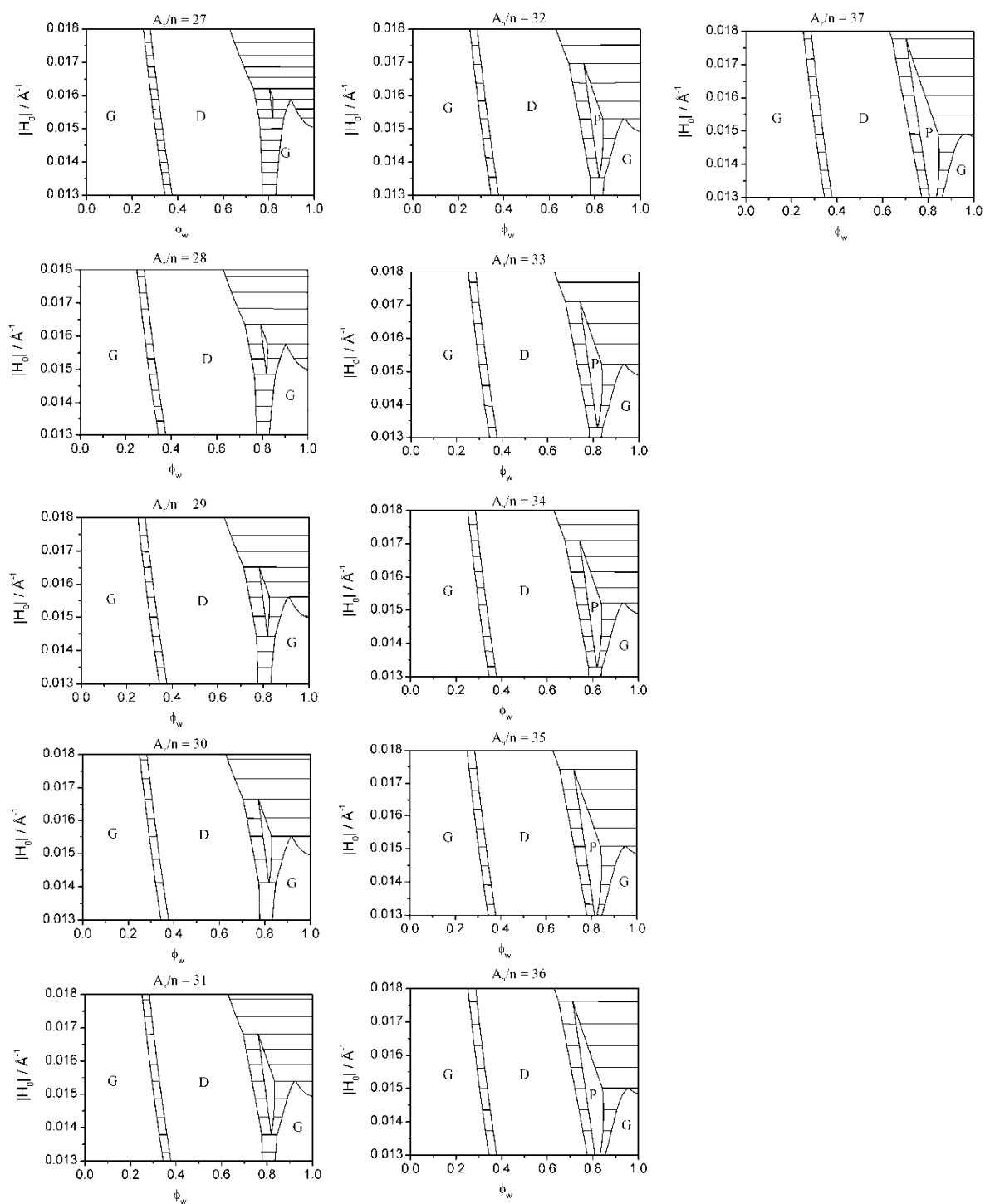


Figure S1. Partial theoretical phase diagrams, where the magnitude of H_0 ($|H_0|$) is acting as a first order proxy for temperature, for which $A_n/v = 0.06 \text{ \AA}^{-1}$, $v_n/v = 0.74$, $\kappa_G/\kappa = -0.75$ and $\lambda/\kappa = 0.0005 \text{ \AA}^{-2}$, with A_n/n varying between 27 \AA^2 and 37 \AA^2 .

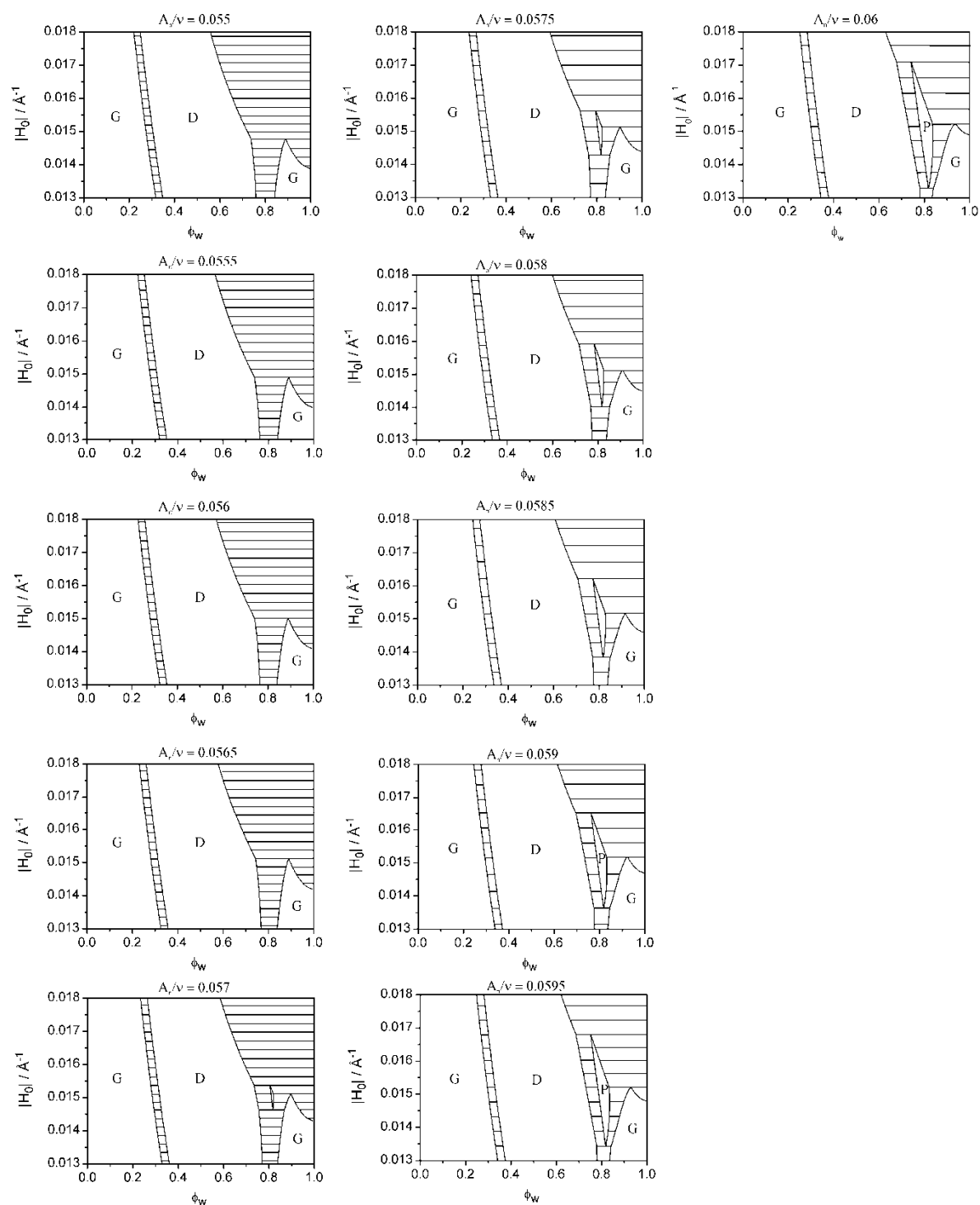


Figure S2. Partial theoretical phase diagrams, where $|H_0|$ is acting as a first order proxy for temperature, for which $A_n/n = 33 \text{ \AA}^2$, $v_n/v = 0.74$, $\kappa_G/\kappa = -0.75$ and $\lambda/\kappa = 0.0005 \text{ \AA}^{-2}$, with A_n/v varying between 0.055 \AA^{-1} and 0.06 \AA^{-1} .

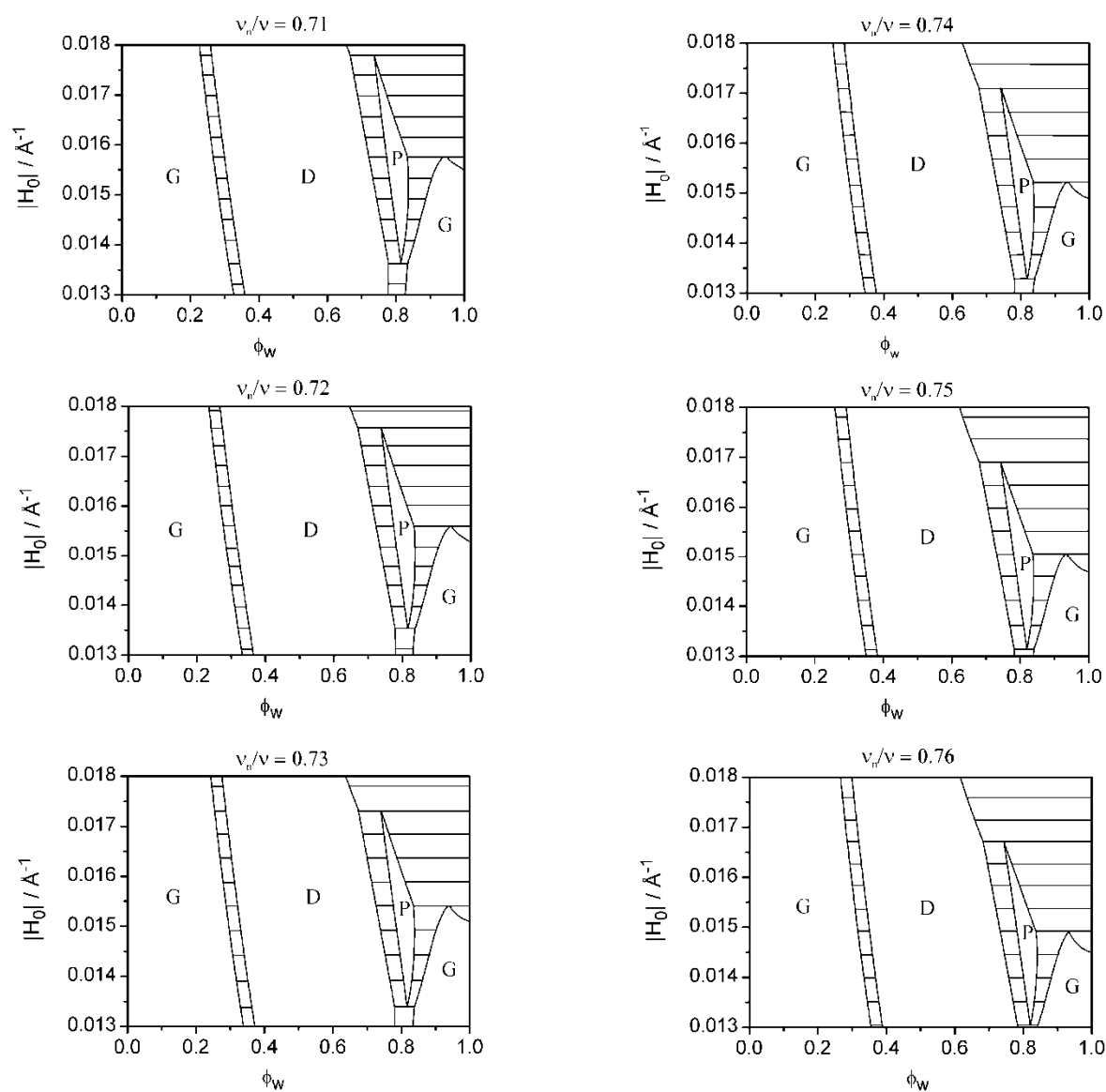


Figure S3. Partial theoretical phase diagrams, where $|H_0|$ is acting as a first order proxy for temperature, for which $A_n/n = 33 \text{ \AA}^2$, $A_n/v = 0.06 \text{ \AA}^{-1}$, $\kappa_G/\kappa = -0.75$ and $\lambda/\kappa = 0.0005 \text{ \AA}^{-2}$, with v_n/v varying between 0.71 and 0.76.

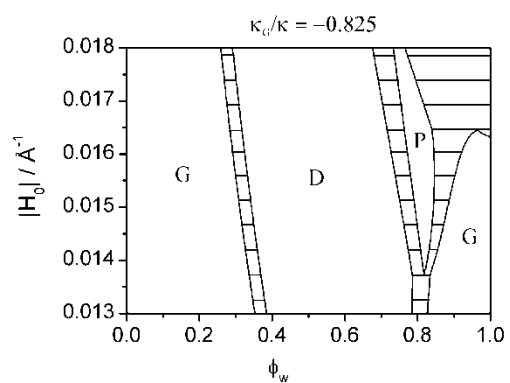
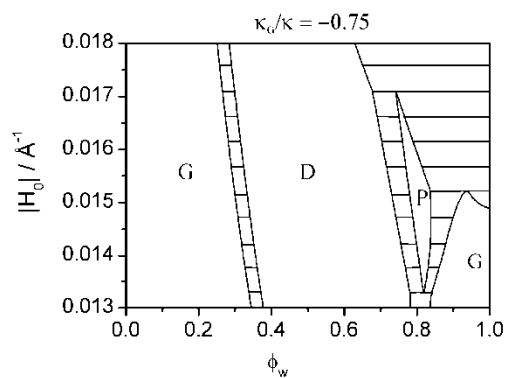
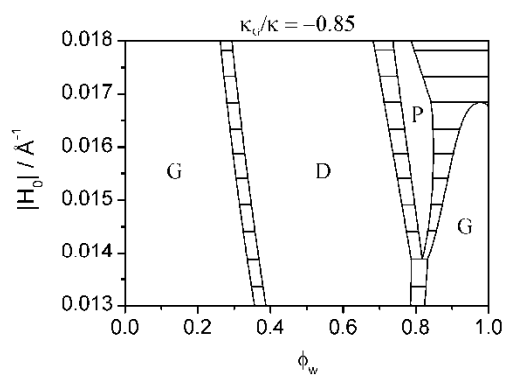
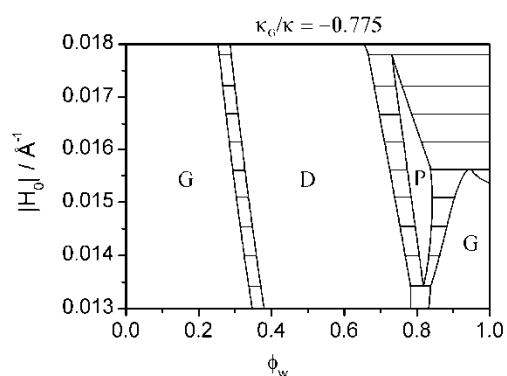
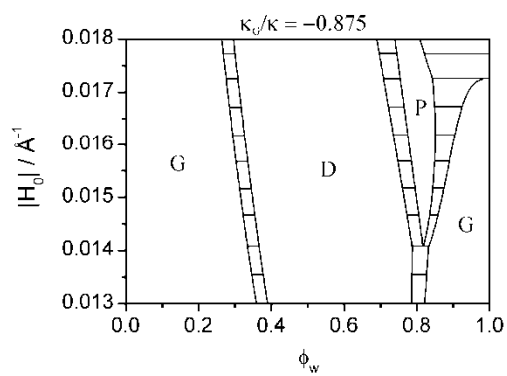
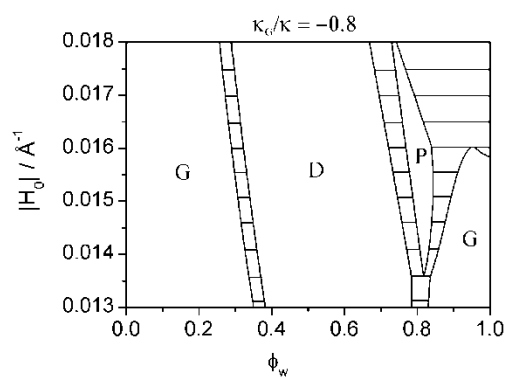
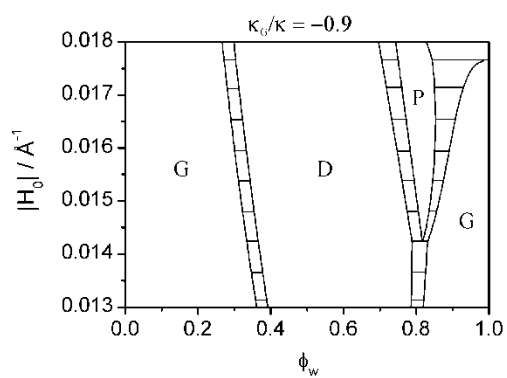


Figure S4. Partial theoretical phase diagrams, where $|H_0|$ is acting as a first order proxy for temperature, for which $A_n/n = 33 \text{ \AA}^2$, $A_n/v = 0.06 \text{ \AA}^{-1}$, $v_n/v = 0.74$ and $\lambda/\kappa = 0.0005 \text{ \AA}^{-2}$, with κ_G/κ varying between -0.9 and -0.75.

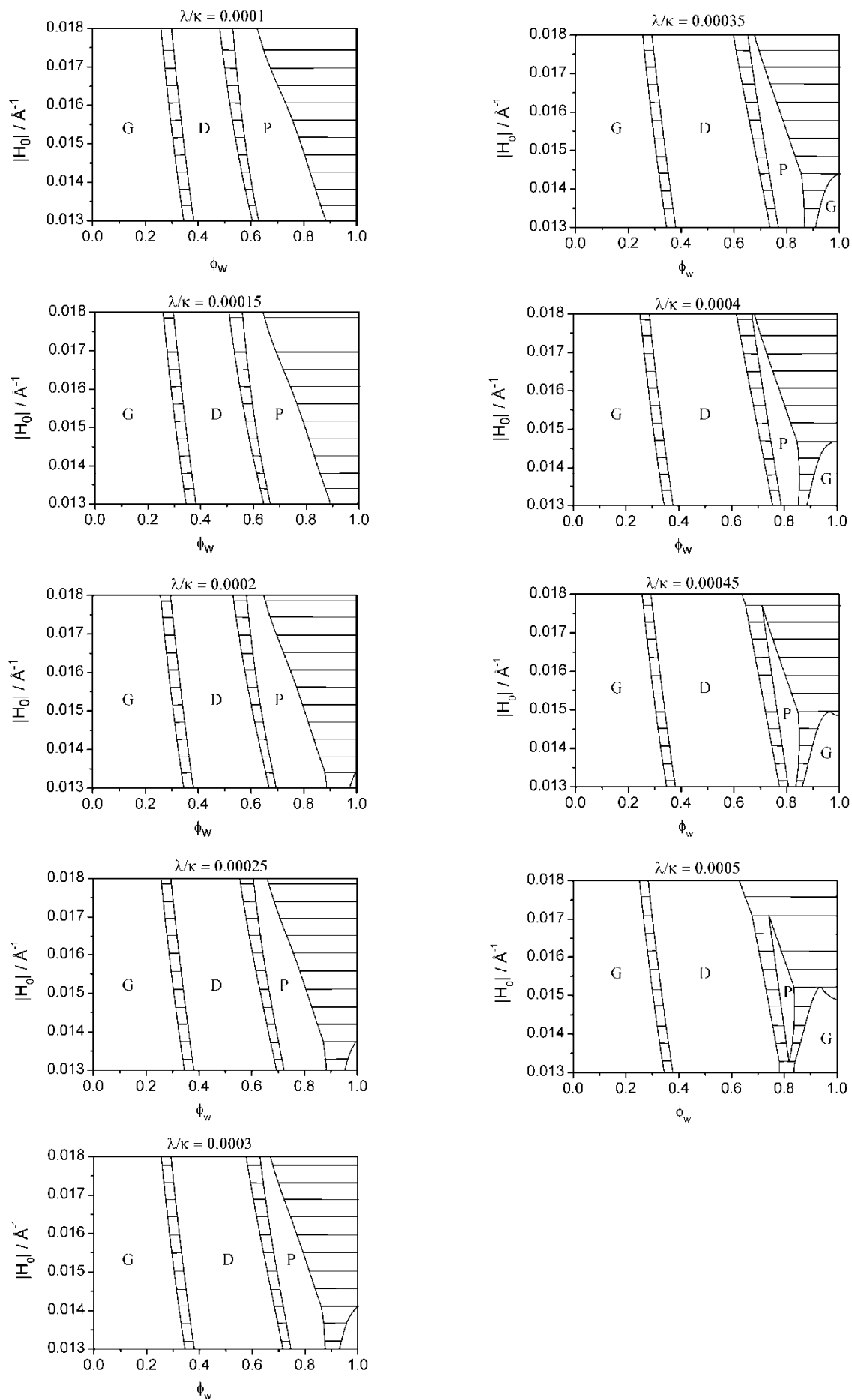


Figure S5. Partial theoretical phase diagrams, where $|H_0|$ is acting as a first order proxy for temperature, for which $A_n/n = 33 \text{ \AA}^2$, $A_n/\nu = 0.06 \text{ \AA}^{-1}$, $\nu_n/\nu = 0.74$ and $\kappa_G/\kappa = -0.75$, with λ/κ varying between 0.0001 \AA^{-2} and 0.0005 \AA^{-2} .

Mathematica Code:

Off[General::spell]

Off[General::spell1]

 $\mu c := \text{Apdivn}*(2*(\text{Hp} - \text{H0})^2 + \kappa \text{Gdiv}\kappa*\text{Kn})$ $\Theta := (\text{vpdivv})*(1 - \phi)$ $\text{suma} := (\sigma a*(\Theta)^0) + (\sigma b*(\Theta)^2) + (\sigma c*(\Theta)^4) + (\sigma d*(\Theta)^6)$ $\text{secsum} := (\zeta a*(\Theta^1)) + (\zeta b*(\Theta^3)) + (\zeta c*(\Theta^5)) + (\zeta d*(\Theta^7)) + (\zeta e*(\Theta^9))$ $a := (2/\text{Apdivv})*(1/(1 - \phi))*\text{suma}$ $\text{Hp} := -\text{secsum} / a$ $\text{Sn} := (\text{Apdivv}/2)*((a^3)*(1 - \phi))$ $\text{Kn} := 2*\pi*\chi / \text{Sn}$ $\text{diamond} := 0.000337618(1 - \phi)^2 + 0.0000337858(1 - \phi)^4 - 0.000489167(1 - \phi)^6 + 0.00216436(1 - \phi)^8$ $\text{primitive} := 0.000210286(1 - \phi)^2 + 0.00258955(1 - \phi)^4 - 0.0166996(1 - \phi)^6 + 0.125123(1 - \phi)^8$ $\text{gyroid} := 0.00010488(1 - \phi)^2 + 0.000356135(1 - \phi)^4 - 0.00228924(1 - \phi)^6 + 0.00450621(1 - \phi)^8$ $\text{varprimfapc} := \text{primitive}*a^2 / . \sigma a \rightarrow 2.3451 / . \sigma b \rightarrow -1.1713 / . \sigma c \rightarrow -0.22227 / . \sigma d \rightarrow -2.4952$ $\text{vardiafapc} := \text{diamond}*a^2 / . \sigma a \rightarrow 1.9189 / . \sigma b \rightarrow -0.8893 / . \sigma c \rightarrow -0.061856 / . \sigma d \rightarrow -0.65474$ $\text{vargyrfapc} := \text{gyroid}*a^2 / . \sigma a \rightarrow 3.0915 / . \sigma b \rightarrow -1.3317 / . \sigma c \rightarrow -0.19974 / . \sigma d \rightarrow -0.80113$ $\mu_{fp} := \lambda \text{div}\kappa*\text{varprimfapc}$ $\mu_{fd} := \lambda \text{div}\kappa*\text{vardiafapc}$ $\mu_{fg} := \lambda \text{div}\kappa*\text{vargyrfapc}$ $\text{da} := a / . \sigma a \rightarrow 1.9189 / . \sigma b \rightarrow -0.8893 / . \sigma c \rightarrow -0.061856 / . \sigma d \rightarrow -0.65474 / . \zeta a \rightarrow 1.8379 / . \zeta b \rightarrow -0.17345 / . \zeta c \rightarrow 16.508 / . \zeta d \rightarrow -62.547 / . \zeta e \rightarrow 76.638 / . \chi \rightarrow -2$ $\text{pa} := a / . \sigma a \rightarrow 2.3451 / . \sigma b \rightarrow -1.1713 / . \sigma c \rightarrow -0.22227 / . \sigma d \rightarrow -2.4952 / . \zeta a \rightarrow 3.0458 / . \zeta b \rightarrow -14.256 / . \zeta c \rightarrow 237.3 / . \zeta d \rightarrow -1365.6 / . \zeta e \rightarrow 2719.7 / . \chi \rightarrow -4$ $\text{ga} := a / . \sigma a \rightarrow 3.0915 / . \sigma b \rightarrow -1.3317 / . \sigma c \rightarrow -0.19974 / . \sigma d \rightarrow -0.80113 / . \zeta a \rightarrow 2.7953 / . \zeta b \rightarrow -9.9778 / . \zeta c \rightarrow 59.478 / . \zeta d \rightarrow -111.96 / . \zeta e \rightarrow 74.685 / . \chi \rightarrow -8$ $\text{d}\mu c := \mu c / . \sigma a \rightarrow 1.9189 / . \sigma b \rightarrow -0.8893 / . \sigma c \rightarrow -0.061856 / . \sigma d \rightarrow -0.65474 / . \zeta a \rightarrow 1.8379 / . \zeta b \rightarrow -0.17345 / . \zeta c \rightarrow 16.508 / . \zeta d \rightarrow -62.547 / . \zeta e \rightarrow 76.638 / . \chi \rightarrow -2$ $\text{p}\mu c := \mu c / . \sigma a \rightarrow 2.3451 / . \sigma b \rightarrow -1.1713 / . \sigma c \rightarrow -0.22227 / . \sigma d \rightarrow -2.4952 / . \zeta a \rightarrow 3.0458 / . \zeta b \rightarrow -14.256 / . \zeta c \rightarrow 237.3 / . \zeta d \rightarrow -1365.6 / . \zeta e \rightarrow 2719.7 / . \chi \rightarrow -4$ $\text{g}\mu c := \mu c / . \sigma a \rightarrow 3.0915 / . \sigma b \rightarrow -1.3317 / . \sigma c \rightarrow -0.19974 / . \sigma d \rightarrow -0.80113 / . \zeta a \rightarrow 2.7953 / . \zeta b \rightarrow -9.9778 / . \zeta c \rightarrow 59.478 / . \zeta d \rightarrow -111.96 / . \zeta e \rightarrow 74.685 / . \chi \rightarrow -8$ $\mu_{\text{ptot}} := \mu_{fp} + \text{p}\mu c$ $\mu_{\text{dtot}} := \mu_{fd} + \text{d}\mu c$ $\mu_{\text{gtot}} := \mu_{fg} + \text{g}\mu c$

The phase diagram can be determined from free energy graphs by obtaining the common tangent lines between different phases - where the common tangent touches the curve becomes the point at

which the phases mix in each case. In order to determine the common tangent line, one must equate both the gradients and the y-intercepts and then solve the simultaneous equation. The excess water point can be determined by finding the minimum of each of the free energy curves by differentiating and equating to zero (to find a turning point). These can then be compared to each other to find the one which lies at the lowest energy.

Please change the OpenWrite and Import addresses to more suitable ones of your preference.

```
phasematrix = OpenWrite["C:\phasematrix_t", FormatType -> OutputForm];
yphasematrix = OpenWrite["C:\yphasematrix_t", FormatType -> OutputForm, PageWidth -> 200];
```

We need to initialise the starting values first, then increment them as:

H₀ varies as the spontaneous radius of curvature ratio of 0.2A/K

An/n increases 0.17%/K

An/v increases 0.09%/K

vn/v does not change

Kg/K scales as (An/n)^{-2.5}

lambda/K scales as (An/n)^{7.5}

Here we have set our initial R₀ value as 35, but this can be changed.

```
Do[
Clear[phaserec];
gtopsecboundl = 10;
gtodsecboundl = 10;
dtopsecboundl = 10;
dtogsecboundl = 10;
ptodsecboundl = 10;
ptogsecboundl = 10;
Apsdivn = 33 + 33*(0.0017*k);
vpsdiv = 0.76;
Apsdivv = 0.057 + 0.057*(0.0009*k);
κGdivκ = -0.75*((Apsdivn/33)^(-2.5));
λdivκ = 0.00035*((Apsdivn/33)^(7.5));
T = k;
R0 = (35 - 0.2 k);
H0 = -1/2/R0;
diffp = D[μptot, φ];
diffd = D[μdtot, φ];
diffg = D[μgtot, φ];
pmin = FindRoot[diffp == 0, {φ, 0.1}, MaxIterations -> 200];
dmin = FindRoot[diffd == 0, {φ, 0.1}, MaxIterations -> 200];
gmin = FindRoot[diffg == 0, {φ, 0.1}, MaxIterations -> 200];
γμptot = μptot /. φ -> a1;
γμdtot = μdtot /. φ -> b;
γμgtot = μgtot /. φ -> c;
diffpal = diffp /. φ -> a1;
diffdb = diffd /. φ -> b;
diffgc = diffg /. φ -> c;
yintp = γμptot - (diffpal*a1);
yintd = γμdtot - (diffdb*b);
yintg = γμgtot - (diffgc*c);
```

```
record[1] = T;
record[2] =  $\phi$  /. pmin[[1]];
record[3] =  $\phi$  /. dmin[[1]];
record[4] =  $\phi$  /. gmin[[1]];
phaserec[1] = T;
ypmin =  $\mu$ ptot /.  $\phi$  -> record[2];
ydmin =  $\mu$ dtot /.  $\phi$  -> record[3];
ygmin =  $\mu$ gtot /.  $\phi$  -> record[4];
If[ypmin < ydmin && ypmin < ygmin,
phaserec[2] = record[2];
If[record[2] > 0.999,
phaserec[2] = 1]];
If[ydmin < ypmin && ydmin < ygmin,
phaserec[2] = record[3];
If[record[3] > 0.999,
phaserec[2] = 1]];
If[ygmin < ypmin && ygmin < ydmin,
phaserec[2] = record[4];
If[record[4] > 0.999,
phaserec[2] = 1]];
player = Array[record, 4];
t = 1;
n = 0;
Do[
If[ $\mu$ gtot <  $\mu$ dtot, w = 1];
If[ $\mu$ dtot <  $\mu$ gtot, w = 3];
If[t  $\neq$  w && t == 1 && w == 3,
n = n + 1;
m = (3*(n - 1));
record[m + 5] = t;
record[m + 6] = w;
record[m + 7] =  $\phi$ ;
];
If[t  $\neq$  w && t == 3 && w == 1,
n = n + 1;
n = n + 1;
m = (3*(n - 1));
record[m + 5] = t;
record[m + 6] = w;
record[m + 7] =  $\phi$ ;
];
t = w;
Null, { $\phi$ , 0.226, 0.5, 0.001}}
Do[
If[ $\mu$ gtot <  $\mu$ dtot &&  $\mu$ gtot <  $\mu$ ptot, w = 1];
If[ $\mu$ ptot <  $\mu$ gtot &&  $\mu$ ptot <  $\mu$ dtot, w = 2];
If[ $\mu$ dtot <  $\mu$ gtot &&  $\mu$ dtot <  $\mu$ ptot, w = 3];
If[t  $\neq$  w && t == 1 && w == 2,
n = n + 1;
m = (3*(n - 1));
```

```
record[m + 5] = t;
record[m + 6] = w;
record[m + 7] =  $\phi$ ;
];
If[t  $\neq$  w && t == 2 && w == 1,
n = n + 1;
m = (3*(n - 1));
record[m + 5] = t;
record[m + 6] = w;
record[m + 7] =  $\phi$ ;
];
If[t  $\neq$  w && t == 1 && w == 3,
n = n + 1;
m = (3*(n - 1));
record[m + 5] = t;
record[m + 6] = w;
record[m + 7] =  $\phi$ ;
];
If[t  $\neq$  w && t == 3 && w == 1,
n = n + 1;
m = (3*(n - 1));
record[m + 5] = t;
record[m + 6] = w;
record[m + 7] =  $\phi$ ;
];
If[t  $\neq$  w && t == 2 && w == 3,
n = n + 1;
m = (3*(n - 1));
record[m + 5] = t;
record[m + 6] = w;
record[m + 7] =  $\phi$ ;
];
If[t  $\neq$  w && t == 3 && w == 2,
n = n + 1;
m = (3*(n - 1));
record[m + 5] = t;
record[m + 6] = w;
record[m + 7] =  $\phi$ ;
];
t = w;
Null, { $\phi$ , 0.5, 0.999, 0.001}
j = 0;
Do[
phaserec[i] = 1;
Null, {i, 3, (2 n) + 2}];
Do[
m = (3*(i - 1));
If[record[m + 5] == 1 && record[m + 6] == 3 && record[m + 7] < phaserec[2],
gtod = FindRoot[{diffgc == diffdb, yintg == yintd}, {c, record[m + 7] - 0.05, 0.112, 1}, {b, record[m + 7]
+ 0.05, 0.226, 1}, MaxIterations -> 200];
```

```
gtodboundl = c /. gtod[[1]];
gtodboundr = b /. gtod[[2]];
ygtodboundl =  $\gamma\mu$ gtot /. c -> gtodboundl;
ygtodboundr =  $\gamma\mu$ dtot /. b -> gtodboundr;
slopegtod = (ygtodboundr - ygtodboundl)/(gtodboundr - gtodboundl);
If[record[m + 5] == 1 && record[m + 6] == 3 && record[m + 8] == 3 && record[m + 9] == 2 &&
record[m + 10] < phaserec[2],
gtopsec = FindRoot[{diffpal == diffgc, yintp == yintg}, {c, record[m + 7], 0.112, 1}, {al, record[m + 10],
0.5, 1}, MaxIterations -> 200];
gtopsecboundl = c /. gtopsec[[1]];
gtopsecboundr = al /. gtopsec[[2]];
If[gtopsecboundl > 0.112 && gtopsecboundl < 1 && gtopsecboundr > 0.5 && gtopsecboundr < 1,
ygtopsecboundl =  $\gamma\mu$ gtot /. c -> gtopsecboundl;
ygtopsecboundr =  $\gamma\mu$ ptot /. al -> gtopsecboundr;
slopegtopsec = (ygtopsecboundr - ygtopsecboundl)/(gtopsecboundr - gtopsecboundl);
If[slopegtopsec < slopegtod,
j = j + 1;
phaserec[(2 (j - 1)) + 3] = gtopsecboundl;
phaserec[(2 (j - 1)) + 4] = gtopsecboundr;
];
];
];
If[record[m + 5] == 1 && record[m + 6] == 3 && record[m + 2] == 2 && record[m + 3] == 1 &&
record[m + 6] < phaserec[2] && phaserec[(2 (j - 1)) + 3] == ptodsecboundl,
j = j + 1;
phaserec[(2 (j - 1)) + 3] = ptodsecboundl;
phaserec[(2 (j - 1)) + 4] = ptodsecboundr;
];
If[ygtodboundl > ygtodboundr && phaserec[(2 (j - 1)) + 3]  $\neq$  gtopsecboundl && phaserec[(2 (j - 1)) +
3]  $\neq$  ptodsecboundl,
j = j + 1;
phaserec[(2 (j - 1)) + 3] = gtodboundl;
phaserec[(2 (j - 1)) + 4] = gtodboundr;
];
];
If[record[m + 5] == 3 && record[m + 6] == 1 && record[m + 7] < phaserec[2],
dtog = FindRoot[{diffdb == diffpal, yintd == yintp}, {b, record[m + 7] - 0.05, 0.226, 1}, {c, record[m + 7]
+ 0.05, 0.112, 1}, MaxIterations -> 200];
dtogboundl = b /. dtog[[1]];
dtogboundr = c /. dtog[[2]];
ydtogboundl =  $\gamma\mu$ dtot /. b -> dtogboundl;
ydtogboundr =  $\gamma\mu$ gtot /. c -> dtogboundr;
slopedtog = (ydtogboundr - ydtogboundl)/(dtogboundr - dtogboundl);
If[record[m + 5] == 3 && record[m + 6] == 1 && record[m + 8] == 1 && record[m + 9] == 2 &&
record[m + 10] < phaserec[2],
dtopsec = FindRoot[{diffdb == diffpal, yintd == yintp}, {b, record[m + 7], 0.226, 1}, {al, record[m + 10],
0.5, 1}, MaxIterations -> 200];
dtopsecboundl = b /. dtopsec[[1]];
dtopsecboundr = al /. dtopsec[[2]];
If[dtopsecboundl > 0.226 && dtopsecboundl < 1 && dtopsecboundr > 0.5 && dtopsecboundr < 1,
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ydtopsecboundl =  $\gamma\mu dtot / . b \rightarrow dtopsecboundl$ ;
ydtopsecboundr =  $\gamma\mu ptot / . al \rightarrow dtopsecboundr$ ;
slopedtopsec = (ydtopsecboundr - ydtopsecboundl)/(dtopsecboundr - dtopsecboundl);
If[slopedtopsec < slopedtog,
j = j + 1;
phaserec[(2 (j - 1)) + 3] = dtopsecboundl;
phaserec[(2 (j - 1)) + 4] = dtopsecboundr;
];
];
];
If[record[m + 5] == 3 && record[m + 6] == 1 && record[m + 2] == 2 && record[m + 3] == 3 &&
record[m + 6] < phaserec[2] && phaserec[(2 (j - 1)) + 3] == ptogsecboundl,
j = j + 1;
phaserec[(2 (j - 1)) + 3] = ptogsecboundl;
phaserec[(2 (j - 1)) + 4] = ptogsecboundr;
];
If[ydtogboundl > ydtogboundr && phaserec[(2 (j - 1)) + 3]  $\neq$  dtopsecboundl && phaserec[(2 (j - 1)) +
3]  $\neq$  ptogsecboundl,
j = j + 1;
phaserec[(2 (j - 1)) + 3] = dtogboundl;
phaserec[(2 (j - 1)) + 4] = dtogboundr;
];
];
If[record[m + 5] == 1 && record[m + 6] == 2 && record[m + 7] < phaserec[2],
gtop = FindRoot[{diffpal == diffgc, yintp == yintg}, {c, record[m + 7] - 0.05, 0.112, 1}, {al, record[m +
7] + 0.05, 0.5, 1}, MaxIterations -> 200];
gtopboundl = c /. gtop[[1]];
gtopboundr = al /. gtop[[2]];
ygtopboundl =  $\gamma\mu gtot / . c \rightarrow gtopboundl$ ;
ygtopboundr =  $\gamma\mu ptot / . al \rightarrow gtopboundr$ ;
slopegtop = (ygtopboundr - ygtopboundl)/(gtopboundr - gtopboundl);
If[record[m + 5] == 1 && record[m + 6] == 2 && record[m + 8] == 2 && record[m + 9] == 3 &&
record[m + 10] < phaserec[2],
gtodsec = FindRoot[{diffgc == diffdb, yintg == yintd}, {c, record[m + 7], 0.112, 1}, {b, record[m + 10],
0.226, 1}, MaxIterations -> 200];
gtodsecboundl = c /. gtodsec[[1]];
gtodsecboundr = b /. gtodsec[[2]];
If[gtodsecboundl > 0.112 && gtodsecboundl < 1 && gtodsecboundr > 0.226 && gtodsecboundr < 1,
ygtodsecboundl =  $\gamma\mu gtot / . c \rightarrow gtodsecboundl$ ;
ygtodsecboundr =  $\gamma\mu dtot / . b \rightarrow gtodsecboundr$ ;
slopegtodsec = (ygtodsecboundr - ygtodsecboundl)/(gtodsecboundr - gtodsecboundl);
If[slopegtodsec < slopegtog,
j = j + 1;
phaserec[(2 (j - 1)) + 3] = gtodsecboundl;
phaserec[(2 (j - 1)) + 4] = gtodsecboundr;
];
];
];
If[record[m + 5] == 1 && record[m + 6] == 2 && record[m + 2] == 3 && record[m + 3] == 1 &&
record[m + 6] < phaserec[2] && phaserec[(2 (j - 1)) + 3] == dtopsecboundl,

```

```
j = j + 1;
phaserec[(2 (j - 1)) + 3] = dtopsecboundl;
phaserec[(2 (j - 1)) + 4] = dtopsecboundr;
];
If[ygtopboundl > ygtopboundr && phaserec[(2 (j - 1)) + 3] ≠ gtodsecboundl && phaserec[(2 (j - 1)) +
3] ≠ dtopsecboundl,
j = j + 1;
phaserec[(2 (j - 1)) + 3] = gtopboundl;
phaserec[(2 (j - 1)) + 4] = gtopboundr;
];
];
If[record[m + 5] == 2 && record[m + 6] == 1 && record[m + 7] < phaserec[2],
ptog = FindRoot[{diffpal == diffgc, yintp == yintg}, {al, record[m + 7] - 0.05, 0.5, 1}, {c, record[m + 7] +
0.05, 0.112, 1}, MaxIterations -> 200];
ptogboundl = al /. ptog[[1]];
ptogboundr = c /. ptog[[2]];
yptogboundl =  $\gamma \mu$ ptot /. al -> ptogboundl;
yptogboundr =  $\gamma \mu$ gtot /. c -> ptogboundr;
slopeptog = (yptogboundr - yptogboundl)/(ptogboundr - ptogboundl);
If[record[m + 5] == 2 && record[m + 6] == 1 && record[m + 8] == 1 && record[m + 9] == 3 &&
record[m + 10] < phaserec[2],
ptodsec = FindRoot[{diffdb == diffpal, yintd == yintp}, {al, record[m + 7], 0.5, 1}, {b, record[m + 10], -
0.226, 1}, MaxIterations -> 200];
ptodsecboundl = al /. ptodsec[[1]];
ptodsecboundr = b /. ptodsec[[2]];
If[ptodsecboundl > 0.5 && ptodsecboundl < 1 && ptodsecboundr > 0.226 && ptodsecboundr < 1,
yptodsecboundl =  $\gamma \mu$ ptot /. al -> ptodsecboundl;
yptodsecboundr =  $\gamma \mu$ dtot /. b -> ptodsecboundr;
slopeptodsec = (yptodsecboundr - yptodsecboundl)/(ptodsecboundr - ptodsecboundl);
If[slopeptodsec < slopeptog,
j = j + 1;
phaserec[(2 (j - 1)) + 3] = ptodsecboundl;
phaserec[(2 (j - 1)) + 4] = ptodsecboundr;
];
];
];
If[record[m + 5] == 2 && record[m + 6] == 1 && record[m + 2] == 3 && record[m + 3] == 2 &&
record[m + 6] < phaserec[2] && phaserec[(2 (j - 1)) + 3] == dtogsecboundl,
j = j + 1;
phaserec[(2 (j - 1)) + 3] = dtogsecboundl;
phaserec[(2 (j - 1)) + 4] = dtogsecboundr;
];
];
If[yptogboundl > yptogboundr && phaserec[(2 (j - 1)) + 3] ≠ ptodsecboundl && phaserec[(2 (j - 1)) +
3] ≠ dtogsecboundl,
j = j + 1;
phaserec[(2 (j - 1)) + 3] = ptogboundl;
phaserec[(2 (j - 1)) + 4] = ptogboundr;
];
];
```

```

If[record[m + 5] == 3 && record[m + 6] == 2 && record[m + 7] < phaserec[2],
dtop = FindRoot[{diffdb == diffpal, yintd == yintp}, {b, record[m + 7] - 0.05, 0.226, 1}, {a1, record[m +
7] + 0.05, 0.5, 1}, MaxIterations -> 200];
dtopboundl = b /. dtop[[1]];
dtopboundr = a1 /. dtop[[2]];
ydtotboundl =  $\gamma \mu dtot$  /. b -> dtopboundl;
ydtotboundr =  $\gamma \mu ptot$  /. a1 -> dtopboundr;
slopedtop = (ydtotboundr - ydtotboundl)/(dtopboundr - dtopboundl);
If[record[m + 5] == 3 && record[m + 6] == 2 && record[m + 8] == 2 && record[m + 9] == 1 &&
record[m + 10] < phaserec[2],
dtogsec = FindRoot[{diffgc == diffdb, yintg == yintd}, {b, record[m + 7], 0.226, 1}, {c, record[m + 10],
0.112, 1}, MaxIterations -> 200];
dtogsecboundl = b /. dtogsec[[1]];
dtogsecboundr = c /. dtogsec[[2]];
If[dtogsecboundl > 0.226 && dtogsecboundl < 1 && dtogsecboundr > 0.112 && dtogsecboundr < 1,
ydtogsecboundl =  $\gamma \mu dtot$  /. b -> dtogsecboundl;
ydtogsecboundr =  $\gamma \mu gtot$  /. c -> dtogsecboundr;
slopedtogsec = (ydtogsecboundr - ydtogsecboundl)/(dtogsecboundr - dtogsecboundl);
If[slopedtogsec < slopedtop,
j = j + 1;
phaserec[(2 (j - 1)) + 3] = dtogsecboundl;
phaserec[(2 (j - 1)) + 4] = dtogsecboundr;
];
];
];
If[record[m + 5] == 3 && record[m + 6] == 2 && record[m + 2] == 1 && record[m + 3] == 3 &&
record[m + 6] < phaserec[2] && phaserec[(2 (j - 1)) + 3] == gtopsecboundl,
j = j + 1;
phaserec[(2 (j - 1)) + 3] = gtopsecboundl;
phaserec[(2 (j - 1)) + 4] = gtopsecboundr;
];
If[ydtopboundl > ydtopboundr && phaserec[(2 (j - 1)) + 3]  $\neq$  dtogsecboundl && phaserec[(2 (j - 1)) +
3]  $\neq$  gtopsecboundl,
j = j + 1;
phaserec[(2 (j - 1)) + 3] = dtopboundl;
phaserec[(2 (j - 1)) + 4] = dtopboundr;
];
];
If[record[m + 5] == 2 && record[m + 6] == 3 && record[m + 7] < phaserec[2],
ptod = FindRoot[{diffdb == diffpal, yintd == yintp}, {a1, record[m + 7] - 0.05, 0.5, 1}, {b, record[m + 7]
+ 0.05, 0.226, 1}, MaxIterations -> 200];
ptodboundl = a1 /. ptod[[1]];
ptodboundr = b /. ptod[[2]];
yptodboundl =  $\gamma \mu ptot$  /. a1 -> ptodboundl;
yptodboundr =  $\gamma \mu dtot$  /. b -> ptodboundr;
slopeptod = (yptodboundr - yptodboundl)/(ptodboundr - ptodboundl);
If[record[m + 5] == 2 && record[m + 6] == 3 && record[m + 8] == 3 && record[m + 9] == 1 &&
record[m + 10] < phaserec[2],
ptogsec = FindRoot[{diffpal == diffgc, yintp == yintg}, {a1, record[m + 7], 0.5, 1}, {c, record[m + 10],
0.112, 1}, MaxIterations -> 200];

```

```

ptogsecboundl = a1 /. ptogsec[[1]];
ptogsecboundr = c /. ptogsec[[2]];
If[ptogsecboundl > 0.5 && ptogsecboundl < 1 && ptogsecboundr > 0.112 && ptogsecboundr < 1,
yptogsecboundl =  $\gamma\mu_{ptot}$  /. a1 -> ptogsecboundl;
yptogsecboundr =  $\gamma\mu_{gtot}$  /. c -> ptogsecboundr;
slopeptogsec = (yptogsecboundr - yptogsecboundl)/(ptogsecboundr - ptogsecboundl);
If[slopeptogsec < slopeptod,
j = j + 1;
phaserec[(2 (j - 1)) + 3] = ptogsecboundl;
phaserec[(2 (j - 1)) + 4] = ptogsecboundr;
];
];
];
If[record[m + 5] == 2 && record[m + 6] == 3 && record[m + 2] == 1 && record[m + 3] == 2 &&
record[m + 6] < phaserec[2] && phaserec[(2 (j - 1)) + 3] == gtodsecboundl,
j = j + 1;
phaserec[(2 (j - 1)) + 3] = gtodsecboundl;
phaserec[(2 (j - 1)) + 4] = gtodsecboundr;
];
If[yptodboundl > yptodboundr && phaserec[(2 (j - 1)) + 3]  $\neq$  ptogsecboundl && phaserec[(2 (j - 1)) +
3]  $\neq$  gtodsecboundl,
j = j + 1;
phaserec[(2 (j - 1)) + 3] = ptodboundl;
phaserec[(2 (j - 1)) + 4] = ptodboundr;
];
];
Null, {i, 1, n}
Do[
If[phaserec[i] > phaserec[2],
phaserec[i] = 1];
Null, {i, 3, (2 (j - 1)) + 4}];
Do[
Write[phasematrix, phaserec[i], " ", phaserec[1]];
Null, {i, 2, (2 (j - 1)) + 4}];
totalst = ToString[phaserec[1]];
Do[
stpart = ToString[phaserec[i]];
totalst = StringJoin[totalst, " ", stpart];
Null, {i, 2, (2 (j - 1)) + 4}];
Write[yphasematrix, totalst];
Null, {k, 0, 31, 0.5}
Close[phasematrix];
Close[yphasematrix];
phasedata = Import["C:\phasematrix_t", "Table"];
phaseplot = ListPlot[phasedata, DefaultFont -> {"Times", 8}, FrameLabel -> {" $\phi_w$ ", " $\Delta T / ^\circ C$ "},
FrameStyle -> AbsoluteThickness[0.5], DisplayFunction -> $DisplayFunction, Frame -> True,
PlotRange -> {{0, 0.995}, {0, 30}}, AxesOrigin -> {0, 0}];
Null

```